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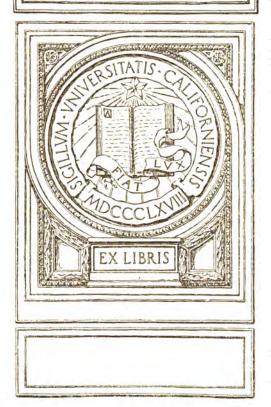
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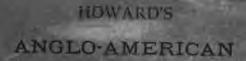
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C. FRUSHER/HOWARD,
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### NTRODUCTION.

HE perfection of Art will be the most apt and efficient system of Rules."—Karslake.

"Every Science is evolved out of its corresponding Art." "There must be practice and an accruing experience, with its empirical generalisations before there can be Science." "Progress from the simple to the complex, from the concrete to the abstract, from the empirical to the rational."—Herbert Spencer.

The ability to make business calculations with ease, accuracy, and speed, is an invaluable acquisition. The methods of Arithmetic used in schools are too tedious and complex for practical uses, they are weighted with superfluous elements that needlessly encumber the operations and distract and confuse the learner: the Rules in this New Art of Reckoning omit the needless work, and by an easily-learned, simple, and natural arrangement, lead directly to the required answer.

They are especially adapted to that large class of persons who find it difficult, or impossible, mentally to grasp, and retain complex numbers; such persons will find in this book

"A Complete Teacher of Business Arithmetic," all the examples being worked out, and explained so as to be readily understood, transforming the drudgery of calculation into a pleasing pastime, and qualifying persons of ordinary intellect to surpass the performances of the "Lightning Calculators" who have astonished mankind.

O Accountants, Brokers, Farmers, Tradesmen and persons engaged in the ruder mechanical pursuits, a knowledge of the Science of Numbers is of minor importance; Skill in the Art of Reckoning is absolutely indispensable; the business of this book is by new, original, and easily-acquired methods, to teach that Art in accord with, yet distinct from, the Science; its province is to qualify the learner either for practical Business pursuits, or to study the science; he will master the higher Arithmetic with greater facility if he is first an exact and Rapid Reckoner.

The phenomenal success achieved by the Author's former works—two hundred and fifty thousand copies have been sold—encourages the hope that this new Art of Reckoning will soon be in every School, making ALL the boys "Quick at Figures."

As a SCHOOL BOOK, its aim is to make the learner a GOOD CALCULATOR, with the greatest possible economy of time and study.

As a MANUAL for Business Men, Bookkeepers, Teachers, etc., to give the maximum of useful information in the briefest form consistent with clearness and completeness.

The REFERENCE TABLES are very comprehensive,

and their arrangement simple and original.

The miscellaneous section is unique; it embraces almost every variety of BUSINESS CALCULATION, the work of finding the answer to each question is so expressed that it constitutes a formula for all similar examples.

One Reviewer of these Rules and Tables says:

"Students, Teachers, and Business Men can no more afford to be without them than they can afford to travel by OX-TEAMS, now the BAILWAY spans the Continent."

"Exact! Clear! Brief! Brilliant!"

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# howard's ART OF RECKONING.

### DEFINITIONS AND SIGNS.

ARITHMETIC is the Science of Numbers, and the ART OF RECKONING by the use of figures.

ACCOUNT SALES is a written account of goods sold, their price, expenses, and the net proceeds.

AGENT.—An Agent, or Commission Merchant, transacts business for another person, who is called the *Principal*.

ALIQUOT.—An aliquot part of a number is such a part as will exactly divide that number.

Angle, a corner, or point where two lines meet; a square corner is called a *right angle*; an angle greater or less than a right angle is called an *oblique angle*: The difference in the direction of two lines proceeding from a common point.

AREA, the surface included within any given lines.

Assessment,—a specific sum charged against each share of a stock company, or against property for the purpose of Taxation.

Assets.—the available property of a Person, or a Company.

Note. These definitions are limited to the sense in which the words are used in Practical Business Arithmetic.

For Definitions omitted here see related subjects in the Book.

ARITHMETICAL SIGNS are characters indicating operations to be performed, and are indispensable for briefly and clearly stating a problem:

- +, plus, and more, signifying addition;
- -, minus, less, signifying subtraction;
- $\times$ , multiplied by, as  $2 \times 2 = 4$ ;
- $\div$  signifies Division, or divided by;  $6 \div 3$ , or  $\frac{3}{3}$  means 6 divided by 3;  $\frac{3\times 2}{3}$  —4 means 6 multiplied by 2, divided by 3, equals 4.
- =, equality, or is equal to, as  $\overline{6+2} \times 2 = 16$ , and is read thus, "6 plus 2, multiplied by 2, equals 16";
- the vinculum; or ( ) the Parenthesis, are used to show that the numbers to which they are applied, are to be considered as one quantity, thus  $\overline{(6\times4)+3\times2}\div\overline{4+2}$ , means, the sum of the products of 6 multiplied by 4, and 3 multiplied by 2 is to be divided by the sum of 4 and 2.
- √ 9, sign of the square root, read "the square root of 9";
  - 4<sup>3</sup>, sign of the square, read "the square of 4"; 3/8, the cube root of 8. 8<sup>3</sup>, the cube of 8.

Base, the side upon which a figure is supposed to stand,—the foundation of a calculation.

BROKER, a person who buys or sells stocks, bills of exchange, real estate, etc., for another on commission. Bulls are Brokers who aim to increase the price of stocks etc.; the opposite of Bears A Call is the privilege to demand the delivery of shares of Stock within a certain time agreed upon; the privilege to deliver shares of Stock within a certain time is called a Put; the sum of money deposited with a Broker by a Speculator in Stocks to secure the Broker against loss is called a Margin.

CAPITAL.—The money and stock employed in trade; the *Principal*.

COMMISSION is the fee allowed an agent, usually at some rate per cent.

Consignment.—Goods sent to an agent to be sold; the person who sends the goods is called the *Consignor*, or *Shipper*; the person to whom they are sent is the *Consignee*.

CIRCLE, a plane figure comprehended by a single curved line, called its *circumference*, every part of which is equidistant from its center.

CIRCUMFERENCE, the line that goes around a circle or sphere.

CYLINDER, a body bounded by a uniformly curved surface, its ends being equal and parallel circles.

Cube, a solid body with six equal square sides. A product formed by multiplying any number twice by itself, as  $4 \times 4 \times 4 = 64$ , the *cube* of 4.

CUBE ROOT is the number or quantity which twice multiplied into itself produces the number of which it is the root; thus 4 is the *cube root* of 64.

CURRENCY,—lawful money; coin or notes, or both; gold and silver coins are sometimes called *Specie*. A currency whose denominations increase and diminish in a tenfold ratio is called *Decimal Currency*.

DIAMETER, a right line passing from one side to the other and through the center of a circle, a sphere, or any object. DIVIDEND.—A sum divided.

The pro rata division of assets among creditors, or profits among stockholders.

Ellipse, an oval figure bounded by a regular curvé.

FACTORS.—Numbers from the multiplication of which proceeds the product; thus 3 and 4 are the factors of 12; the divisor and quotient of a number are its factors.

FIGURE. —A figure is a written sign representing a number.

FORMULA,—a rule or principle concisely expressed by the use of signs.

GRAVITY, the force by which all bodies are attracted to the centre of the earth.

Insolvent, one who is unable to pay his debts.

INTEREST is the price, or sum charged for the use of money lent; the sum of money bearing Interest, or invested, is called the *Principal*. Simple Interest is that which arises from the principal sum only. The sum of Principal and Interest is called the Amount.

INVENTORY, a catalogue of property on hand.

INVOICE, an account in detail of goods sold.

Manifest, a detailed list of a ship's cargo.

MATHEMATICS is the science of quantities.

MENSURATION is the art of measuring lengths, surfaces, and solids; *lineal* measure relates to length only; *superficial* measure to length and breadth; *cubic* or *solid* measure to length, breadth and thickness.

MULTIPLE, a quantity which contains another a certain number of times without a remainder. A common multiple of two or more numbers contains each of them a certain number of times, exactly. The least common multiple is the least number that will do this; 12 is the least common multiple of 3 and 4.

MOMENTUM, the quantity of motion in a moving body; impetus.

NET PROCEEDS, the sum remaining after all expenses are paid.

Number,—a number is a unit, or a collection of units; a Whole Number, or Integer, is a complete sum having no fractions. A Mixed Number consists of an integer and a fraction, as 73, etc. A Prime Number is one that cannot be separated into two or more integral factors, except unity and itself; an abstract number is a number used without reference to any particular object, as 9, 184, etc. A number used with reference to some particular object or quantity is called a Concrete Number.

PER CENT., from per centum, by the hundred; any per cent of a number is so many hundredths of that number; one per cent. is one of each hundred; the number of hundreths taken is called the rate per cent.

PER CENTAGE,—the Per Centage is the sum total obtained by taking any number of hundredths of any given number.

Power—A power is the product arising from multiplying a number by itself, or repeating it several times as a factor; thus,  $3 \times 3 \times 3$ , the product, 27, is the third power of 3.

The Exponent of a Power is the number denoting how many times the factor is repeated to produce the power, and is written thus:  $2^1$ ,  $2^3$ ,  $2^3$ .

$$2 = 2^1 = 2$$
, the first power of 2.  
 $2 \times 2 = 2^2 = 4$ , the second power of 2.  
 $2 \times 2 \times 2 = 2^3 = 8$ , the third power of 2.

PYRAMID, a solid body uniformly tapering to a point at the top, standing on a plane, or flat surface; if the base is round, the body is called a *Cone*; the part that remains of a Pyramid, or of a Cone, after cutting off the top parallel with the base, is called its *Frustrum*.

QUADRANGLE, a plane figure with four angles, and consequently four sides.

QUANTITY is any thing that can be increased, diminished or measured; therefore, all numerical calculations are made by one of two operations, viz: Addition or Subtraction.

RADIUS, half the diameter of a circle. A right line passing from the center to the circumference.

RECIPROCAL is a unit divided by any number. The *reciprocal* of any number or fraction, is that number or fraction inverted; thus the *reciprocal* of  $\frac{4}{1}$  is  $\frac{1}{4}$ , of  $\frac{3}{4}$  is  $\frac{4}{3}$ , of  $3\frac{1}{3}$  is  $\frac{3}{10}$ .

RECTANGLE, a plane figure bounded by four sides, having all its angles right angles.

REDUCTION is the act of changing numbers from one denomination to another without altering their value, as the reduction of fractions to other terms, the reduction of acres to yards, bushels to gallons, etc.

RULE—A rule is a prescribed method of performing an operation.

Scale—A scale is a series of numbers regularly ascending or decending.

A Solid or Body has length, breadth and thickness Sphere, a body in which every part of the surface is equally distant from the center.

SURFACE or SUPERFICES, the exterior part of anything that has length and breadth.

SQUARE, a figure having four equal sides, and four right angles. The product of a number multiplied by itself; thus 16 is the square of 4.

Square Root is the number which multiplied into itself, produces the number of which it is the root. 4 is the square root of 16.  $4 \times 4 = 16$ .

TERMS, the terms of a fraction are numerator and denominator taken together.

The terms of a Proportion are its members

TRIANGLE, a figure with three sides and angles.

Unit.—A unit is one thing; one taken in the abstract is called an Abstract Unit, in distinction from a concrete or Denominate Unit. A Fractional Unit is the unit of a fraction; thus \(\frac{1}{4}\) is the unit of \(\frac{2}{4}\).

Unity, any definite quantity or number taken as one.

Usury is a higher rate of interest than is allowed by law.

VALUE is the estimated price or equivalent of anything; in trading, money is the measure of value.

VOLUME is the solid contents of a body—the space included in the surfaces that bound it.

Weight is the measure of gravity

Zero,—0, naught, the starting point of a scale or reckoning.

NOTATION is the act of expressing numbers by figures.

All numbers are represented by the ten following

figures: 1, 2, 3, 4, 5, 6, 7, 8, 9, 0.

To establish their significance clearly in the minds of beginners it will be of great advantage occasionally to write and read them in the following manner:

The different values which the same figures have, are called *simple* and *local* values.

The simple value of a figure is the value it expresses

when it stands alone, or in the right hand place.

The *local* value of a figure is the increased value which it expresses by having other figures placed on its right.

Each removal of a figure one place to the left in-

creases its value ten times.

Numeration is reading numbers expressed by figures:

To read numbers expressed by figures: Point them off into periods of three figures each, commencing at the right hand; then, beginning at the left hand, read the figures of each period in the same manner as those of the right hand period are read, and at the end of each period pronounce its name.

NOTE.—By the English method of numeration, the periods from millions upward have the same name, but consist of six figures each.

### ADDITION.

Addition is the act of adding numbers. The answer is called the Sum.

Various suggestions have been made referring to improved methods of addition. In nearly every case the proposed improvement has been more fanciful than real. In practice, I have found no better or quicker method than the following:

 $\begin{array}{r}
3746 \\
8743 \\
6978 \\
1256 \\
3021 \\
\hline
23744
\end{array}$ 

Commence at the bottom of the right hand column; add thus, 7, 15, 18, 24; set down the 4 in unit's place, and carry the two tens to the second column; then add thus, 4, 9, 16, 24; set down the 4 in ten's place, and carry the two hundreds to the third column, and so on to the end. Never add in this manner: 1 and 6 are seven, and 8 are 15, and 3 are 18, and 6 are 24. It is just as easy to name the sum at once, omitting the name of each separate figure, and saves two thirds of time and labor.

Book-keepers and others who have long columns of figures to add will find the following methods and suggestions acceptable.

In adding long columns of figures, write in the margin, lightly with pencil, opposite the last figure added, the unit figure of the sum mediately exceeding 100. By doing this the mind is never burdened with numbers beyond 100; and if interrupted in the work, it can be resumed at the stage at which the interruption occurred. The example in the margin shows the method; opposite the figure 7; the 2 indigrams cating the column, so far, with the 7 included, a amounts to 102.

#### INSTANTANEOUS ADDITION BY COMBINATION.

Write two, three, four, or more rows of miscellaneous figures, then write such figures as will make an equal number of nines in each column; under these again, write another row of miscellaneous figures.

### EXAMPLE-

4 9 8 7 4 7 3 6 2 1 8 7 5 0 1 2 one 9. 5 2 6 3 two 9's. 7 8 1 2 three 9's. 4 9 8 6 3 4 9 8 3\*

RULE.—Bring down the last row, less the number of nines in each column, and prefix the number of nines.

<sup>\*</sup>This example has three nines in each column.

Rule of addition for two columns at once: first practice adding two columns of two figures each, until you are able to grasp at a glance, and pronounce their sum.

	323 $44$		

Add from the left, and say three seven, four eight, twelve eight, &c., &c., instead of thirty-seven, forty-eight, one hundred and twenty-eight, &c., &c.; this habit is readily acquired and saves half the time.

When you can instantly, at sight, name the sum of two pairs of figures, practice with gradually increasing columns of pairs, then take examples consisting of two or more columns of pairs.

	36	•		2147
	41			3472
47	74		*	1463
83	22		4614	2634
<b>32</b>	36	2123	7843	1785
21	41	4679	2183	<b>6823</b>
183	250	6802	14840	18394

\* The process is twelve six, one four naught; the 40 is put down and the 1 carried to the units column in the next pair, then ten naught, one four six.

Any person who will PRACTICE this method, may add two columns with perfect ease; there is no royal road to this accomplishment: speed with precision can be attained only by persistent PRACTICE.

Fives are always easy to add; so are 9's, when it is borne in mind that adding 9 to a sum places it in the next higher ten with the unit 1 less; thus, 17 + 9 = 26; 39 + 9 = 48; 62 + 9 = 72.

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### SUBTRACTION

is the process of finding the difference of two numbers by taking one number called the Subtrahend from another number called the Minuend.

The answer is called the Difference or Remainder.

Rule.—Write the numbers so that the units in the subtrahend shall be directly under the units of the same order in the minuend; under, and in the same order, write the difference. 1694

Subtract 473 from 1694.  $\frac{473}{1221}$ 

To prove Subtraction, add the difference to the subtrahend; if correct, their sum = the minuend.

### MULTIPLICATION.

MULTIPLICATION is the addition of several numbers in one act by adding to zero, one number called the *Multiplicand*, as many times as there are units in another number called the *Multiplier*.

The answer is called the *Product*.

Note.—The multiplier must be an abstract number.

The base of our system of notation is 10; therefore numbers increase and diminish in a tenfold ratio; increasing from the decimal point to the left, and decreasing from the decimal point to the right; hence to multiply any number by 10, annex a cipher, or remove the point one place to the right. To multiply any number by 100, annex two ciphers, or remove the point two places to the right. To multiply any number by 1000, annex three ciphers, or remove the point three places to the right.

In multiplying be careful always to write the units, tens, etc., of the multiplier under the units, tens, etc., of the multiplicand, and the figures of the product in the same order.

To find the product of two numbers, each expressed by two figures only.

Process.—First multiply the units figure of the multiplicand by the units figure of the multiplier, thus:  $4 \times 2 = 8$ ; put the 8 in the units place in the product, then  $\overline{5\times2} + \overline{4\times3} = 22$ , put the units 2 on the left of the 8 and carry the other 2; then,  $\overline{5\times3} + 2 = 17$ , which, put down, making a total of 1728, the answer.

The same method can be applied when the multiplicand has three or more figures. 163
24

3912

The steps are:  $3 \times 4 = 12$ , set down the 2 and carry the 1;  $(6 \times 4) + (3 \times 2) + 1 = 31$ ; set down the 1, and carry the 3.  $(1 \times 4) + (6 \times 2) + 3 = 19$ ; set down 9 and carry 1;  $1 \times 2 + 1 = 3$ , which place at the head of the line, making a total of 3912.

When the multiplier can be resolved into two factors, it is sometimes shorter to multiply by each factor, than by the whole number.

163

Example, multiply 163 by 24.  $8 \times 3 = 24$ .  $\frac{8}{1304}$   $\frac{3}{3912}$  Ans.

When either the tens or the units are alike.

Rule.—Multiply the units, set down the unit figure of the product; multiply the sum of the unlike figures by one of the like figures, then multiply the tens figures together, adding the carrying figures as you proceed.

Multiply 92 by 97 and 74 by 24.

97	•	74
92		24
8924		1776

When the units are alike and the sum of the tens is ten.

RULE.—Add one of the units to the product of the tens, and annex the product of the units.

Multiply 74 by 34.

$$\overline{7\times3}+4$$
 with 16 annexed=2516.

To multiply any two numbers between 10 and 20.

RULE.—Add one number to the units of another; call the sum tens, and add the product of the units.

$$18 \times 14 = 18 + 4 \text{ tens} + 8 \times 4 = 252.$$

The Area of a Circle—the square of the diameter ×.7854.

During the Author's visit to England in 1878, Mr. J. M. Gray, of Peckham, suggested the following easy rule:

To multiply any number by 1854.

Rule.—Multiply by 7, repeat, double and repeat, writing each successive product one place to the right.

.7 = the product of 1×.7.
7 = repeat one place to the right.
14 = double """ ""
14=repeat """ ""
.7854=1×.7854.

When the multiplier is any number between 11 and 20, the process is simply to multiply by the unit of the multiplier, set down the product under, and one place to the right of, and then add to the multiplicand; or multiply units by units, and then add to each succeeding product, the next figure to the right of the figure multiplied, and the figure carried.

Example, multiply 1496 by 17.

The process in the last example is:

$$6 \times 7 = 42$$
, set down 2 and carry 4.  
 $9 \times 7 + 6 + 4 = 73$ ; carry 7.  
 $4 \times 7 + 9 + 7 = 44$ ; carry 4.  
 $1 \times 7 + 4 + 4 = 15$ ; carry 1.  
 $1 + 1 = 2$ .

To multiply two figures by 11.

RULE.—Between the two figures write their sum: thus: multiply 43 by 11. Ans. 473. The sum of 4 and 3 is 7; place the seven between the 4 and 3, for the product.

Note.—Add one to the hundreds when the sum exceeds 9.

To multiply any number by 11.

RULE—Bring down the extreme right hand figure, then add the right hand figure to the next, and bring down the sum; then add the second figure to the third and bring down the sum, adding in the figure carried, in each case, and so on to the end.

Example  $12345678 \times 11 = 135802458$ .

To multiply any two numbers ending with 5.

RULE.—Add ½ the sum of the figures preceding the 5 in each number to the product of the same figures, and annex 25.

Note.—When the sum of the preceding figures is an odd number, add half the number next smaller than the sum and annex 75.

Multiply 85 by 65 and 105 by 35.

$$85 \times 65 = 7 + \overline{8 \times 6}$$
 with 25 annexed = 5525  
 $105 \times 35 = 6 + \overline{10 \times 3}$  " 75 " = 3675

To multiply when the unit figures added, equal 10, and the tens are alike, as  $67 \times 63$ .

Rule.—Multiply the units and set down the result, then add one to the upper number in tens place, and multiply by the lower. 67

$$\begin{array}{c} \phantom{0}6\phantom{0}3 \\ 4\phantom{0}2\phantom{0}1 \end{array}$$

To multiply two numbers when either has one or more ciphers on the right, as 26 by 20, 244 by 200, etc.

RULE.—Take the cipher or ciphers from one number and annex it, or them, to the other, multiply by the number expressed by the remaining figures.

Example 1.—Multiply 26 by 20. Ans. 520.

Process.— $260 \times 2 = 520$ . 2.—Multiply 244 by 200. Ans. 48800,  $24400 \times 2 = 48800$ , To multiply unlike numbers greater than a common base.

· Rule.—To the common base add the differences; multiply the sum by the base and add the product of the differences.

EXAMPLE.—Multiply 603 by 612

$$\overline{603+12} \times 600+\overline{3} \times 12 = 369,036.$$

To multiply unlike numbers less than a common base.

RULE.—To the multiplicand add the tens and units of the multiplier, less the last 1 to carry, multiply the sum by the common base and add the product of the differences.

Example.—Multiply 93 by 89 and 293 by 289.

$$\begin{array}{ccc} 89 & 293 \\ 93 & 89 \\ \hline 8277 & 282 \times 300 + 11 \times 7 = 84,677. \end{array}$$

The product of any two numbers—the square of their mean, diminished by the square of half their difference.

Example.—Multiply 22 by 18. 
$$20^2$$
— $2^2$  = 396.

To multiply two numbers having a common base, one ending with 25, the other ending with 75.

Rule.—Multiply the common base by one more than itself and annex 1875.

Example.—Multiply 675 by 625.

 $6 \times 7$  with 1875 annexed=421,875.

### RAPID METHOD OF SQUARING NUMBERS.

BY THE DIFFERENCE OF A NUMBER AND ITS BASE.

For squaring a number greater than its base.

RULE.—To the given number add the difference, multiply the sum by the base; to the product add the square of the difference.

NOTE. Take the nearest convenient multiple of ten for the base.

Example 1.—What is the square of 11? Ans. 121.

*Process.*—Taking 10 for the base, the difference is one  $(1 + 11) \times 10 + 1^2 = 121$ .

 $(22)^2=484$ . Taking 20 for the Base the difference is two.

 $(22+2)\times 20+2^{*}=484.$ 

 $(104)^{9}=10,816.$   $(104+4)\times 100+(4)^{9}=10,816.$ 

 $(322)^2 = 103,684. (\overline{322+22}) \times 300 + (22)^2 = 103,684.$ 

 $(813)^{2}=660,969.$   $(813+13)\times 800+(13)^{2}=660,969.$ 

For squaring numbers less than the base.

RULE.—From the number to be squared subtract the difference, multiply the result by the base, to the product add the square of the difference.

 $(9)^2 = 81$ . Taking 10 for the Base the difference is *one*.  $(9-1)\times 10+(1)^2 = 81$ .

 $(96)^{2}=9216; \overline{(96-4)\times100}+(4)^{2}=9216.$ 

 $(27)^2 = 729. (\overline{27-3}) \times \overline{30} + (3)^2 = 729.$ 

 $(99,946-54)\times 100,000+(54)^{2}=9,989,202,916=(99,946)^{2}$ .

Multiply £19,,19,,11\frac{2}{4}d by  $19 + \frac{18}{48} + \frac{11}{240} + \frac{8}{880}$ .

 $\frac{(£19,19,11\frac{3}{4}-£_{0\frac{1}{6}0}) \times 20+ \pounds(\frac{1}{0\frac{1}{6}0})^{8} = £399\frac{19}{20} \cdot \frac{9}{240} \cdot \frac{9}{241600}}{\text{or } £19,19,11\frac{3}{4} \times 20 - \frac{1}{200} = £399,19,2 \cdot \frac{1}{200} \text{ of a farthing.}}$ 

Note. In squaring numbers between 50 and 60, take 50 for the base; to 25 add the difference, call the sum hundreds, to this add the square of the difference.

1.—
$$(51)^2 = 2601$$
.  
Process.— $(25+1)\times 100 + 1^2 = 2601$ .  
2.— $(52)^2 = 2704$ .

Norm. In squaring numbers between 40 and 50; to 15 add the unit figure, call the number hundreds, to the sum add the square of the difference, taking 50 for the base.

1.—
$$(41)^2 = 1681$$
.  
Process.— $(15+1)\times 100 + 9^2 = 1681$ .  
2.— $(42)^2 = 1764$ .

By this rule the squares of all numbers up to 1000, and larger numbers near the multiples of 10 may be found with less labor than is required to find them in tables;

The square of any number ending with 25—half the number of hundreds + the square of the number of hundreds  $\times 10,000+625$ .

$$(3+6^2)\times10,000+25^2=390,625=625^2$$

In squaring very high numbers, use the foregoing rule in connection with the following formula:

"The square of any number=the sum of the squares of its parts, plus twice the product of each part by the sum of all the others."

EXAMPLE.—Find the square of 823,732 
$$823,000^2 = 677,329,000,000$$
  $823,000 \times 732 \times 2 = 1,204,872,000$   $732^2 = 535,824$   $678,534,407,824$ 

Note.—Until this rule is thoroughly understood, the learner should limit his exercises to numbers near 10, 100, 1000, etc.; and then operate with more complex numbers.

When the multiplier is a number near, and less, than a multiple of 10.

RULE.—Annex to the multiplicand as many ciphers as there are in the next order of tens higher than the multiplier, subtract the product of the multiplicand by the complement.

Multiply 222 by 93.

$$22,200 - 222 \times 7 = 20,646$$
.

When both numbers have a cipher in the tens place.

RULE.—Write the product of the units, then the sum of the products of the upper hundreds by the lower units, and the lower hundreds by the upper units, prefix the product of the hundreds.

Multiply 409 by 704.

 $\begin{array}{r}
 704 \\
 409 \\
 \hline
 287936
 \end{array}$ 

# DIVISION.

Division is the process of finding how many times one number called the *Divisor* is contained in another number called the *Dividend*.

The answer is called the Quotient.

RULE.—To the left and in a line with the dividend, write the divisor, separated by an arc. Take so much of the dividend as contains a number less than ten times the divisor; the number of times the divisor is contained in that part of the dividend is the first figure in the quotient; annex the next unused figure of the dividend to the remainder to find the second figure of the quotient, and so on to the end.

Divide 49654809 by 4. 4)49654809 Ans. 124137021

Process—The divisor 4 is contained in the first figure of the dividend once, therefore 1 is the first figure in the quotient: 4 is contained twice and 1 remainder in 9; 2 is then the second figure in the quotient: the next unused figure 6 annexed to the remainder 1=16: 4 is contained in 16 four times, and so on to the end.

Divide 7983204 by 23.
28)7983204(34709522)
108
163
220
134
-19

Process.  $79-23\times3$ , the remainder is 10; the next unused figure in the *dividend* 8, annexed to 10=108;  $108-23\times4$ , the remainder is 16; to this remainder annex the next unused figure in the dividend, and so on until the quotient is complete. When the divisor is a composite number, divide by its factors.

# FRACTIONS.

A Fraction is a part or parts of a unit, a quantity, or a whole number. Common fractions are written with figures below the line called the Denominator, and figures above the line called the Numerator, thus  $\frac{2}{4}$ , three-fourths,  $\frac{2}{5}$ , nine-fifths, etc., the Denominator shows into how many parts Unity is divided; the Numerator shows how many parts are taken. When the numerator exceeds the denominator it is called an Improper Fraction.

Multiplying or Dividing both terms of a fraction by the same number does not change its value.

Multiplying the numerator, multiplies the fraction.

Dividing the numerator, divides the fraction.

Multiplying the denominator, divides the fraction.

Dividing the denominator, multiplies the fraction.

Fractions are called similar when they have a common denominator, as  $\frac{3}{6}$ ,  $\frac{3}{6}$ ,  $\frac{2}{6}$ ,  $\frac{1}{6}$ .

To find a common denominator for any two fractions, multiply both terms of either fraction by the denominator of the other; or if the denominator of one fraction will exactly divide the denominator of the other, multiply both terms of the one by the quotient.

To reduce a fraction to its simplest form.

RULE.—Divide both terms by their greatest common divisor or its factors, the simplest form, or lowest term of  $\frac{3}{4}\frac{5}{8}$ , is obtained by dividing both terms by 12,  $\frac{3}{4}\frac{5}{8} = \frac{3}{4}$ .

To find the greatest common divisor of two numbers:

RULE.—Divide the greater by the less, and the previous divisor by the remainder, and so on until there is no remainder; the last divisor is the answer.

Find the greatest common divisor of 18 and 27.

$$\begin{array}{ccc}
18)27(1 & & ; \\
 & 18 & & ; \\
\hline
 & 9)18(2 & & \\
 & 18 & & Ans. 9.
\end{array}$$

To find the least common multiple:

Rule.—Cancel all the numbers that are contained in any of the others; divide all those not canceled by any number, or the *greatest* of its factors, that will exactly divide any one of them, bring down each quotient with the undivided numbers and proceed as before, until no two numbers have a common divisor; the product of all the divisors and the remaining numbers is the answer.

Find the least common multiple of 36, 8, 9, 10,

ADDITION OF FRACTIONS.

RULE.—Reduce the fractions to a common denominator; add the numerators and place the sum over the common denominator, or multiply either denominator by the other numerator, and place the sum of the products over the common denominator.

add 
$$\frac{3}{8}$$
 and  $\frac{1}{4}$ ;  $\frac{3}{8} = \frac{8}{18}$ ,  $\frac{1}{4} = \frac{8}{18}$ ,  $\frac{6}{18} + \frac{18}{18} = \frac{11}{12}$ , or  $\frac{3\times 1}{4\times 2} = 11$  the numerator,  $4\times 3 = 12$  the denominator. add  $\frac{8}{8}$  and  $\frac{1}{2}$ ,  $\frac{8}{8} = \frac{6}{10}$ ,  $\frac{1}{2} = \frac{5}{10}$ ,  $\frac{6}{10} + \frac{5}{10} = \frac{1}{10} = \frac{1}{10}$ , or  $\frac{5\times 1}{2\times 3} = 11$ , the numerator.  $5\times 2 = 10$ , the denominator.

#### SUBTRACTION OF FRACTIONS.

RULE.—Reduce the Fractions to a common denominator, and write the difference of the numerators over the common denominator.

From 
$$\frac{3}{4}$$
 take  $\frac{1}{2}$ . PROCESS:  $\frac{1}{2} = \frac{2}{4}$ ;  $\frac{3}{4} - \frac{2}{4} = \frac{1}{4}$  Ans. From  $9\frac{1}{3}$  take  $4\frac{1}{2}$ . Ans.  $4\frac{5}{3}$ . From  $18\frac{3}{4}$  take  $3\frac{1}{3}$ . Ans.  $15\frac{5}{12}$ .

#### MULTIPLICATION OF FRACTIONS.

RULE.—Multiply the whole numbers together, then multiply the upper whole number by the lower fraction, and the lower whole number by the upper fraction; multiply the fractions together, and add all the products; or reduce mixed numbers to improper fractions, and multiply the numerators by each other, and the denominators by each other, cancelling as shown on pages 40 and 42.

MULTIPLICATION OF ENGLISH MONEY.

Multiply £9 7s.  $5\frac{3}{4}$ d. by 7.

PROCESS.—Say seven times 3 = 21 farthings; put down  $\frac{1}{4}$ d. and carry 5d.; 7 times  $\frac{5}{6}$ d.  $+ \frac{5}{6}$ d. = 3sd.; put down 4d. and carry 3s.; 7 times 7s.  $+ \frac{3}{8}$ s. = £2 12s.; put down 12s. and carry £2; 7 times £9 + £2 = £65. Total £65 12s.  $\frac{4}{4}$ d.

THE UNIT—or one thing—is the idea of number in its simplest form. UNITY is the basis of every number, the primary base of every fraction, the unit of six months in one month, the unit of a fraction is the reciprocal of the denominator, thus a is the unit of a; every step from the unit increases the complexity of numbers, and consequently demands an increase of mental power and energy in dealing with them; therefore, when the price per unit is in pence, find the amount at one penny each, and multiply by the given number of pence each.

Find the cost of 38lbs. of beef at  $7\frac{1}{2}$ d. per lb.: 38lbs. @ 1d.=38d.=3s. 2d., 3s. 2d. $\times 7\frac{1}{2}$ d.=£1 3s. 9d. Find the cost of  $42\frac{1}{2}$ yds. of cloth at 8d. per yd.  $42\frac{1}{2}$ yds. @ 1d,=3s.  $6\frac{1}{2}$ d.; 3s.  $6\frac{1}{2}$ d. $\times 8$ =£1 8s. 4d.

The price per unit being in shillings, find the amount at one shilling, and multiply by the price of one.

Find the cost of 40 articles at 3s. 6d. each.

40 @ 1s. = £2; £2×3 $\frac{1}{2}$  = £7.

or, multiply the given number of units by half the price of one in shillings, and point off one place to the left. Thus:  $\pounds 4.0 \times 13 = \pounds 7$ .

The price per ton, in  $\mathcal{L}$ , regarded as shillings,

equals the price per cwt.

The price of 1 cwt. in shillings, regarded as farthings,  $\times \frac{3}{1}$ —the price of 1lb. in farthings; thus, the price of

11b. in farthings, at 21s. per cwt.  $=\frac{21\times3}{7}$  = 9 farthings.

The price of 1lb. in shillings, regarded as farthings,  $\times 3$ =the price of 1oz.; thus, the price of 1oz. at 4s. per lb.= $4\times 3$ =12 farthings=3d.

The price of 1oz. in farthings, regarded as shillings, ÷3 equals the price of 1lb.; thus, the price of 1lb. at

 $2\frac{1}{4}$ d. per oz. =  $\frac{9}{3}$  = 3s.

When the price is an aliquot part of a £, a florin, or a shilling, multiply the given quantity by the aliquot part.

Find the cost of 2793 articles at 3s. 4d. each. 3s. 4d. =  $\frac{1}{6}$  of the £1, 1793÷6=£465 10s.

NOTE.—To attain greater skill in the Art of Reckoning extend and learn by heart Tables of Multiplication, pence and aliquot parts. See next page.

An aliquot part of a number is a measure of that number, or such a part as will exactly divide it; thus,  $12\frac{1}{2}$  is an aliquot part of 100 because it is contained 8 times exactly in 100; 1s. 8d. is an aliquot part of £1 because it is contained in £1 12 times. The aliquot parts of £1 are 10s., 6s. 8d., 5s., 4s., 3s. 4d., 2s. 6d., 2s., 1s. 8d., 1s. 4d., 1s. 3d., 1s., 10d., 8d., 6d., 4d., 3d., 2d., &c.

To find the cost when the price of one is the aliquot part of a £1. Regard the given number as pounds sterling, and multiply by the aliquot part.

The aliquot parts of a florin are 1s., 8d., 6d., 4d., 3d., 1½d., &c. To find the cost when one is the aliquot part of 2s. Regard the given number of articles as £1 sterling, divide by 10, and multiply by the aliquot part.

Find the cost of 738 73.8

articles at 4d. each, 6 £12·3 = £12 6s. 0d.

The aliquot parts of one shilling are 6d., 4d., 3d., 2d.,  $1\frac{1}{2}$ d.,  $\frac{3}{4}$ d. To find the cost when the price of one is the aliquot part of a shilling. Regard the given numbers as shillings, and  $\times$  the aliquot part.

The aliquot parts of a ton are 10cwts., 5cwts., 4cwts., 2½cwts., 2cwts., 1cwt., ½cwt., &c. The aliquot parts of a cwt. are 56lbs., 28lbs., 14lbs., 7lbs., 4lbs., 3½lbs., &c.

To multiply by the aliquot parts of 100 or 1000. Reduce mixed numbers to decimals, multiply by 100 or 1000, and take the aliquot part.

To divide by the aliquot part of 100 or 1000. Remove the decimal part two or three places left, and multiply by the denominator of the aliquot part.

61 is 11 of 100 62½ is § of 100 250 is 1 of 1000 312 is  $\frac{\bar{\epsilon}}{18}$  of 1000 81 is 12 of 100 66% is % of 100  $12\frac{1}{2}$  is  $\frac{1}{2}$  of 100100 3331 is 1 of 1000 75 is 🛊 of 831 is 1 of 163 is 1 of 100 100 375 is § of 1000-18<sup>2</sup> is 1 of 100 87½ is ¼ of 100 62½ is ¼ of 1000 500 is ⅓ of 1000 625 is § of 1000 25 is 1 of 100 31 is 🎋 of 100 831 is 12 of 1000 666 is a of 1000 331 is 1 of 100 125 is a of 1000 750 is 🛊 of 1000 37½ is § of 100 1664 is 1 of 1000 833\frac{1}{2} is \frac{1}{2} of 1000 50 is 1 of 100 187½ is ¼ of 1000 875 is a of 1000

To multiply any two numbers together, ending with  $\frac{1}{2}$ , as  $9\frac{1}{2}$  by  $3\frac{1}{2}$ :

RULE.—To the product of the whole numbers, add half their sum, plus 4.

NOTE. When the sum is an odd number take half the next number below it, and the fraction in the answer will be %.

What will 9½ lbs. of rice cost, at 3½ cts. per
 Ans. 33½ cents.

Process.—The sum of 9 and 3 is 12; half this sum is 6; then we say 9 times 3 is 27, and 6 = 33; to this add  $\frac{1}{4}$ .

- What will 9½ doz. buttons cost, at 8½ cts. per doz? Ans. 80½ cts.
- 3. What will  $11\frac{1}{2}$  lbs. of beef cost, at  $9\frac{1}{2}$  cents per lb? Ans. \$1.09\frac{1}{4}.
- 4. What will  $7\frac{1}{2}$  doz. eggs cost, at  $13\frac{1}{2}$  cents per doz? Ans.  $$1.01\frac{1}{2}$ .

To multiply any two numbers together having the -- same fraction.

RULE.—To the product of the whole numbers, add the product of their sum by the fraction; to this add the product of the fractions.

1. What will 13 $\frac{3}{4}$  lbs. of beef cost, at  $7\frac{3}{4}$  cents per lb? Ans. \$1.06 $\frac{3}{18}$ .

*Process.*—The sum of 13 and 7 is 20, three-fourths of this sum is 15, so we say, 7 times 13 is 91, and 15 = 106, to which add the product of the fractions,  $\binom{9}{16}$  and the result is the Ans. \$1.06 $\frac{9}{16}$ .

In actual business calculations, any fraction less than a cent is reckoned as one cent; therefore in dealing with such questions as  $13_3^1$  pounds of beef at  $7_5^1$  cents a pound, it is sufficiently accurate to say:

$$\frac{1}{5}$$
 of 13=3.  $\frac{1}{3}$  of 7=2.  $\overline{13\times7}+3+2=96$  cents;  
Or  $17\frac{1}{4}$  lbs. of cheese at  $9\frac{1}{3}$  cents per pound.  
 $\frac{1}{3}$  of 17=6.  $\frac{1}{4}$  of 9=2.  $\overline{17\times9}+6+2=\$1.61$ .

When the whole numbers are alike, and the sum of the fractions is a unit.

RULE.—Take the product of the whole numbers, to this add the integer in the multiplicand, then add the product of the fractions, and the result will be the answer.

$$2\frac{1}{2} \times 2\frac{1}{2} = 2 \times 2 + 2 + \frac{1}{2} \times \frac{1}{2} = 6\frac{1}{4}$$
.  
 $7\frac{1}{8} \times 7\frac{1}{8} = 7 \times 7 + 7 + \frac{1}{8} \times \frac{1}{8} = 56\frac{7}{4}$ .  
 $96\frac{7}{4} \times 96\frac{1}{8} = (96)^8 + 96 + \frac{7}{4} \times \frac{1}{8} = 9312\frac{1}{8}\frac{4}{4}$ .  
 $9956\frac{1}{4} \times 9956\frac{1}{4} = (9956)^8 + 9956 + \frac{1}{4} \times \frac{1}{4} = 99,131,892\frac{198}{1988}$ .  
Division of Fractions.

Rule: Reduce whole and mixed numbers to improper fractions, then multiply the numerator of the dividend by the denominator of the divisor and divide the product by the other two terms; or,

Reduce to a common denominator and divide the numerator of the dividend by the numerator of the divisor.

Divide 8½ by 1¼. 
$$8\frac{1}{2} = \frac{17}{4}$$
  $\frac{17 \times 4}{2 \times 5} = 6\frac{4}{5}$  Ans. or  $8\frac{1}{2} = \frac{34}{4}$ .  $1\frac{1}{4} = \frac{5}{4}$ ,  $\frac{34}{5} = 6\frac{4}{5}$ . Ans. See pages 40 and 42.

# DECIMALS.

The system of Decimal fractions is so pre-eminently simple, that when it is generally understood it will entirely displace the clumsy system of common fractions. In harmony with our system of notation, it is a fraction always having some power of ten for a denominator: thus  $1 = \frac{1}{10}$ ,  $.03 = \frac{3}{10}$ ,  $.007 = \frac{1}{1000}$ ,  $47.8 = 47\frac{3}{10}$ , &c., &c.

Where common fractions occur the calculation may be often simplified by reducing them to decimals.

To reduce a common fraction to a decimal.

Rule.—Divide the numerator by the denominator.

Is performed in the same manner as in whole numbers; care being taken to place the numbers to be added so that the decimal points are in a perpendicular line, and place the decimal point in the *sum* under those in the

numbers added.

# SUBTRACTION OF DECIMALS

Is performed in the same manner as in whole numbers, care being taken to place the decimal point in the subtrahend under that in the minuend, and the decimal point in the remainder under those in the numbers employed.

#### MULTIPLICATION OF DECIMALS.

Rule.—Multiply as in whole numbers, and point off as many places to the left for decimals as there are decimal places in both factors.

1. Multiply .5 by .5.	Ans. 25.
2. Multiply 1.75 by .3.	Ans. $.525$ ;
3. Multiply 27.46 by .4	Ans. 10.984

When there are not as many figures in the product as there are decimals in both factors, supply the deficiency by prefixing ciphers. 3×.3=.09. .29×.004=.00116.

To multiply by .1 remove the decimal point one place to the left, by .01 two places, by .001 three places, by 10 one place to the right, by 100 two places, by 1000 three places, &c., &c.

Note.—In practical business the answer to three decimal places is sufficiently exact, the third decimal only counting for mills, the drudgery of finding, and writing the figures for decimals of no value, may be avoided by reversing the order of the multiplier and writing the first figure of the reversed multiplier under the third decimal figure in the multiplicand, begin each line of the partial products, with the product of the multiplying figure and the figure directly above it, adding the carrying figure, if any, from the immediate right hand figure.

What is the par value in American gold coin of £11, 4, 3, Sterling?

£11.2125 ·	11.2125
4.8665	56,684
560625	44 850 .
672750	8 970
672750	673
897000	67 ·
448500	5
<b>\$</b> 54.56563 <b>125</b>	\$54.565

This example illustrates the difference of the two methods.

#### DIVISION OF DECIMALS.

The division of decimals is performed in the same manner as in whole numbers, care being taken to point off the decimal places in the quotient.

RULE.—Divide as in whole numbers, and point off in the quotient as many places to the left for decimals as the decimal places in the dividend exceed those in the divisor.

Divide .244 by .4.	Ans61.
Divide .255 by .05.	Ans. 5.1.
Divide 776 by 4.2	Ans. 184.77+
Divide 271 by 3.1416	Ans. 86.26+
Divide 3.1416 by .7854	Ans. 4
Divide 500 by 4,8665	Ans. 102.743+
Find the Par value in Po	unds Sterling of \$54.5656 U.S.

Find the Par value in Pounds Sterling of \$54.5656 U.S. Gold Coin. See pages 57, 59 and 100. Ans. £11,,2,3.

The learner can supply additional examples at discretion, bearing in mind the following: The dividend must always contain, at least, as many decimal places as the divisor. When the number of figures in the quotient is less than the excess of the decimal places in the dividend over those in the divisor, the deficiency must be supplied by prefixing ciphers. When there is a remainder after dividing the dividend, annex ciphers, and continue the division; the ciphers annexed are decimals to the dividend.

To divide by any number expressed by 1 and any number of ciphers, remove the decimal point as many places to the left as there are ciphers in the divisor.

74864 - 1000 = 74.864

To Divide by adding the Difference of 10, 100, 1000, etc. when the Divisor is something less than any power of ten.

Rule.—To the left and in a line with the Dividend write the Divisor; under; write the Difference; find the first figure in the Quotient and with it Multiply the Difference, add the Product to the part of the number divided, write down the sum, with the next figure in the dividend annexed, point off the left hand figure, and so proceed to the end.

Divide 99847632 by 97 Ans. 1029357 4. 97)99847632(1029357 97)99847632(1029357 3)10,284 2,907284 common method 9.346194  $\overline{3.553}$ 907  $5,\overline{68}2$ 873 7.03 346 291 The Difference of 97 and 100=3. 553 The left hand figures pointed 485 off are the same as the Quo-682 tient, and serve to check and 679 prove the answer.

The labor of finding the answer to valueless decimals may be saved by cutting off a figure from the right hand of the divisor, as each new figure in the quotient is found, carrying what would have been obtained by the multiplication of the figure cut off, 1 if the multiplication produces more than 5 and less than 15, 2 if more than 15 and less than 25, etc.

73.412)648.765	4386(8.8373	73.412)648.7654386(8.8373				
587.296	` ,	<b>587.296</b> . <b>`</b>				
61469	Ī <b>4</b>	61469				
58729		58730				
2739	83	2739				
2202	36	2202				
537	478	537				
513	884	514				
23	5946	23				
	0236	22				
<u>-</u> 1	5740	1				

# PROPORTION.

Proportion is the equality of ratios.

Ratio is the relation which one quantity bears to another of the same kind, with reference to the number of times that the one is contained in the other; the Quotient is the Ratio.

Thus, the ratio of 7 to 21 is 3, because 7 is contained 3 times in 21, or 21 is 3 times seven. The same result is obtained if we divide 7 by 21, for we then find  $\frac{7}{21} = \frac{1}{8}$ , which means that 7 is  $\frac{1}{8}$  of 21, and this expresses the very same relation as before, to say that 7 is  $\frac{1}{8}$  of 21 is precisely the same as to say that 21 is 3 times 7. The ratio of 9 to 27 is 3, but we have seen that the ratio of 7 to 21 is also 3, therefore, the ratios of 7 to 21 and 9 to 27 are the same,  $21 \div 7 = 27 \div 9$ , and these quantities are thefore called proportionals.

In any proportion, as 7:21::9:27
the product of the middle numbers, 21 and 9, equals the product of the extremes, 7 and 27; hence the *rule*, that when the fourth proportional is unknown,

Multiply the second and third terms, and divide the product by the first.

EXAMPLE.—If 7 sheep cost 21 dollars, what will 9 cost at the same rate?

27 dollars, Ans.

 $21 \times 9 \div 7 = 27$ , or,  $\frac{21 \times 9}{7} = 27$ 

Nore.—The first and third terms are of the same kind; the second term is of the same kind as the required Term.

All Arithmetical business problems may be solved by Proportion: in fact, an exact knowledge of the principles of *Proportion* and skill in *Cancellation* are the essential qualifications of a *Good Calculator*.

# CANCELLATION

is the process of abridging operations in division by rejecting equal factors from both divisor and dividend.

Note.—Be careful to write all the terms of the kind required in the answer, in the required denomination; that is, feet or fractions of a foot; pounds, or fractions of a pound, etc.

CANCELLING IN CALCULATION.—Whenever it is required to multiply two or more numbers together, and divide by a third, the first step is to state the problem in its most manageable form; this can only be done by the use of the arithmetical signs.

The statement  $28 \times 12$ 

14

is to be read, 28 multiplied by 12 is to be divided by 14.

Stating the problem as above we see at a glance if the divisor is contained, and how many times, in either of the multipliers.

In the foregoing example the divisor, 14, is contained twice in the multiplier, 28; then cancel the 14 and substitute 2 for the 28, and say, twice 12 is 24 the answer.

Process,

$$\frac{2}{2\% \times 12} = 24.$$

EXAMPLE.—If 9 turkeys cost \$18, what will be the cost of 27?

$$\frac{18 \times \cancel{2} \cancel{1}}{\cancel{9}} = \$54, \text{ Answer.}$$

If the divisor is not contained evenly in either of the multipliers, there may be a common divisor for the divisor itself and one of the multipliers; if so, the common divisor may be used in cancelling, thus:

$$\frac{7}{\cancel{63} \times 8} = 18\frac{2}{3}, \text{ Ans.}$$

A glance shows that 9 is the common divisor for 63 and 27.

When a common divisor has been used to change the expression of the divisor and one of the multipliers, the new divisor may be cancelled when it is contained an even number of times in the other multiplier.

Example 
$$\frac{7}{\cancel{53} \times \cancel{5}} = 14$$

Process—36 and 63 divided by 9, the common divisor, becomes 4 and 7 respectively, the 4 into 8, 2 times, cancel 4 and 8, and twice 7 is 14, the answer.

Summary of the rapid process for cancelling.

- 1. Draw a horizontal line; above the line write dividends only; below the line write divisors only.
- 2. If there are ciphers above and below the line, erase an equal number on either side; 1 standing alone may be disregarded.
- 3. If the same number stands above and below the line, erase them both.
- 4. If any number on either side of the line will divide any number on the other side of the line without a remainder, divide, and erase the two numbers, retaining the quotient figure on the side of the larger number.
- 5. If any two numbers on either side have a common divisor, divide them by that number, and retain the quotients only.
- 6. Multiply all the numbers above the line for a dividend, and those below the line for a divisor; divide, and the quotient is the answer.
- 7. Write all the terms of the same kind in units, or fractions, of the same denomination; *i. e.*, feet, or fractions of a foot; yards, or fractions of a yard.

EXAMPLE.—If 7 inches of velvet cloth cost 2½ dollars, what will be the cost of 7 yards? \$90, Ans.

Process, 
$$\begin{array}{ccc}
5 & \pi & 36 \\
- \times - \times - \times \frac{\pi}{\pi} & = 90.
\end{array}$$

Note.— $2\frac{1}{2}$  dollars =  $\frac{5}{2}$ , 7 yards =  $\frac{7}{1}$ , 7 inches =  $\frac{7}{36}$  of a yard,  $\frac{7}{36}$  inverted is  $\frac{36}{1}$ .

If an upright line is used put dividends on the right, and divisors on the left. In stating a question put the term of the same kind as the required term first, at the top, on the right of the line; then the other terms in pairs of the same kind; if the conditions tend to increase, put the larger term on the right of the line; if otherwise, on the left.

EXAMPLE:—If 5 compositors, in 16 days of 14 hours long, can compose 20 sheets of 24 pages in each sheet, 50 lines in a page, and 40 letters in a line, in how many days of 7 hours long may 10 compositors compose a volume containing 40 sheets, 16 pages in a sheet, 60 lines in a page, and 50 letters in a line, 1 of the second set of compositors being equal to 2 of the first?

Ans. 16 days.

Hours 7 14 Sheets 20 40	0 more time to set 40 than 20 sheets. 6 less time to set 16 than 24 pages. 0 more time to set 60 than 50 lines. 0 more time to set 50 than 40 letters.
-------------------------	---

Note.—Excepting the upper term 16, the numbers on one side exactly balance the numbers on the other, and may all be canceled.

This method acts like a pair of scales, we use known to find the value of unknown quantities; the arrangement of the terms is so very plain and natural as to be easily apprehended; by its use the most complex problems are simplified, and all business calculations made with very few figures, and very little mental effort; it is accurate, and free from the risk of error.

## PERCENTAGE.

PER CENTAGE is the term applied to operations in which 100 is the basis of calculation.

The total result obtained by taking hundredths of any number is called the Per Centage.

PER CENT—from per centum, by the hundred; any number of hundredths of a number is so many per cent. of it; thus, five hundredths is five per cent.

THE RATE per cent is the number of hundredths taken.

Interest, Discount, Broker's fees, etc., etc., are calculated on the basis of an agreed price per cent.

The number of which any per cent. is taken is called the Base, or the Principal.

The Base x the Rate = the Per Centage.

The Base plus the Per Centage = the Amount.

The  $Base \times 1$ , plus the Rate = the Amount.

The Per Centage : the Base = the Rate.

The Amount: the Base=1, plus the Rate.

The Per Centage: the Rate the Base.

The Amount: 1, plus the Rate the Base,

The Amount—the Base—the Per Centage.

The following examples embrace most of the conditions under which percentage occurs in business, and the mode of solution in each case applies to all similar examples.

How many of 500 sheep will be left, if 20 per cent. of them are sold?

 $500 \times .20 = 100$ .

500-100=400 sheep.

What per cent of 300 is 75? 75÷300=25 p ct.

Of what number is 48, 8 p ct.? 48:.08=600.

Sold a horse for £40, lost 20  $\varphi$  ct. What did it cost?

$$1-.20=\frac{80}{100}=\frac{8}{10}$$
 8 10 = 50 pounds.

The population of a village increased from 900 to 1200, at what rate per cent, did it increase?

$$\frac{300}{9}$$
 =  $33\frac{1}{8}$  per cent. Or,  $\frac{1200}{900}$  = 1.33\frac{1}{8}.

The sales of a firm fell off from £12000 to £9000, what was the rate per cent. of decline?

$$\frac{300}{12} = 25 per cent,$$

Bought a horse for \$80, sold it for \$105. What percent. profit?  $\frac{250}{8}$ =31\frac{1}{4} per cent. Or,  $\frac{105}{80}$ =1.31\frac{1}{4}.

Bought a piano for \$300, sold it for \$250. What per cent. loss?  $\frac{50}{3}$ =16% per cent.

Bought a horse for \$40. What must it be sold for to gain 20 per cent?

$$40 \times .20 + 40 = 48 \ dollars.$$

A horse was sold for \$24; the rate per cent profit was the same as the number of dollars it cost. What was the cost, and what the gain per cent?

Cost \$20. 
$$20^2 = 400 \times .01 = 4$$
. Profit \$4, or

Vof the profit is .1 the cost. Vof  $4=2\times10=20$ Cost \$20. Profit 20 per cent.

How many dollars will earn 1 cent a day at 9 per cent per annum?

Find the commission at 2 per cent., and the net proceeds on £147 15s.  $^{\bullet}$ £147.75×.02=2.955=£2 19s. 1d.=the commission. £147 15s. -£2 19s. 1d.=£144 15s. 11d.=net proceeds.



#### INTEREST.

INTEREST is the price or sum charged for the use of money lent; the sum of money bearing interest is called the *Principal*; Simple interest arises from the use of the *Principal* only. The *Rate* per cent. is the *number* of units charged for the use of each hundred units.

The Common Method of reckoning interest in the United States is based on a year of 360 days; in England and U. S. Courts interest is reckoned on the basis of a year of 365 days; when using the common method, count thirty days only for each entire month and the difference, if any, will be unimportant.

Find the interest by both methods on any example from March 3rd to July 27th; \frac{144}{145} exactly equals \frac{145}{145}.

COMMON METHOD, GENERAL RULE TO RECKON INTEREST.

The Principal V the number of days V the Rai

The Principal  $\times$  the number of days  $\times$  the Rate  $\div 360 \times 100 =$  the Interest.

ENGLISH METHOD, GENERAL RULE TO RECKON INTEREST.

The Principal  $\times$  the EXACT number of days  $\times$  the Rate  $\div 365 \times 100 =$  the interest.

TO FIND THE DIFFERENCE OF TIME BETWEEN TWO DATES.

Rule.—Subtract the earlier from the later date.

EXAMPLE.—For what time must Interest be charged on a debt due April 12th, 1882 and settled June 24th, 1883?

83 6 24 Process, 82 4 12 Ans. 1 yr. 2 mos. 12 days.

TO FIND THE NUMBER OF DAYS BETWEEN TWO DATES.

Common Method.--Multiply the number of entire months by three; call the Product tens and add the extra days; for the English Method add one day for each month of 31 days; when February occurs, deduct two days for the Common year, one day for Leap year.

TO RECKON INTEREST ON £ STERLING AT 5 PER CENT, PER ANNUM,—One tenth of the principal is the interest for 2 years, at 5 per cent.

Multiply 1 of the principal by half the given number of years. Find the interest on £240 10s. for 8yrs. 8mos. at 5 per cent.

 $8:8\div2=4\frac{1}{3}$ . £24.05  $\times$   $4\frac{1}{3}=104.216=$ £104 4s. 4d. Note.—If the exact number of days in each month is taken for a multiplier, and 360 used for a divisor, the difference or excess will be  $\frac{1}{3}$ ; about 1\frac{1}{3} conts to be taken off each 100, or one penny off each six shillings of interest.

Any number of  $\mathcal{L}$  sterling, regarded as *pence*, is the interest for *one month*, at 5 per cent. per annum: 1 of the principal in  $\mathcal{L}$  sterling, regarded as *pence*, is the interest for *three* 

days; hence the following Rules:-

Multiply the principal by the given number of months, and parts of a month; or multiply '1 of the principal by one-third the given number of days; the answer will be in pence. Or multiply '1 of the principal by half the number of months, and divide by 12, the answer will be in £ sterling.

Find the interest on £428 from July 27th, 1882, to March 3rd, 1883. £12 16s. 9\frac{1}{2}d. Ans.

Interest at 5 per cent.  $\times 2=1$  per cent.;  $\times 4=2$  per cent.;  $\times \frac{1}{2}=2\frac{1}{2}$  per cent.;  $\times 6=3$  per cent.;  $-\frac{1}{4}=3\frac{1}{2}$  per cent.;  $\times 7=3\frac{1}{2}$  per cent.;  $-\frac{1}{4}=3\frac{3}{4}$  per cent.;  $\times 8=4$  per cent.;  $\times 9=4\frac{1}{2}$  per cent.;  $+1=5\frac{1}{2}$  per cent.; +2=6 per cent.;  $+3=6\frac{1}{2}$  per cent.; +4=7 per cent., &c., &c.

TO RECKON INTEREST ON £ STERLING AT 6 PER CENT. PER ANNUM:

One hundredth of the principal is the interest for two months at 6 per cent; 001 of the principal is the interest for six days; 1 of the principal in £ is the interest in shillings for one month; 01 of the principal in £ is the interest in shillings for three days; hence the following Rules:  $\frac{1}{2}$ 

Multiply '01 of the principal by half the given number of months; or multiply '001 of the principal by 1, the number of days; to have the answer in shillings multiply '11 of the principal by the number of months; or multiply '01 of the principal by 1, the number of days.

Find the interest on £428 10s., from March 3rd to July 27th.

\$\frac{1}{2}\$ of the interest at 6 per cent.=1 per cent.; \$\frac{1}{2}\$=2 per cent.\$
\$\frac{1}{2}\$=3 per cent.\$; \$-\frac{1}{2}\$=4 per cent.\$; \$-\frac{1}{2}\$=5 per cent.\$; \$+\frac{1}{2}\$=6\frac{1}{2}\$ per cent.\$; \$+\frac{1}{2}\$=6 per cent.\$; \$+\frac{1}{2}\$=8 per cent.\$; \$+\frac{1}{2}\$=8 per cent.\$; \$\frac{1}{2}\$=8 per cent.\$

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TO RECKON INTEREST AT 1 PER CENT PER MONTH.

Rule No. 1.—Multiply the Principal by  $\frac{1}{3}$  the given number of days and remove the decimal point three places to the left.

Find the interest on \$143 for 33 days at 1% per month.

$$$143 \times 11 \div 1000 = $1.573$$
 Ans.

Find the interest on \$428.50 from March 5th to July 29th.

0s. Days

3 5

 $\overline{4}$  24 = 144 days.  $\overline{\$428.50 \times 48} \div 1000 = \$20.568$  Ans.

Rule No. 2.—Multiply the Principal by the time in months and fractions of a month and remove the decimal point two places to the left.

Find the interest on the above examples by this Rule.

Interest at 1% per month is equal to 12% per annum; interest at 12% per annum; 4=3%; 3%; 3=4%; 3%; 3=5%; 4=6%, 3%; 3=7%; 3%; 3%; 3%; 3%; 3%; 3%; 3%; 3%; 3%; etc.

TO RECKON INTEREST BY CANCELLATION.

1st.—On the right of an upright line write the Principal, the time,—in days—and the Rate per cent.

2nd.—On the left the number of days, or its factors, in the year, and remove the decimal point two places to the left.

Find the interest on \$428.50 at 5% per annum of 360 days, from March 3rd to July 27th.

Ans. \$8.57

Find the interest on \$99 at 4% for 72 days.

$$\frac{99\times72\times4}{36\times10\times100} = .792$$
 Ans.

Find the interest on £428,10 Stg. at 5% per annum of 365 days from March 3rd to July 27th. Ans. £8,11,5.

See note on pages 46 and 59.

When the given rate is not a convenient part of five or six per cent., find the interest for the given time at one per cent., and multiply by the given rate.

TO RECKON INTEREST AT ONE PER CENT. PER ANNUM.

#### COMMON METHOD.

RULE.—To find the interest for one year, divide the Principal by 100; to find the interest for 36 days remove the decimal point three places to the left; for any other time or Rate, increase or diminish in the manner shown in the following examples.

Find the interest on \$1000 for 11 years, 1 month and 6 days, at 1 per cent. per annum.

Ans. \$111.00

\$ 10.00 int. for 1 0 0 at 1% == the Principal 
$$\div$$
 100  $100.00$  " 10 0 0 = first line  $\times$  10  $\frac{1.00}{111.00}$  "  $\frac{1}{11} \frac{6}{11} =$ " "  $\times$  .1  $\frac{1}{11} \frac{6}{11} =$ " at 1% per annum.

Find the interest on £124,,10,, Stg., from March 6th, 1882 to May 18th, 1883, at 7% per annum. Ans. £10,,9,,2.

The interest is found on all sums at 1 per cent. a month by removing the decimal point to the left, 3 places for 3 days, and 2 places for 30 days.

Find the interest on £143 for 1 mo. 3 da. at 1 per cent per month.

Ans. £1,,11, $5\frac{1}{2}$ .

£1.43 int, for 1 mo.  

$$.143$$
 " 3 days 1st line×.1  
£1.573

Nore 1.—The Decimal expression of values has the same significance whether the examples are stated in terms of the Pound Sterling, the Dollar, or any other Standard Coin. (See page 59.)

Nore 2.—Only a sufficient number of examples to clearly illustrate the working of the several rules are presented; the Teacher or the Student may furnish additional examples for exercises to any extent.

Note 3.—The answer to three decimal places is sufficiently exact; the time being less than one year, use only two decimal places in the principal

For Reckoning Interest at 5 per cent per year of 365 days.

 $\overline{1\times1} \div \overline{73\times100} = \overline{1\times1\times5} \div \overline{365\times100}$ 

RULE.—Multiply the Principal by the given number of days, remove the decimal point two places to the left and divide by 73.

Find the interest on £100 Stg. for 365 days at 5% a year.

 $\frac{£100\times365}{100\times73} = £5 \text{ Ans.}$ 

RULE No. 2.—To Reckon Interest at 5 per cent per annum.  $(1\times365+\frac{1}{8})+\frac{1}{10}$  and  $\frac{1}{100}$  of  $\frac{1}{8}\div10,000=.05$  nearly; the excess is exactly  $\frac{1}{10000}$ , hence the following.

RULE.—Multiply the Principal by the given number of days, Divide the Product by 3, and to it add the Quotient plus .1, plus .01 and remove the decimal point four places to the left.

Find the Interest on £100 for 365 days at 5% per annum.

3)36500=100×365 121666=the quotient. 12166=.1 Do. 1216=.01 Do. £5.0005=The Answer.

To Reckon Interest on the basis of a year of 365 days.

 $1 \times 1_{\frac{3}{10}} \div 1000 = 1 \times 42 \div 365 \times 100$  nearly.

The deficiency is about .0006 or 1150; six cents to be added to each \$100; one penny to each £7 of interest.

RULE.—Multiply the Principal by 130, remove the point three places to the left and the interest will be shown for

42 days at 1 per cent, 12 days at 3 per cent, 21 " 2 " 7 " 6 " 14 " 3 " 6 " 7 "

divide this interest by the number of days opposite the given rate and the Quotient is the interest for one day, multiply by the given number of days and add .0006 to the product.

Note.—To Multiply by  $1\frac{2}{10}$  add  $\frac{1}{10}$  and  $\frac{1}{2}$  of  $\frac{1}{10}$  of any number to itself.

EXAMPLE 1.—Find the interest on £100 for 7 days at 6 per cent per annum. Ans. 2s,,3\frac{3}{4}d.

100= the Principal,

10=.1= $\frac{9}{20}$  of the Principal,  $5=\frac{1}{2}$  of  $\frac{1}{10}=\frac{1}{10}$  of the Principal,

.115=the interest for 7 days at 6 per cent.

٠,

HOWARD'S LIGHTNING RULE FOR RECKONING INTEREST.

Divide 36 by any given Rate and the Quotient is the time, in days, in which the Interest on any given sum is equal to .001 of the Principal; in 10 times the Quotient the interest equals .01 of the Principal; in 100 times the interest equals .1; and in 1000 times the Quotient, the interest equals the principal.

Rule.—Divide 36 by the given Rate, Multiply the Principal by the given number of days, divided by the Quotient, and remove the decimal point three places to the left.

Find the interest on \$1000 for 9 days at 4% per annum.

$$36 \div 4 = 9$$
  $\frac{\$1000 \times 9}{9 \times 1000} = \$1.00$  Ans.

The interest for 9 days is \$1.000; for 90 days, \$10.00; for 900 days, \$100.00; and for 9000 days, \$1000.00, or the interest is equal to the Principal.

If millions of examples were written together in a column, the same denominations being placed exactly under each other; a straight line drawn three decimal places to the left, from the top of the column to the bottom, would show the interest on each, and every one of these millions of examples for 9 days at 4 per cent. per annum without altering one figure of the Principal; similar lines drawn two places, and one place to the left would show the interest for 90 days, and 900 days; thus doing the work of a long life in a moment of time.

$$36 \div 3 = 12$$
 the divisor at  $3\%$ .  $36 \div 9 = 4$  the divisor at  $9\%$   $36 \div 4 = 9$  "  $4\%$ .  $36 \div 12 = 3$  "  $12\%$   $36 \div 6 = 6$  "  $6\%$ .  $36 \div 18 = 2$  "  $18\%$ 

Find the interest on £428 Stg. at 9% per annum from July 27th, 1882 to March 3rd, 1883.

Yr. Mos. Days.  
83: 3: 3  
82: 7: 27 
$$\frac{428 \times 216 \ 54}{7: 6} = 23.112 = £23,2.3$$
. Ans

See note on pages 46 and 59.

## COMPOUND INTEREST.

Compound interest is interest on the principal, and also on the interest added to the principal, each time it becomes due.

Rule.—Multiply the principal by the rate, setting the product under, and two decimal places to the right of the principal; the sum of principal and interest will be the amount.

Or, find the amount of £1, or \$1, for the given time and rate, and multiply by the given principal.

Note.—To avoid writing decimals of no value, begin at the third decimal adding in the figure carried, if any, from the right hand figures.

Find the amount of £864 10s. 0d. for six years at 8%. Ans. £1371 17s.  $0\frac{3}{4}$ d.

School Book Method, 184 Figures.

69160

8645

746928

93366

1008.3528

933,660

Note.—Persons having frequent occasion to compute compound interest may save time and labor by the use of a table showing the amount of one pound, or one dollar, for a series of years, or other stated periods; the amount of one pound, or one dollar, for the given time and rate, multiplied by the given number of pounds, or dollars, will be the amount sought. (See page 65.)

Howard's Method, 74 Figures.

864.5 69.16 933.66 74.693 1008.353 80.668 1089.021 87.122 1176.143 94.091 1270.234 101.619 £1371.855  $\begin{array}{c} 80668224 \\ 10083528 \\ \hline 1089,021024 \\ 8 \\ \hline 8712168192 \\ 1089021024 \\ \hline 1176,14270592 \\ 8 \\ \hline 940914164736 \\ 117614270592 \\ 1270,2341223936 \\ 8 \\ \hline 101618729791488 \\ \end{array}$ 

1270.2341223936 £1371.85285.2185088 Paying Simple Interest for fractions of any given single period is usual, but it involves a loss to the Payer, because Simple Interest is more than Compound interest for any portion of any single period. Estimating our National debt at \$2,000,000,000 and the average Interest at 5 per cent, the Bondholders gain and the Nation losses \$1,890,673 a year by computing the quarterly payments at simple interest.

Every day's true Compound Interest differs, increasing as the day is distant from one.

Every day's true discount differs, decreasing as the day is distant from one,

The product of the amount for any two periods=the amount for the

sum of the two given periods.

The Square of the amount at Compound Interest for any given num-

ber of terms=the amount for twice that number of terms.

The Square Root of the amount for any given number of terms=

the amount for half that number of terms.

The Cube of the amount for any given number of terms=the amount.

for three times that number.

The Cube Root of the amount for any given number of terms=the amount for one-third that number.

Example.—\$10,000 invested at 10 per cent. per annum true Compound Interest is to be divided so that each of three sons on becoming 21 years old is to receive an equal sum; A is 17%, B 13% and C 10 years old; find how much each will receive and the present value of each son's share.

1st. Find the present worth of \$1 due in 3½, 7% and 11 years, true Compound Interest, then find the sum of the results.

2nd. Divide \$10,000 by this sum and the Quotient will be the amount due when each son comes of age.

3rd. Multiply this result by the present worth of \$1, as before found, for each son, and the products will be the present worths required.

1st.  $\frac{1}{1.226226}$  = present worth of \$1 for 3½ years = \$.8155104

1.563189 = present worth of \$1 for 7% years = \$.6397176

1.898298 = present worth of \$1 for 11 years = \$.5267875 Sum of results, \$1.9820155

2nd. \$10,000:-1.9820155=\$5045.37=sum each son will receive.

\$5045.37×.8155104=\$4114.55=present worth of A's share. " ×.6397176= 3227.61= " " B's " " ×.5207875= 2057.84= " " C's "

Another method. 1st.—Find, by Proportion, what sum invested for 31/4, and 7% years respectively will equal the amount of \$1 for 11 years.

2nd. Multiply each such investment by the \$10,000 and divide the product by the sum of the investments; the quotient is the present value of each son's share.

Note.—By computing simple, instead of true Compound Interest for the fractions of a year, the present values would be \$2658.62, \$227.38 and \$114.02, and the amount when of age, \$5046.86.

### DISCOUNT.

DISCOUNT is a certain per cent. deducted from, or allowance made for the payment of a debt or other obligation, before it is due. The PRESENT WORTH of any sum is a sum which if put at interest now at a given rate will amount to the required sum when due. True DISCOUNT is the difference between the *Present Worth* and the amount.

BANK DISCOUNT is simple interest on the Principal for a specified time, with three days added, called Days of Grace; a note for 3 months is due 3 months 3 days from date; a note for 90 days is due in 93 days; a possible difference of 2 days.

In reckoning Bank Discount the sum on which interest is to be paid, is known, but in reckoning True Discount we have to find what sum must be placed at interest so that the sum together with its interest may amount to the given Principal.

To find the present worth of any sum, and the true discount for any time at any rate per cent.

RULE.—Divide the given sum by the amount of \$1 for the given time and rate; the quotient will be the present worth, and the difference will be the discount.

Find the present worth and the true discount on \$1000 for 1 year at 10 per cent.

 $\frac{1000}{1,10}$ \$909.09 present worth, 1000-909.09=\$90.90 true dis.

Find the Bank Discount on a note for \$1000 for 1 year at 10% per annum. \$100+.83=\$100.83. Ans.

\$100=interest for 1 year. .83=interest for 3 days.

TO RECKON TRUE DISCOUNT, NEW METHOD.

RULE.—Write a common fraction that shows the part required, \* take the Denominator, plus 1, for a Divisor and the Principal for a Dividend, the Quotient is the true Discount.

\* The Quotient of the Reciprocal of the Rate, that is the Rate inverted, is the denominator of the fraction that shows the part to be taken,  $5\% = \frac{1}{100}$ ,  $\frac{180}{100} = 20$ ,  $5\% = \frac{1}{20}$ .

EXAMPLE.—An agent receives 10% on the net sum paid to his Principal, find his commission on \$1000.

$$10\% = \frac{10}{100} = \frac{1}{10} \ 10 + 1 = 11$$
,  $\frac{1000}{11} = $90.90$ . Ans.

COMMERCIAL DISCOUNT is a given Rate per cent. allowed off a *Debt* or part of a *Debt* for Cash, that is, "ready money;" and is reckoned the same as interest.

A bill of goods is bought, amounting to 960 dollars at a year's credit, the merchant offers to deduct 10% for ready cash, what amount is to be deducted?

$$\$960 \div 100 \times 10 = \$96.00$$
. Ans.

By discounting the face of bills, a loss may be sustained without suspecting it; this arises from the fact that the discount is not only made on the first cost of the goods, but also on the profits; for instance, if a profit of 30% be made on any article of merchandise, and the 10% be deducted, the gain at first sight would appear to be 20%, but is in reality only 17%. If a profit of 60% be added to the first cost, and then a discount made of 45%, the apparent profit would be 15%; instead of this, an actual loss is made of 12%, as will be seen by the following examples:

Example 1.	Example 2.			
Cost of goods,	\$100	Cost,	\$100	
Add 30% profit,	30	Profit 60%,	60	
Selling price,	130	Selling price,	$\frac{160}{72}$	
Deduct 10% discount,	13	Discount 45%,		
Cash price, Gain 17%.	\$1,17	Cash price, Loss 12%.	\$88	

The net amt. of a bill, less 10 per cent. discount, will be shown by multiplying by .9. Example. £100 $\times$ .9=£90.0

To find the net. amt. less discount at

5	per	cen	t×9⅓	. 30	per	cen	t X7.	50	per	cen	t X 5.
			X84				×6₫.	55	٠,	44	×43.
			X8.	40	"	66	×6.	60	"	"	X4.
25	"	"	X74	45	"	"	X 51.	70	"	"	× 3.
an	r h	emo	wa th	e point	1 n	lace	to the 1	eft.			

and remove the point 1 place to the left.

## PARTNERSHIP.

A Partnership or Firm is an association of two or more persons for the purpose of transacting business with an agreement to share the profits and losses according to the amount of capital furnished by each, and the time it is employed.

Capital or Joint Stock is the amount of money or property used in the business; the amount due together with the property of all kinds belonging to the firm, is sometimes called the Assets.

The Net Capital is the excess of assets over liabilities. The Liabilities of a firm are its debts.

To find each partner's share of the profit or loss.

RULE.—Multiply the whole profit or loss by the ratio of the whole Capital to each man's share of the Capital.

Example, A and B engage in trade, A furnishes \$300 and B \$400, they gain \$91; what is each man's share of the profits?

Capital \$300, 
$$\frac{3}{6}\frac{6}{6} = \frac{3}{4}$$
. Gain,  $\frac{91}{4} \times \frac{39}{4} = \frac{39}{4}$ 's Share.  $\frac{400}{4}\frac{400}{6}\frac{400}{6} = \frac{3}{4}$ . "  $\frac{52}{4} = \frac{52}{6}$ " "

Whole stock,\$700.

Whole profit, \$91

Another method:—Find the rate per cent. gained or lost, and multiply each person's share of the capital by the rate per cent.

$$\frac{91}{700}$$
=13%.  $\frac{300 \times .13}{400 \times .13}$ =39 \ =\$91.

When the respective capital of each partner is invested for unequal periods of time.

RULE.—Multiply each man's capital by the time it is employed, and regard each product as his capital, and the sum of the products as the entire capital.

Take the above example, A's capital being invested for four months, and B's for three months, and find each man's share of profits.

\$300 $\times$ 4=1200 \$91 $\times$ 12=\$45.50=A's share. 400 $\times$ 3=1200 91 $\times$ 12=45.50=B's "Profits \$91,00

#### EXCHANGE.

Exchange, in Arithmetic, is a method of finding the value of one denomination of money in the terms of another.

Exchange, in Commerce, is the paying, or receiving any sum in one kind of money for its value in another; when the parties are distant from each other this is done by means of an *Order* or *Draft* called a *Bill of Exchange*. Bills drawn in one Country and made payable in another are called *Foreign Bills*; when drawn and payable in the same country they are called *Inland Bills*.

PAR OF EXCHANGE is the established value of the Standard Coin of one country when expressed in terms of the Standard Coin of another; the value of £1 Stg. in U. S. gold coin is \$4.8665.—See page 100.—Exchange is at Par when a Bill in New York, for the payment of £100 Stg in London can be bought for \$486.65. Exchange is in favor of a place when it can be bought there at or above par; Exchange diverges from Par by the difference in the amount of the indebtedness between one country and another, called the Balance of Trade.

Find the value in currency of a gold dollar, the market price of currency being 75 cents.

Ans. 133\frac{1}{3} cents.

Process— 
$$\frac{100}{75} = \frac{4}{3} = 132\frac{1}{3}$$

2. Find the value of currency, the price of gold being 133½. Ans. 75 cents.

Process 
$$\frac{100}{1334} = \frac{3}{4} = .75$$

\$500 in gold at 8 per cent. premium will buy how much currency?  $$500 \times 1.08 = $540$ .

\$500 in currency will buy how much gold at 8 per cent. premium?

500-108=\$462.96.

\$1000 in gold is worth how much currency at 80 cents?  $1000 \div .80 = 1250$ .

What is the face value of a bill of Exchange cost. Commission 2 per cent? ing £1000.

£1000 $\div$ 1.0075=£992.55

What is the cost of a bill of Exchange for \$1000 Premium ? per cent.

 $$1000 \times 1.003 = $1007.50$ .

Find the par value of £473, 5, 9 St'g. in American gold coin.

£473.2875 $\times$ 4.8665=\$2303.25.

Note. To avoid encumbering the operation with valueless decimals, reverse the multiplier, and begin each line of the partial products with the product of the multiplying figure and the figure directly above

it, adding what otherwise would have been carried. The par value of £1 st'g is fixed by act of Con-

.237 gress 1873, at \$4.8665. 2303.254 Pounds Sterling × 4.866563 = the Par value of U.S. Dollar. U. S. Dollars × .2054838=the Par value of Pounds Stg.

# BRITISH MONEY.

Howard's new rules for Interest, Equation of PAYMENTS, &c., may be used with equal facility in dealing with British and other foreign money.

The British people would simplify all their monetary operations, and save millions every year in labor alone, by adopting the decimal system of currency. The cost and temporary inconvenience incident to the change would be trifling, almost nil, in view of the advantage to be gained. pound, the florin, the shilling and the sixpence might be retained. Make the smallest coin, the farthing, equal to the 1000 of a pound, and the thing is done.

See page 35.

473.2875 56.684

1893.150

378.630

28.39×3 F 2.839

NOTE.—By carefully observing and practicing the following instructions, the converting of shillings, pence and farthings into decimals of a pound, and vice versa, will become a purely mental and instantaneous operation.

- 1. For every two shillings, or florin, write .1, because two shillings is  $\frac{1}{10}$  of a pound stg.
- 2. For every 1 shilling, write .05, because one shilling is  $\frac{5}{10}$  of a florin, or  $\frac{5}{100}$  of a pound stg.
- 3. For every ninepence, write .0375, because ninepence is 10000 of a pound stg.
- 4. For every sixpence, write .025, because sixpence is  $^{25}_{100}$  of a florin or  $^{25}_{100}$  of a pound stg.
- 5. For the pence multiply 1, the given number of pence, by  $\frac{1}{12}$  of  $\frac{1}{2}$ .
- 6. For the farthings multiply 1, the given number of farthings, by  $\frac{1}{12}$  of  $\frac{1}{8}$ .

The learner may extend the exercises indefinitely, the essentials to remember are that florins, shillings, ininepence, sixpence and threepence are decimally expressed absolutely correct. The answer to three decimal places is sufficiently correct.

#### STOCKS AND BONDS.

A Bond is a duly certified instrument showing the indebtedness, with the limits and conditions of the debt,—of a Corporation or a Government.

Government Bonds are sometimes called Consols.

The capital of a company in transferable Shares, each of a certain amount, is called Stocks.

The value expressed on the face of any certificate of value, as Stocks, Commercial Paper, etc., is called the *Par Value*. When the market value is greater or less than par value, the Stock is said to be above or below *Par*, or is said to be at a *Premium*, or *Discount*, as the case may be.

To find to what rate of interest a given dividend corresponds.

Rule.—Divide the rate per unit of dividend by 1 plus or minus the rate per cent., premium or discount, according as the stocks are above or below par.

What per cent will be gained by investing in 8 per cent stock, at 20 per cent premium?

 $120 \mid 800 = 6\frac{2}{3} per cent.$ 

What per cent will be gained by investing in 6 percent stock at 10 per cent discount.

100-10=90.  $90 \mid 600=6\frac{2}{3}$  per cent.

To find at what price stock paying a given rate per cent. dividend can be purchased, so that the money invested shall produce a given rate of interest.

Rule.—Divide the rate per unit of dividend by the rate per unit of interest.

What must be paid for stock paying 6 per cent dividend, in order to realize on the investment 8 per cent?

8 \ 600=75.

#### TAXES.

A Tax is a sum of money assessed on persons or property for the purpose of defraying public expenses.

Real Estate is fixed property, such as houses and lands.

Personal Estate consists of money, cattle, ships, furniture and other movable property.

To find the rate of taxation, the required tax and the value of the taxable property being known:

RULE.—Divide the required tax by the value of the taxable property, the quotient is the rate of taxation.

Example.—The taxable property of a township is valued at \$4,835,000, the required tax is \$96,700; what is the rate?

 $\frac{96,700}{4.835.000}$ =.02 Ans. 2%, or 2 cents on each dollar.

The required tax divided by the rate=the valuation.

To find the amount of any person's tax.

Rule.—Multiply the value of the property by the Rate.

Example.—The assessed value of Oscar Wilde's property in Dublin is £48,500; the Rate is  $\frac{7}{8}$  of 1%; what is the amount of his Tax?

£48,500 $\times$ .00 $\frac{7}{8}$ =424;375=£424,,7,,6 Ans. •

#### DUTIES.

Duties are taxes paid on many kinds of goods imported from abroad and are collected by the Custom house officers; when the duty is a certain per cent. on the value of the goods it is called Advalorem duty; when the duty is on a certain quantity, as agreed, a pound, a gallon etc., it is called a Specific Duty.

A Tariff is a schedule showing the rates of duties fixed by law on all kinds of imported merchandise.

Gross weight or value is the weight or value of the goods before any allowance is made.

Net weight or value is the weight or value of the goods after all allowances have been deducted.

### INSURANCE.

Insurance is a contract of indemnity against loss or damages.

Fire Insurance is indemnity for loss of property by fire.

Marine Insurance is indemnity for loss of vessels or cargo-

Life Insurance is an agreement to pay a certain sum in case of the death of the insured.

The Insurer or Underwriter is the party who takes the risk; the written contract between the two parties is called the Policy.

The Premium is the sum paid for Insurance.

To find the Premium, the sum insured and the Rate being given.

Rule.-Multiply the sum invested by the rate.

To find what sum must be insured to cover both the Property and Premium, the Rate being given.

Rule.—Divide the value of the Property by 1 minus the Rate.

PROFIT AND LOSS.

To find the gain or loss per cent.

Rule.—Divide the gain or loss by the cost.

To find the selling price to gain a given per cent.

RULE.—Multiply 100, plus the gain per cent. by the cost and divide by 100.

To mark goods so that a given per cent. may be deducted and yet make a given per cent profit.

Rule.—Divide the real selling price by 1 minus the given per cent. to be deducted, the quotient is the marking price.

Example.—Bought hats at \$2.55 each, at what price must they be marked so that 15 per cent. may be deducted, and yet be sold at 20% profit.

\$2.55+20% = \$3.06 =the selling price.  $3.06 \div 1 - 15 = $3.60 =$ the asking price.

To mark goods to gain a given per cent. on the selling price: Divide the cost by 1, minus the required Rate per cent

See page 106.

### ALLIGATION.

Alligation treats of mixing or compounding two or more ingredients of different values or quantities; the process of finding the mean value or quantity of several ingredients, is called Alligation Medial.

RULE.—Find the entire cost, or value of the ingredients and divide it by the sum of the simples.

Alligation Alternate is the process of finding the proportional quantities to be used in any required mixture.

RULE.—Arrange the ingredinents in pairs, one of less and the other of greater value than the required value, the difference of one member of a pair and the required value is the required quantity of the other member.

To prove the answer, multiply each value by its quantity, and divide the sum of the products by the sum of the quantities.

Example.—Having four qualities of tea worth 1, 2, 3 and 4 dollars a pound, how much of each must be used to make a mixture worth 2½ dollars a pound.

$$2\frac{1}{4}\begin{cases} 1 \times \frac{1}{2} = \frac{1}{4} & \text{or } \begin{cases} 1 \times 1 = 1 \\ 3 \times 1 = 4 \\ 2 \times 1 = 3 \end{cases} & 2\frac{1}{4} \begin{cases} 4 \times 1 = 6 \\ 2 \times 1 = 3 \\ 4 \times \frac{1}{2} = 2 \end{cases} & 2\frac{1}{4} \begin{cases} 1 \times 1 = 1 \\ 4 \times 1 = 6 \\ 2 \times \frac{1}{2} = 1 \end{cases} & 2\frac{1}{4} \begin{cases} 1 \times 1 = 1 \\ 1 \times 1 = 1 \\ 1 \times 1 = 1 \end{cases}$$

By the first arrangement we get  $\frac{1}{2}$ ,  $1\frac{1}{2}$ ,  $1\frac{1}{2}$  and  $\frac{1}{2}$  as the required quantities, in all 4 pounds, costing \$10, an average of  $2\frac{1}{2}$  dollars a pound.

Questions in Alligation may have different answers, the preference for any one depends upon the quantity of particular ingredients on hand.

For adjusting the fineness of Gold and Silver, see page 119.

### BARTER.

Barter is the exchange of commodities.

Rule.—Divide the given quantity of the given commodity and its price by the constituents of the commodity whose value is required.

Example.—How much tea at 64 cents a pound must be given for 448 pounds of cheese at 20 cents a pound?

$$8 \times 8 = 64$$
.  $448 \times 20 = 140$  lbs. Ans.  $8 \times 8$ 

### ANNUITIES.

## MODEL OF ANNUITY TABLE, ANNUITY £1, RATE 5 PER CENT

Years.	Amount.	Present Worth	Amt. of Annuity.	Pres. Worth of Ann.
1	1.05	.95238095	1	.95238095
2	1.1025	.90702947	2.05	1.85941042
3	1.157625	.86383759	8.1525	2,72324801
4	1.21550625	.82270247	4.310125	3.54595048
5	1.27628156	.78352616	5.52563125	4.32947664

The amount of an annuity of £1=the compound interest on one pound; the Rate, hence the amount of an annuity of £1 forborne for three years=.157625;.05=3.1525.

The Present value of an annuity of £1 for any number of terms = the compound interest  $\div$  the Rate  $\times$  the amount; thus the Present Worth of an annuity of £1 for three years at 5% =1.157625 =2.72324801=£2,,14,,5}

The amount of £1 for any given time and rate Multiplied by the Rate per cent. divided by the compound interest equals the annuity that £1 will buy.

To find what Annuity, or monthly sum, for any number of terms, a given sum will buy.

RULE.—Multiply the given Principal by the Annuity or the monthly payment that one Pound, or one Dollar will buy.

EXAMPLE.—What must be one of six equal annual payments to discharge a loan of £864,10 for six years at 8%.

$$\frac{£1.5869 \times .08 \times 864.5}{.5869}$$
 =£187. Ans. £187,,0,0.

To find the cost of a given annuity, for any time. and Rate.

Rule.—Multiply the Present Worth of an Annuity of £1 for the given time and Rate by the given number of Pounds.

EXAMPLE.—Find the cost of an Annuity of £187 Stg. for six years, interest 8 per cent, per annum.

$$\frac{.5869 \times 187}{.08 \times 1.5869}$$
 = 864.5 £864,,10,,0. Ans.

# COMPOUND INTEREST TABLE.

TABLE showing the amount of one Pound sterling, or one Dollar at various rates per cent. for from one to twenty years, or other periodical terms.

This Table will serve as a model for making Compound Interest Tables for any number of terms, at any rate per cent. See Note, page 52.

1				7 per ct.	8 per ct.	10 per ct.
	1.010000	1.050000	1.060000	1.070000	1.080000	1.100000
2	1.020100	1.102500	1.123600	1.144900	1.166400	1.210000
3	1.030301	1.157625	1.191016	1.225043	1.259712	1.331000
4	1.040604	1.215506	1.262477	1.310796	1.360489	1.464190
5	1.051010	1.276282	1.338226	1.402552	1.469328	1.610510
6	1.061520	1,340096	1.418519	1.500730	1.586874	1.771561
7	1.072135	1.407100	1.503630	1.605781	1.713824	1.948717
š l	1.082856	1.477455	1.593848	1.718186	1.850930	2.143589
9	1.093685	1.551398	1.689479	1.838459	1.999004	2.857948
10	1.104622	1.628895	1.790848	1.967151	2.158924	2.593742
ii	1.115668	1.710340	1.898299	2.104851	2.331638	2.853116
12	1.126825	1.795857	2.012197	2.252190	2.518169	3.138428
13	1.138093	1.885650	2.132929	2.409843	2.719628	3.452271
14	1.149474	1.979933	2.260905	2,578532	2.937193	3.797498
15	1.160969	2.078929	2.396559	2.759029	3.172169	4.177248
16	1.172578	2.182875	2.540355	2.952161	3.425942	4.594973
17	1.184303	2.292019	2.692776	3.158812	8.700017	5.054470
18	1.196146	2.406620	2.854343	3.379929	3.996018	5.559917
19	1.208107	2.526951	3.025603	3.616524	4.315699	6.115908
20	1.220188	2,653298	3.207139	3,869681	4,660955	6.727498

72 divided by the given rate will show the time in years in which any sum of money will double itself at Compound Interest; nearly.

The square of the amount for any given number of terms equals the amount for twice the given number of terms.

The cube of the amount for any given number of terms equals the amount for three times that number.

To prove interest: divide the computed interest by the interest for one day; the quotient should be the number of days in the example; or divide by the interest for one month: the quotient should be the number of months.

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# EQUATION OF PAYMENTS.

EQUATION OF PAYMENTS is the process of finding the EQUATED TIME, or the date when the sum of several debts due at different times may be paid.

AVERAGING ACCOUNTS is the process of finding the date on which the BALANCE is due.

Partial Payments are parts of a debt paid at different times; usually written on the back of notes and other interest bearing obligations, and called indorsements. The term also includes payments made on account of a debt before it is due.

THE TERM OF CREDIT is the time to elapse before a bill becomes due.

THE AVERAGE TERM of credit is the time at the end of which the sum of several debts due at different dates may be paid at once.

THE EQUATED TERM is the average time for which interest is due on an account, or balance, and is always reckoned from the Zero Date.

THE ZERO DATE is the date,—or starting point,—from which all the other dates are reckoned; in this rule it is always the beginning—or starting point—of the month in which the first debt in the account occurs.

An Account is a statement of business transactions between Debtor and Creditor.

A BALANCE is the difference of two sides of an account.

A CASH BALANCE is the same, with the interest due.

The Creditor is entitled to *Interest* on the Balance from the date on which it is due to the date of settlement. The debtor is entitled to *Discount* off the Balance for the time he pays it before it is due.

### BILLS BOUGHT ON UNEQUAL TIME ON THE SAME DATE.

On what date may the whole £300 be paid?

Under the terms of this transaction the Debtor is entitled to the use of

The product of any number of pounds multiplied by any number of months, and fractions of a month, a Debtor is entitled to use them, is the number of pounds he is entitled to use for 1 month under the same terms, hence the following:—

Rule.—Multiply each debt by its term of credit, divide the sum of the products by the sum of the debts, and the quotient is the equated term.

First study this very simple example thoroughly, make yourself familiar with each operation, the reason for its use, and the causes of the results, and you will then have no difficulty in comprehending the most complex Debtor and Creditor accounts.

### BILLS BOUGHT ON EQUAL TIME AT DIFFERENT DATES.

Required the equated time of paying the following bills each bought on 8 months credit.

No of months, 
$$\frac{1878}{\text{June}}$$
 0—Zero date. from zero date  $\frac{1}{1}$   $\frac{1}{1}$   $\frac{9}{1}$   $\frac{1}{1}$   $\frac{1$ 

mo. da. yr. mo. da. 11.4

Equated term 2, 11 after 78, 6, 0 zero date.

Plus term of Cr. 8, 0 = 10, 11,

Equated time 79, 4, 11, or April 11th, 1879.

Rule,—Multiply each debt by the time—in months and fractions of a month,— between its occurrence and the zero date, divide the sum of the products, by the sum of the debts, and the quotient is the equated term—in months and hundredths of a month,—counting from the zero date, add the term of credit, and the sum is the equated time.

NOTE 1. To reduce hundredths of months to days, multiply by 3, and point off the right hand figure, when the right hand figure in the product is 5 or more add 1 day, otherwise disregard it.

NOTE 2, When the figures representing the day of the month are multiples of 3, such as the 3d, 9th, 27th, &c. &c., multiply by tenths, because 3 days is .1 of a month; when they are not multiples of 3 then multiply by the simplest fraction, or fractions of a month. In the above example, Sept. 14th, 3 months 14 days from zero date, we multiply by 3.3 1, 3 months, plus 9 days, plus 5 days. Facility in selecting the simplest fractions for multipliers is easily acquired by practice.

BILLS BOUGHT ON UNEQUAL TIME AT DIFFERENT DATES.

Required the equated time of paying the following bills of goods.

Term of Cr. Mos.	April	0				
6	"	10	To M	ſdse.	£310×63	$=\{^{1860}_{108}$
2	1 May	21	"	e,	468×3.7	$=$ $\begin{cases} 1404 \\ 328 \end{cases}$
4	2 June	1	":	"	$520 \times 6\frac{3}{3}$	$=\{^{3120}_{17}$
3	3 July	8	"	"	$520 \times 6\frac{1}{30}$ $750 \times 6.1$	$=\begin{cases} 4500 \\ 75 \\ 195 \end{cases}$
-	ate ed term	5	Da. 0 19	_	2048	)11532(5.63
Equate	ed time	9	19 or	Sept.	19th.	18.9

Rule—Multiply each debt by the term of credit, plus the time between the date of the transaction and the zero date; divide the sum of the products by the sum of the debts, and the quotient is the equated term.

The figures on the extreme left represent the terms of credit; the figures on the left of the month represent the number of months from the zero date, these together with the day of the month are the multipliers.

Note.—The use of the beginning of the month, instead of the date of the first transaction for the starting point, makes no difference in the ultimate result, and avoids the continual labor of finding on each item, the time between two dates, each date as written, itself representing the time.

## AVERAGING ACCOUNTS.

	the	e e	quat	ed time of p	payin	g the ba	ılaı	nce	of the	: followir	ig accts
1878				Dr.		1878	_			Cr.	_
Mar.	0					Mar	0				,
6.	15	8	mos.	600×3½=	1800 800	2 мау	10	Ву	Cash	300×2×	$= \begin{cases} 600 \\ 100 \end{cases}$
1 Apr.	3	4	"	700×5.1=	3500	4 July	1	"		400×4⅓₀	
2 May	10	в	"	1000×8⅓=	8000 833	5 Aug	15	"	46	500×5⅓:	$=\left\{ \substack{2500 \ 250} \right\}$
	•	•		2300	14003	•				1200	5063
				1200	5063						
			_	1100	18940	R 19					

Balance due Nov. 4th, 8 mos. 4 days after zero date.

1877				Cr.			1877			Dr.	
June 1 July	0	Ву	Note	158×1.	11/0=	158	June	0 20	To Goods	986×%	$=\begin{cases} 329 \\ 329 \end{cases}$
	18			228×6.		5 1368	5 Nov.		l	152×5¾	$y_{5} = \begin{cases} 760 \\ 51 \\ 80 \end{cases}$
1878 9 Mar	5	"	ee	450×9¹	/6 =	137 4050 75	1878 8 Feb.	26	" "	110×8.7	- 000
		ı		836		5809	l		ا _	<u> </u>	( is
					412	2474	(8.09		_	1248 836	2213
Zero Minu		te	77	7, 6, 8,	0 3			m	o. 8da be	412 efore zei	o date.
			7	76, 9,	27 Ba	lance	due Se	ept	. 27th, 18	76.	•

Note.—The Dr. and Cr. sides are here transposed for convenience.

In this example the balance of the products is on the smaller side of the account; when this happens the equated term is deducted from the zero date to find the equated time.

The credit side has the ADVANTAGE of the use of the equivalent of £3335 for one month, then the other side is entitled to interest on the balance for as many months as 412 is contained in 3335.

Rule.—Multiply each item by the time between its occurrence and the zero date, added to the term of credit—if any— divide the balance of the products by the balance of the account and the quotient is the equated term.

### CASH BALANCES.

By the use of the following Rule the final desired result, the Cash Balance, may be found in less time than is required to find the Date on which the Balance is due.

RULE.—Multiply each item by the number of months and fractions of a month between its date and the date on which the Cash Balance is required; the difference of the sums of the Products ×.01 is the interest on the Balance at one per cent.

per month.

See note page 46.

Find the Cash Balance on the lower example page 70, March 5th, 1878; interest 1% per month. Ans. \$483.13.

1877	Dr.		1877			cr.	
June 20 Nov. 16 1878 Feby 26	To Goods. \$986 × 8½ ==  " 152 × 3.3½ ==  110 × .3 ==  \$1248 836	<b>( 456</b>	July Dec. 1878	4 18 5	By Cash	\$158 × 8, 228 × 2. 450 \$836	( 456
	Balance \$412 Interes	t \$71.13					

#### MONTHLY STATEMENTS.

Find the Cash Balance on the following account, at the end of the month, Interest 6% per annum. Ans. \$5345.73.

Jany. " " " " "	3 5 6 10 15 18 27	To Goods. " " " " "	$730.75 \times \frac{1}{2} \times \frac{1}{8}$ $815.00 \times .8$ $660.00 \times \frac{2}{3}$ $786.20 \times \frac{1}{2}$ $1000.00 \times .4$	= = = = =	757.1 609.0 652.0 440.0 393.0 400.0 49.6
\$33.00-+2=	=Int	t. at 6%.=	\$5329.23 Int 16.50 \$5345.73	at 12%	\$33.007

Interest at 1% per month is equal to 12% per annum; interest at 12% per annum; 4=3%; 3=4%; 3=5%; 4=5%; 4=5%; 4=5%; 4=5%; 4=5%; 4=5%; etc.

### PARTIAL PAYMENTS.

Bankers make a Business of loaning Money for Profit; they therefore find the *Amount* due at the date on which a Payment is made, deduct the Payment, and regard the Balance as a new *Principal*.

Merchants and Traders charge and allow the same Rate of Interest on both sides of the account.

BANKERS' RULE AT ONE PER CENT. PER MONTH INTEREST.

RULE.—Multiply the Principal by the number of months and fractions of a month between its date and the date of a Partial Payment, add the product × .01 to the Principal and deduct the Payment; the Balance is the new Principal.

A note is made for £1000 Stg. March 3rd, 1882, endorsed May 15th, £100, July 27th, £200, find the Cash Balance March 3rd, 1883.

Ans. £799,,18,,0.

£1000.00×2.4×.01=24.00. 1000+24.00—100=924= Bal. May 15 £924,0,0

924.00 × 2.4 × .01 = 22.176. 924 + 22.176—200 = 746.176 = Bal. July 27, 746,3,6 746.176 × 7.2 × .01 = 53.724 746,176 + 53.724 = 799.9 = Cash Bal. Mar. 3, 799,18

MERCHANTS AND TRADERS' RULE AT ONE PER CT. PER MONTH.

RULE.—Multiply each item by the number of months and fractions of a month between its date and the date of settlement; the Balance of the Products × .01 is the Interest on the Balance.

Find the Cash Balance on the above Note, Merchants and Traders Rule.

Ans. £796,,0,0.

May 15th,  $100 \times 9.6 = 960$ July 27th,  $200 \times 7.2 = 1440$   $1000 \times 12 = 12000$   $300 \times 12 = 2400$ 

2400 Bal. 700 Int. on Bal. 9600

£700+96=£796,,0,,0 Cash Balance March 3rd, 1883.

MERCHANTS AND TRADERS' RULE AT FIVE PER CT. PER ANNUM.

RULE.—Multiply each item by the number of days between its date and the date of settlement; divide the Balance of the Products by 3; to the Balance add the Quotient plus .1 plus .01, and remove the decimal point four places to the left.

Find the Cash Balance on the same acct. interest 5% May 15th.  $100\times292=29200$   $.1000\times365=36.5000$ 

May 15th,  $100 \times 292 = 29200$  .10 July 27th,  $200 \times 219 = 43800$   $\overline{73000}$ 

7.3000

9.7333 .9733

.0973

£700+40=£740,0,0. Ans. \*See page 50. 40.0040 \*

COMMERCIAL DISCOUNT is a given rate per cent. allowed off a Debt, or part of a Debt,—not off the money paid,—in consideration for Cash.

The terms of the following transaction are 6 months' credit; 7°/, discount for cash in ten days;

6% in one month; 4% in two months.

A discount of 7% enables £93 to pay £100, consequently every £100 paid discharges £107.5269 of the Debt: discounts at the other rates named result in like manner.

<i>Dr</i> 1883.			ount with Brown & Co. 1883.					
<sup>7</sup> an14	To Mdse. 6 mo.	2,147	583	Feb 18 Mch 13	" Discount 6 p. c.	500 31 300 12	269 91 <b>5</b>	
		2,147	583			2,147	583	
July14	To Balance	227	899		,			

On what date is the following balance due? Rule, page 70.

1883.	Dr.		1883.		Cr.	
Jan1	To goods, 6 mes	1500	March 1 May1	By Cash Balance .		300 400 800
Jan1	1500×6 =8	9000 2200 00)6800		300 × 2 = 400 × 4 =	•	600 1600 2200

Ans.-81 months after Jan. 1st,-Sept. 15th.

EXPLANATION.—Under the terms of this transaction the debtor is entitled to the use of \$1500 for 6 months, equal to 6 times 1500 or \$9000 for 1 month

entitled to the use of the balance for a time equal to the use of \$6800 for one month.

### CASTING OUT THE NINES.

The number nine has many peculiar properties in our system of notation. Any number is divisible by nine when the sum of its digits is divisible by nine.

Any remainder left after dividing a number by 9, will be left after dividing the sum of its digits by 9.

This peculiarity may be used with advantage in proving the four fundamental rules, by casting out the nines; that is, dropping 9 whenever the sum reaches or exceeds that number; thus to cast the 9s out of 846732, we say 8+4, less 9 leaves 3; 3+6 less 9 leaves 0; 7+5 less 9 leaves 3; hence the following.

To prove Addition, cast out the nines from the example, and from the ascertained sum; if correct the excess in each will be the same.

To prove Subtraction, the excess of the remainder should equal the excess in the minuend less the excess in the subtrahend.

Note. If the excess in the minuend is less than the excess in the subtrahend, it must be increased by nine.

To prove Multiplication. The excess of the product must equal the product of the excesses of the factors.

Note. If the multiplier or multiplicand is a multiple of nine, the product will have no excess.

To prove Division. The excess of the dividend must equal the product of the excesses in Quotient and Divisor plus the excess of the remainder.

Subtraction, by Addition, by the use of the Number Nine.

Rule. Write nine times the subtrahend under the minuend, add each figure of the upper number to the figure of the same order, and all the inferior places, of the lower number, carrying as in addition, and stopping at the last carrying figure.

### RAPID RULES FOR FARMERS.

The practice of buying or selling grain by the 100 pounds, or the *cental* system, is becoming almost universal, and has many advantages over the old practice of selling grain by the bushel.

The following rules for finding the relative values of the bushel and the cental are easy to learn, and true and rapid in execution.

To find the value per cental when the price per bushel is given.

RULE.—Set down the price per bushel; remove the decimal point two places to the right, and divide by the number of pounds in the bushel.

Example.—If wheat is \$1.80 per bushel, what is its value per cental?  $\frac{180}{60}$  = 3. Ans. \$3.

To find the value per bushel when the price per cental is given.

RULE.—Set down the price per cental; multiply by the number of pounds in the bushel, and remove the decimal point two places to the left.

In dealing with English market quotations write the given price per cental in pence, and divide by 20, the answer will be in shillings.

Example.—If wheat is quoted at 8s. 9d. per cental,

what is the value of a bushel?

8s. 9d.=105d.  $\frac{105\times60}{100}$ =63d., or  $\frac{105}{20}$ =5·25=5s.3d.

The price per cental in U.S. Dollars, multiplied by 4:11, equals the value per cental in English shillings, thus: wheat at \$3 per cental=4:11×3=12:33=12s. 4d.

NOTE—The number of pounds estimated to the bushel must conform to the local usage; in the above examples the bushel is assumed to be equal to 60ibs.

To find the number of cubic feet in a Hay Stack.

If the Stack is round, add the height to the eaves—in feet to  $\frac{1}{3}$  the height from the eaves to the top, Multiply this sum by the square of the diameter Multiplied by .7854; or Multiply by the square of the circumference Multiplied by .07958.

If the Stack is square find the height in the same way and Multiply the height by the square of one side.

If the Stack is rectangular with gable ends add the height to the eaves to ½ the height from the eaves to the top, Multiply the sum by the length of the stack Multiplied by the width.

The number of cubic feet to be reckoned for a ton, depends upon the character of the hay and local usuage.

### RAPID RULE FOR RECKONING THE COST OF HAY.

RULE.—Multiply the number of pounds by half the price per ton, and remove the decimal point thate places to the left.

EXAMPLE.—What is the cost of 764 lbs. of hay at \$14' per ton?

 $764 \times 7 \div 1000 = 5.348$ 

Note.—The above rule applies to anything of which 2,000 pounds is a ton.

To find the number of trees required to plant an acre.

RULE.—Divide 43560 by the number of square feet occupied by one tree.

The trees being eight feet apart, how many are required to plant an acre?  $\frac{43560}{8\times7} = 778$  trees. Ans.

#### TO MEASURE GRAIN.

RULE.—Level the grain; ascertain the space it occupies in cubic feet; multiply the number of cubic feet by 8, and point off one place to the left.

EXAMPLE.—A box level full of grain is 20 feet long, 10 feet wide, and 5 feet deep. How many bushels does the box contain? Ans. 800 bush.

Process—20 × 10 × 5 × 8 ÷ 10 = 800.  
Or, 1 0 0 0 ft. 
$$\frac{8}{800.0}$$

Note.—Exactness requires the addition of 44.5 bushels to every ten thousand U. S. Bushels.

Cubic feet×.779=Imperial Bushels nearly.

The foregoing rule may be used for finding the . number of gallons, by multiplying the number of bushels by 8.

If the corn in the box is in the ear, divide the answer by 2, to find the number of bushels of shelled corn, because it requires two bushels of ear corn to make one of shelled corn.

# RAPID RULES FOR MEASURING LAND WITHOUT INSTRUMENTS.

In measuring land, the first thing to ascertain is the contents of any given plot in square yards; then, given, the number of yards, find out the number of rods and acres.

The most ancient and simple measure of distance is a step. Now, an ordinary-sized man can train himself to cover 1 yard at a stride, on the average, with sufficient accuracy for ordinary purposes.

To make use of this means of measuring distances, it is essential to walk in a straight line; to do this, fix the eye on two objects in a line straight ahead, one comparatively near, the other remote; and, in walking, keep these objects constantly in line.

Farmers and others by adopting the following simple and ingenious contrivance, may always carry with them the scale to construct a correct yard measure.

Take a foot rule, and commencing at the base of the little finger of the left hand, mark the quarters of the foot on the outer borders of the left arm, pricking in the marks with indelible ink.

To find the area of a four-sided figure, the opposite sides being parallel

RULE.—Multiply the length and the breadth together, and the product is the area.

To find the area of a square, square one of its sides.

When the length of two opposite sides is unequal, add them together, and take half the sum and multiply by the breadth.

Example 1. How many square yards in a square piece of land, 101 yds. on each side?

Process—1012 =

Ans. 10,201 yards.

EXAMPLE 2. How many yards in a piece of land 60 yards long and 20 yards wide? Ans. 1200.

Process— $600 \times 2 = 1200$ .

Only a sufficient number of examples to clearly illustrate the working of the Rules are presented; the Teacher or Student may furnish additional examples for exercises,

EXAMPLE 3. How may yards in a piece of land, one side is 40 yards long, and the other side 60 yards long, parallel sides being 10 yards apart?

Process, 
$$\frac{40 + 60 \times 10}{2} = 500.$$
500 yards, Ans.

To find the area of any three-sided figure.

Rule.—Multiply the longest side into one-half the distance from this side to the opposite angle.

EXAMPLE.—What is the area of a triangular plot of land, the longest side of which is 80 yards, and the shortest distance from this side to the opposite angle 40 yards?

Process, 
$$\frac{40 \times 80}{2} = 1600 \text{ yds. Ans.}$$

To find how many rods in length will make an acre, the width being given.

Rule.—Divide 160 by the width, and the quotient will be the answer.

Example.—If a piece of land be 4 rods wide, how many rods in length will make an acre?

 $160 \div 4 = 40 \text{ rods Ans.}$ 

Note.—In measuring irregular plots of land divide it into rectangles and triangles, and take the sum of the measurements.

To find the number of acres in any plot of land, the number of rods being given.

RULE.—Divide the number of rods by 8, and the quotient by 2, and remove the decimal point one place to the left.

EXAMPLE.—In 6840 rods, how many acres? 423 acres Ans.

Process.— 
$$8)6840$$
  
 $2)855$   
 $42.78$ 

To find the number of acres, the number of yards being given.

Divide the number of yards by 4840 or its factors. Example.—Find how many acres in 21,780 yds.

$$\frac{21,780}{10\times11\times11\times4} = 4.5$$
 Ans.  $4\frac{1}{2}$  acres.

A circle encloses the largest area within the short est fence.

The length of a circular fence = the square root of the area  $\times 1\frac{1}{8} \times 3\frac{1}{7}$ .

Find the length in yards of a circular fence to enclose 10 acres.

$$\sqrt{48400} = 220$$
.  $220 \times 1_{\frac{1}{8}} \times 3_{\frac{1}{7}} = 780$  yards.

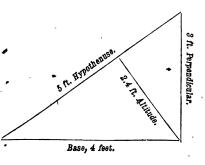
A square plot of the same area requires a fence 880 yards long.

The largest area enclosed within the shortest fence, in a rectangular plot, is a square.

3931 yards of fence will enclose a square plot of two acres; it would require 2 miles and 2 rods of fence to enclose the same area in a rectangular plot 1 rod wide.

# RAPID RULES FOR MECHANICS

To lay off a square corner. — Take a measure and lay off with it a triangle, one side of which is four ft long, another three feet, and the remaining side five ft., this triangle will be right-angled, and the two shorter sides will serve to lay off an exact square.



TRIANGLES.—The Area—the Base x half the Altitude.

The Area—\( \sigma \) of the product of half the sum of the three sides\( \times \) by the three remainders of each side subtracted from the half sum.

The Hypothenuse of the sum of the squares of the base and the perpendicular.

Or, divide the square of the Base by the sum of the Hypothenuse and the Perpendicular. Half the sum of the Divisor and the Quotient, equals the Hypothenuse.

A Diagonal line from the upper, to the opposite lower corner of a room = the square root of the sum of the squares of the length, breadth and height of the room.

Either Base or Perpendicular—Jof the difference of the squares of the Hypothenuse and the given side.

The Altitude  $\rightleftharpoons$  twice the quotient of the area  $\rightleftharpoons$  the given base, or the Hypothenuse being the base, divide the product of the two other sides by the Hypothenuse.

The number of board feet in a *Telegraph pole*, or any frustrum of a Pyramid,—four times the sum of the areas of the two ends and the mean\* in feet × the height.

The number of board feet in a wedge = twice the sum of the three parallel edges, in feet × the width of the Butt × the length.

The Area of a square constructed upon the Hypothenuse of a transle is equal to the sum of the areas of the squares constructed upon the other two sides.

A WEDGE,—the solidity  $\Longrightarrow_{\overline{t}}$  the sum of the three parellel edges  $\times$  by the breadth of the but  $\times$  by the length.

The Frustrum of a Cone, a Pyramid, or a Wedge, the Solidity= $\frac{1}{2}$  the sum of the areas of the two ends and the mean proportional  $\times$  the height.

The Mean Proportional of the Frustrum of a Cone, or the Frustrum of a Pyramid—the product of the diameters of the two ends; of the Frustrum of a Wedge—1 the sum of the products of either of the different edges of the butt×the other edge of the top.

The height of a Pyramid—the height of its Frustrum× the diameter of the Base+the difference of the two end

diameters.

To find the number of BOARD feet in a telegraph pole, the diameters being given in inches, and the height in feet.

If the two ends are square, multiply the sum of the squares of the two end diameters, plus the product of the two end diameters by \( \frac{1}{2} \) the height, and divide by 12. If the pole is round, multiply the squares of the two end diameters, plus the product of the two end diameters, by the heightx by 0218. For cubic feet x .001818.

Acoustics. — The time, in seconds, multiplied by 1125, gives, in feet, the distance of sound.

Gravity.—The square of the number of seconds × 1613—the distance, in feet, a body will fall in a given time.

Momentum.— The weight, in pounds the velocity in feet, per second, gives the momentum of bodies.

ATMOSPHERE.—The weight of the atmosphere, in pounds, at the surface of the ocean—the given area, in square inches × 15.

WATER POWER.—The weight or pressure, in pounds, of water at any given depth, on a square foot—the depth, in feet × 62½.

THE LATERAL pressure, in pounds—the area of the reservoir, × half its average depth × 62}

## MEASURE OF SUPERFICES AND SOLIDS.

Lineal Measure relates to length only, Superficial Measure to length and breadth; Cubic or Solid Measure to length, breadth and thickness.

- 1. If the floor of a room be 20 feet long by 18 feet wide, how many square feet are contained in it?  $180 \times 2 = 360$ . Ans. 360 feet.
- 2. If a board be 4 inches wide, how much in length will make a foot square? Ans. 36 inches.

  144 divided by the width, thus, 144=36.
- 3. If a board be 21 feet long and 18 inches broad, how many square feet are contained in it?

  Ans. 31½ sq. ft.

Process — Multiply the length in feet by the breadth in inches, and divide the product by 12.

$$\frac{21 \times 18}{12} = 31\frac{1}{2}.$$

Or thus, 18 inches equals  $1\frac{1}{2}$  ft.;  $21 \times 1\frac{1}{2} = 31\frac{1}{2}$ .

To measure a board wider at one end than the other, of a true taper.

Rule.—Add the widths of both ends together; halve the sum for the mean width, and multiply the mean width by the length.

Example.—How many square feet in a board 20 feet long, 9 inches in width at one end, and 11 inches at the other?

Ans. 162 sq. ft.

Process-

$$\frac{9+11}{2}$$
 = 10 in., mean width;  $\frac{20\times10}{12}$  = 163

To find the board measure of planks and joists.

RULE.—Multiply the length in feet, by the Product of the thickness and the width, in inches; and divide by 12.

EXAMPLE.—What is the board measure of a plank 18 feet long, 10 inches wide, and 4 inches thick?

Ans. 60 ft.

$$Process = \frac{18 \times 10 \times 4}{12} = 60.$$

To find how many board feet, one inch in thickness, can be sawed from a round log of any given length.

RULE.—Subtract four inches from the given diameter, square the difference, Multiply by the length in feet, and divide by 16.

How many board feet can be cut from a log 24 inches in diameter, 18 feet long?

$$24-4=20$$
  $20\times 20\times 18$  = 450 feet. Ans.

To find the cost of any number of feet of Lumber.

RULE.—Multiply the given number of feet by the price per 1000 and remove the point three places to the left.

To find how many solid feet a round stick of timber of the same thickness throughout, will contain when squared.

RULE.—Multiply the length by the Product of the diameter and the Radius, all in feet.

Find how many solid feet when squared, in a round log 2½ feet wide and 10 feet long.

$$\frac{5\times5\times10}{2\times4}$$
 =31.25 feet. Ans.

General rule for measuring timber to find the solid contents in feet.

RULE.—Multiply the depth, in feet, or fractions of a foot, by the breadth, multiplied by the length.

How many solid feet in a piece of timber 2 feet wide, 10 inches thick and 12 feet long.

$$\frac{2\times5\times12}{6} = 20 \text{ feet.}$$

To find the contents of a true tapered pyramid, whether round, square, or triangular.

Rule.—Multiply the area of the base by  $\frac{1}{3}$  the height.

How many cubic feet in a round stick of timber, truly tapering to a point,  $1\frac{1}{2}$  feet in diameter at the base and 24 feet long.

$$\frac{3\times3\times22\times8}{4\times4\times7} = 14.14 + \text{ feet.}$$

How many cubic feet in a square block of marble, truly tapering to a point, 24 inches on each side at the base, and twelve feet high.

$$\frac{24\times24\times4}{144}$$
 or  $2\times2\times4$ =16 feet, Ans.

The diameter being given, to find the circumference.

Rule.-Multiply the diameter by 31.

EXAMPLE.—What is the circumference of a wheel the diameter of which is 42 inches?

Ans. 11 ft.

$$\frac{42\times3\frac{1}{7}}{12} \quad \text{or} \quad \frac{7\times22}{2\times7} = 11 \text{ feet.}$$

To find the diameter when the circumference is given.

Rule.—Divide the circumference by 31.

EXAMPLE.—What is the diameter of a wheel, the circumference of which is 11 feet?

Ans. 3½ feet.

Process 
$$\frac{11}{1} \times \frac{7}{222} = 3\frac{1}{2}$$

What is the width of a circular pond, 154 rods in circumference?

Ans. 49 rods.

Process— 
$$7 \frac{154}{1} \times \frac{7}{22} = 49.$$

The diameter being given, to find the area.

RULE.—Multiply the square of the radius by 3½. Find the area of a circle 36 inches in diameter.

$$\frac{3\times3\times22}{2\times2\times7} = 7.07 \text{ feet.}$$

The length of a cylinder is equal to the capacity  $\div$  the square of the radius  $\div 3\frac{1}{7}$ .

Find the depth of a circular cistern, 7 feet wide, containing 2400 U. S. gallons.

$$\frac{2400\times2\times2\times2\times7}{15\times7\times7\times22} = 8.31 \text{ feet.}$$

To find the volume of a Cylinder.

RULE.—Multiply the square of the radius by the thickness, both in feet, or fractions of a foot, and the product by 34; or,

Multiply the square of the diameter by the thickness, both in inches, and divide by 2200, the answer is in cubic feet; or,

Multiply the square of the diameter by .7854, and that product by the length.

EXAMPLE.—How many feet in a grindstone 24 inches in diameter and 4 inches thick?

$$\frac{1 \times 1 \times 22}{3 \times 7} = 1.04$$
2nd Method.
$$\frac{24 \times 24 \times 4}{2 \times 11} = 1.04 \text{ ft.}$$

A Cylindrical foot is the volume of a cylinder, one foot in depth and diameter, and is equal to 1728 cylindrical inches. Cylindrical inches, ×.7854=cubic inches.

A Cylinder, — the surface = the circumference  $\times$  the length.

## TO MEASURE FREIGHT, ETC.

RULE.—Multiply together the length, breadth and depth of one package—in feet, and the largest fractions of a foot—and multiply by the given number of packages of the same dimensions.

Find the number of cubic feet in six packages, each

1ft. by 1ft. 2in. by 13ft.

$$\frac{1\times7\times7\times6}{6\times4}=12\frac{1}{4}\text{ft. Ans.}$$

Find the charges on 1000 cases, each  $16 \times 12 \times 6$  inches, at 16s. per ton of 40ft.

$$\frac{1000 \times 4 \times 1 \times 1 \times 16}{3 \times 2 \times 40} = .266\frac{2}{8}s. = £13 \text{ 6s. 8d.}$$

# Bricklayers' Work

Is sometimes measured by the perch, but more frequently by the 1000 bricks aid in the wall.

The following scale will give a fair average for estimating the quantity of brick required to build a given amount of wall:

$4\frac{1}{2}$	in. wall,	per	ft.,	superficial,	$\left(\frac{1}{2}\right)$	brick)	7	bricks.
9	"	"		46	(1	brick)	14	46
13	.46	"		66	$(1\frac{1}{2}$	brick)	21	46
18	"	"		"	(2)	bricks)	28	"
<b>22</b>	44	"		" (	21 1	bricks)	35	"

NOTE.—For each half brick added to the thickness of the wall, add seven bricks.

A bricklayer's hod measuring 1 ft. 4 in.  $\times$  9 in.  $\times$  9 in., equals 1,296 inches in capacity, and will contain 20 bricks.

A load of mortar measures 1 cubic yard, or 27 cubic feet; requires 1 cubic yard of sand, and 9 bushels of lime, and will fill 30 hods.

## Plasterers' Work

Is measured by the square yard, for all plain workby the foot, superficial, for plain cornices; and by foot, lineal, for enriched or carved mouldings in cornices.

## Painters' Work

Is computed by the superficial yard; every part is measured that is painted, and an allowance is added for difficult cornices, deep mouldings, carved surfaces, iron railings, etc. Charges are usually made for each coat of paint put on, at a certain price per yard per coat.

# SQUARE AND CUBE ROOT.

- 1. A square number multiplied by a square number, the product will be a square number.
- 2. A square number divided by a square number, the quotient is a square.
- 3. A cube number multiplied by a cube, the product is a cube.
- 4. A cube number divided by a cube, the quotient will be a cube.
- 5. If the square root of a number is a composite number, the square itself may be divided into integer square factors; but if the root is a prime number, the square cannot be separated into square factors without fractions.
- 6. If the unit figure of a square number is 5, we may multiply by the square number 4, and we shall have another square, whose unit period will be ciphers.
- 7. If the unit figure of a cube is 5, we may multiply by the cube number 8, and produce another cube, whose unit period will be ciphers.
- 8. If a supposed cube, whose unit figure is 5, be multiplied by 8, and the product does not give 8 ciphers on the right, the number is not a cube.

To prove cube root: from a cube number subtract its root; the remainder will be a multiple of 6.

From a number that is not a cube, subtract the ascertained part of its cube root; divide the difference by 6; then divide the remainder in the example by 6; the excess, if any, should in each case be the same.

#### TABLE

For comparing the natural numbers with the unit figure of their squares and cubes. By the use of this, many roots may be extracted by observation:

Numbers... 1 2 8 4 5 6 7 8 9 10 Squares... 1 4 9 16 25 36 49 64 81 100 Cubes.... 1 8 27 64 125 216 343 512 729 1000

The product of a number taken any number of times as a factor, is called a power of the number.

A root of a number is such a number as taken some number of times as a factor, will produce a given number.

If the root is taken twice as a factor to produce the number, it is the square root; if three times, the cube root; if four times, the fourth root.

By observing the above table, it will be seen that the square of any one of the digits is less than 100, and the cube of any one of the digits is less than 1000; therefore, the square root of two figures cannot be more than one figure.

The square of any number equals its root, plus the preceding square and root of a consecutive series.

$$4^2 = 16. \quad 4 + 9 + 3 = 16.$$

The units figure in the cube root of a perfect cube is the units figure in the *product* of the units figure of the cube multiplied twice into itself.

Find the cube root of 343.

The units figure  $3\times3\times3=27$ . Ans. 7.

The difference of the squares of two numbers equals their sum multiplied by their difference.

To find the square root of a number.

Use, to find the length of one side of a given square. RULE 1. Separate the given number into periods of two figures each, beginning at the unit's place.

The number of figures in the root equals the number of periods.

- 2. Find the greatest number whose square is contained in the period on the left; this will be the first figure in the root. Subtract the square of this figure from the period on the left; to the remainder annex the next period to form a dividend.
- 3. Divide this dividend, omitting the figure on the right, by double the part of the root already found, and annex the quotient to that part, and also to the divisor; then multiply the divisor thus completed by the figure of the root last obtained, and subtract the product from the dividend.
- 4. If there are more periods to be brought down, continue the operation in the same manner as be-

Note 1. If a cipher occurs in the root, annex a cipher to the trial divisor, and another period to the dividend, and proceed as before,
2. If there is a remainder after the root of the last period is found, annex periods of ciphers, and continue the root to as many decimal places as are required.

Example.—Find the square root of 643204.

64\32\04 (802 Square Root.

**1602**) 3204

or, Divide the number into two parts, take twice the Root of the larger part for a Divisor, and the other part for a Dividend, the sum of the two Roots is the Root required.

Ex.—Required the length of a ladder standing 80 feet from the Base, to reach the top of a cliff 798 feet high.

 $798 \times 2 + 4 = 1600)6400(4$  $80^{\circ} = 6400.$ 6400 798+4=802 ft. Ans. To find the cube root of a number.

Use, to find the length of one edge of a given cube.

RULE 1. Beginning at the units' place, separate the given number into periods of three figures each; the number of figures in the root will be equal to the number of periods.

2. Find the greatest number whose cube is contained in the left-hand period; this will be the first figure in the root; subtract its cube, and to the remainder annex the next period.

3. Multiply the ascertained part of the root by 3, then multiply that result by the first figure in the root, the product with two ciphers annexed is the first trial divisor.

4. Find how many times the divisor is found in the dividend and place the result in the root, and also to the right of the first term in the left hand column; multiply the last result by the new figure in the root and add the product to the trial divisor; the sum is the complete divisor.

5. Multiply the complete divisor by the second figure in the root, subtract the product from the dividend and

bring down the next period.

6. To find the next trial divisor add the square of the last found figure in the root to the preceding divisor and its smaller part; to the sum annex two ciphers, complete the divisor as before.

7. Repeat the foregoing process with each period until the exact root, or a sufficient approximation to it is found.

EXAMPLE.—Find the length of one edge of an excavation from which a cubic mass of earth = 1,745,337,664 cubic feet is to be taken. Ans. 1204 feet.

32	300	1,745,337,664(1	204, cube
1st complete divisor,	64	1	root.
		745 728	
3604	4,320,000 14,416	17,337,664	-
	4,334,416		

Note 1.—If a cipher occurs in the root, annex two ciphers to the trial divisor and another period to the dividend, and then proceed as before.

 If there is a remainder, after the root of the last period is found, annex periods of ciphers and proceed as before to as many decimal places as the answer requires.

The cube root of a fraction may be found by extracting the cube root of the numerator and denominator, or reduce the fraction to a decimal and extract the root.

# REFERENCE TABLES.

## MULTIPLICATION TABLE.

1	2	3	4	5	6	7	8	9	10	11	12
2 3 4 5 6 7 8 9 10 11 12	4 6 8 10 12 14 16 18 20 22 24	9 12 15 18 21 24 27 80 33 86	16 20 24 28 32 36 40 44 48	25 30 35 40 45 50 55 60	36 42 48 54 60 66 72	49 56 63 70 77 84	64 72 80 88 96	81 90 99 108	100 110 120	121 132	144

## ABBREVIATIONS USED IN BUSINESS.

A I, First Class.	\$, Dollar
@At.	GuarGuarantee.
% or Acc't Account.	GalGallon.
Am't Amount.	Hhd Hogshead.
Ass'dAssorted.	InsInsurance.
Bal Balance.	Inst This month.
BblBarrel.	InvtInventory
B. LBill of Lading.	IntInterest.
% Per cent.	Mdse Merchandise.
CoCompany.	Mo Month.
C. O. D Collect on Delivery.	Net Without disc't.
CrCreditor.	NoNumber.
ComCommission.	Pay'tPayment.
Cons'tConsignment.	PdPaid.
Cwt Hundred Weight,	Per An By the year.
DftDraft.	Pk'gsPackages.
Disc'tDiscount.	PerBy.
DoThe same	£,,s,,d, Pounds, shil'gs, pence
DozDozen.	Prem Premium.
DrDebtor.	Prox Next month.
E. E Errors excepted.	PsPieces.
EaEach.	Rec'dReceived.
Exch Exchange.	R. R Railroad.
Exps Expenses.	Ship't Shipment.
FolFolio.	Sund'sSundries.
Fw'dForward.	S. S Steamship.
Fr'tFreight,	UltLast month.

Specific Gravity is the weight of a body compared with another of the same bulk taken as a standard. The exact weight of a cubic inch of gold, compared with a cubic inch of water, is called its Specific Gravity. Water is the standard for solids and liquids. A cubic foot of rain water weighs 1000 ounces Avoirdupois.

Nors.—To find the weight, in ounces, of one cubic foot of any substance here named, remove the decimal point three places to the right.

Acid, Acetic	
Acid, Arsenic3.391	
Acid, Arsenic	
Acid, Nitric1.271	
Air	
Air,	
Dane	
Pure,	
Alderwood,	
Ale1.085	
Alum,	
A1	
Aluminum, 2.560	
Amber,	
Amethyst,2.750	
Ammonia	
Ammouia,	
Ash,	
Blood, Human 1.054	
Brass, (about)8.000	
D. 1-1-	
Brick2.000	
Butter,	
Cherry,	
Cider,1.018	
Cluer,	
Coal, bituminous, (about) 1.250	
" anthracite,1.500	
Copper,8.788	
0.540	
Coral	
Cork	
Cork	
Cork	
Coral,	
Coral,	
Corsl	
Corsl	
Coral     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Rther     632	
Corial     2.540       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923	
Corial     2.540       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923	
Corial     2.540       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923	
Corial     2.540       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923	
Corial     2.540       Cork     240       Diamond     8.550       Earth (mean of the Globe)     5.210       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold     19.362	
Corial     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.362       "Coin     17.647	
Coral     2.540       Cork     240       Diamond     3.530       Earth (mean of the Globe) 5.210     671       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.362       "Coin     17.647       Granite     2.625	
Corial     2.540       Cork     240       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Ether     632       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, harmered     19.362       "Coin     17.647       Granhite     2.625       Granhite     1.987	
Corial     2.540       Cork     240       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Ether     632       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, harmered     19.362       "Coin     17.647       Granhite     2.625       Granhite     1.987	
Corial     2.540       Cork     240       Cork     240       Diamond     8.530       Earth (mean of the Globe)     5.210       Elm     671       Ether     632       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, harmered     19.362       "Coin     17.647       Granhite     2.625       Granhite     1.987	
Coral	
Corial     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.302       "Coin     17.647       Granite     2.625       Graphite     1.987       Gunpowder     900       Gunshic     1.452       Gypsum     2.288	
Corial     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.302       "Coin     17.647       Granite     2.625       Graphite     1.987       Gunpowder     900       Gunshic     1.452       Gypsum     2.288	
Corial     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.302       "Coin     17.647       Granite     2.625       Graphite     1.987       Gunpowder     900       Gunshic     1.452       Gypsum     2.288	
Corial     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.362       "Coin     17.647       Granite     1.987       Graphite     1.987       Gunpowder     900       Gypsum     2.288       Hazel     600       Hematite Ore     4.705	
Corial     2.540       Cork     240       Diamond     8.530       Barth (meanof the Globe) 5.210     Elm       Elm     671       Emerald     2.678       Ether     632       Fat of Beef     923       Fir     550       Glass plate     2.760       Gold, hammered     19.362       "Coin     17.647       Granite     1.987       Graphite     1.987       Gunpowder     900       Gypsum     2.288       Hazel     600       Hematite Ore     4.705	
Coral	
Coral	
Coral. 2.540 Cork. 240 Diamond. 8.530 Barth (meanof the Globe) 5.210 Blm. 671 Emerald. 2.678 Ether. 632 Fat of Beef. 923 Fir. 550 Glass plate. 2.760 Gold, hammered. 19.302 "Coin. 17.647 Granite. 2.635 Graphite. 1.987 Gunpowder. 900 Gum Arabic. 1.452 Gypsum. 2.288 Hazel. 600 Hematite Ore. 4.705 Honey. 1458 Ice. 930 Lodine. 4948	
Coral	

Tron	7.648
Iron, Ore,	
T	1 017
Ivory, Lard,	1.811
Lard,	.94/
Lead, cast,	1.350
" white,	7.235
Lignum Vitae,	1.333
Lime	.804
44 stone	2.386
Mahogany,	
Malachite	9 700
Malachite	0.100
maple,	.700
Maple, Marble, Men (Living,)	2,710
Men (Living,)	.891
mercury, pure,	4.000
Mica	2,750
Milk,	1.032
Naptha,	.700
Nickel,	970
Nitre,	1 000
Nitre,	1 100
Oak,	1.110
Oil, Castor	.970
Opál,	Z.114
Opium,	1.337
Opium,Pearl,	1.337 2.510
Opium,Pearl,	1.337 2.510 7 471
Opium,Pearl,	1.337 2.510 7 471
Opium, Pearl, Pewter, Platinum Wire,2	1.337 2.510 7.471 1.041
Opium, Pearl, Pewter, Platinum Wire, 2 Poplar.	1.337 2.510 7.471 1.041 .883
Opium, Pearl, Pewter, Platinum Wire, Popplar,	1.337 2.510 7.471 1.041 .883 2.385
Opium, Pearl, Pewter, Platinum Wire, 2 Poplar, Porcelsin, Quartz,	1.337 2.510 7.471 1.041 .883 2.385
Opium, Pearl, Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin	1.337 2.510 7.471 1.041 .883 2.385 <b>2</b> .500 1.100
Opium, Pearl, Pewter, Platinum Wire, 2 Poplar, Porcelain, Quartz, Rosin, Salt	1.337 2.510 7.471 1.041 .383 2.385 8.500 1.100 2.130
Opium. Pearl. Pewter. Platinum Wire, 2 Poplar, Porcelain, Quartz. Rosin, Salt. Sand.	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 1.750
Opium, Pearl, Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, 1	1.337 2.510 7.471 1.041 .883 2.385 2.385 2.100 1.100 2.130 1.750 0.584
Opium, Pearl, Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, 1	1.337 2.510 7.471 1.041 .883 2.385 2.385 2.100 1.100 2.130 1.750 0.584
Opium, Pearl, Pearl, Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Slate, Steel	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 1.750 0.584 2.110 7.816
Opium, Pearl, Pearl, Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Slate, Steel	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 1.750 0.584 2.110 7.816
Opium, Pearl, Pearl, Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Slate, Steel	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 1.750 0.584 2.110 7.816
Opium Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silate, Steel, Stone, Tallow,	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 0.584 2.110 7.816 2.504 7.901
Opium Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silate, Steel, Stone, Tallow,	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 0.584 2.110 7.816 2.504 7.901
Opium Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silate, Steel, Stone, Tallow,	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 0.584 2.110 7.816 2.504 7.901
Opium Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silate, Steel, Stone, Tallow,	1.337 2.510 7.471 1.041 .383 2.385 2.500 1.100 2.130 0.584 2.110 7.816 2.504 7.901
Opium Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silver coin, Tallow, Tin, Trunpentine, spirits of, Wainut, Water, distilled	1.337 2.510 7.471 1.041 2.883 2.500 1.100 2.130 1.750 0.584 2.110 7.816 2.500 941 7.291 671 1.000
Opium. Pearl. Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silete, Stone, Tallow, Tin, Turpentine, spirits of, Wainut, Water, distilled, Wax,	1.337 2.510 7.471 1.041 1.883 2.385 2.385 2.500 1.700 2.130 7.816 2.500 .941 7.291 .671 1.000
Opium, Pearl, Pearl, Pewter, Platinum Wire, Poplar, Porcelsin, Quartz, Rosin, Salt, Sand, Silver coin, Slate, Steel, Stone, Tallow, Tin, Turpentine, spirits of, Walnut, Water, distilled, Wax, Willow,	1.337 2.510 7.471 1.041 1.883 2.385 2.500 1.100 2.130 0.584 2.500 .941 7.291 .870 .671 1.000 .897 .585
Opium. Pearl. Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Salt, Silver coin, Silver coin, Tallow, Trin Turpentine, spirits of, Walnut, Water, distilled, Waz, Willow, Wine,	1.337 2.510 2.510 1.041 1.041 1.883 2.385 2.500 1.100 2.110 7.816 2.501 7.891 7.291 870 .671 1.000 .897 .585 .599
Opium. Pearl. Pearl. Pewter, Platinum Wire, Poplar, Porcelain, Quartz, Rosin, Salt, Sand, Silver coin, Silete, Stone, Tallow, Tin, Turpentine, spirits of, Wainut, Water, distilled, Wax,	1.337 2.510 2.510 1.041 1.041 1.883 2.385 2.500 1.100 2.110 7.816 2.501 7.891 7.291 870 .671 1.000 .897 .585 .599

```
\times 3.1416
                                   =The Circumference.
                     -÷ .3183
                     \times .8862
                                    =The side of an equal
The Diameter
                     \div 1.1284
                                       Square.
                                    The side of an inscribed
  of a Circle.
                     \times .866
                     \div .1547
                                       Equilateral Triangle.
                     ×.707=The side of an inscribed square
                     ×the Radius=The area of
                     \times .3183
                                  =The Diameter.
                     +3.1416
                     \times .2821
                                  The side of an equal
                     +3.545
                                       Square.
The Circumfer-
                     \times .2756
                                  =The side of an inscribed
ence of a Circle.
                     +3.6276
                                       Equilateral Triangle.
                     \times .2251
                                  =The side of an inscribed
                     <del>+4</del>.4428
                                       Square.
                     \times .15915
                                  =The Radius.
                     \div 6.28318
                     \div 3.1416
                                  =The square of Radius.
The Area of a
                     ★1.2732
                                  =The square of Diameter
                     \div .7854
     Circle.
                     \times 12.5663
                                  =The square of Circum-
                     ÷ .07958
                                       ference.
  The Chord and Sine of an Arc or Segment of a Circle
peing given, the Diameter=the Sine, plus the quotient of
the square of half the Chord the Sine.
  The Surface of a Sphere, =(\text{circumference})^{\circ} \times .3183.
                    Surface \times 1-6 its Diameter.
                     (Radius)3 × 4.1888
The Volume
                     (Diameter)^3 \times .5236
 of a Sphere
                     (Circumference)^3 \times .0169
The Diameter__
                   \checkmark of Surface \times .5642
                   \sqrt[3]{} of Volume \times 1.2407
 of a Sphere
                   \checkmark of Surface \times 1.77255
The Circum-
                   \sqrt{3} of Volume \times .38978
  of a Sphere
                   \checkmark of Surface \times .2821
The Radius of_
                   \sqrt[4]{} of Volume \times .6204
  a Sphere
  The Area of a Circle=1 the product of the circumfer-
ence × the radius.
   An Ellipse.—The area equals the product of the two
diameters \times .7854.
```

The height of any object—the length of its shadow X the height and ÷ the length of the shadow of any other object.

it displaces when immersed.

The Solid contents of any Body=the volume of water

# Longitude reckoned from the Meridian of Greenwich. NORTH AND SOUTH AMERICA.

Place.	Lat.	Long.	Place.	Lat.	Long.
-	0 /	0 /		0 /	0 /
Albany, N. Y.	42 40 N	78 45w	Lima,	12 8 s	77 6
AnnArb'r, Mich	42 17	83 43		84 40 N	92 12
Annapolis, Md.		76 29		38 8	85 30
Augusta, Me		69 50		19 26	99 5
Austin, Texas.	80 13	97 39		43 2	87 54
Baltimore, Md.		76 37		30 41	88 1
Bangor, Me		68 46		45 81	73 33
Boston, Mass		71 03		41 18	72 55
Brooklyn, N. Y.	40 42	73 58		29 58	90 2
Buffalo, N. Y	42 50	78 59		40 43	74
Burlington, Vt.		73 10	Ottawa, C. W	45 23	75 42
Buenos Ayres.		58 22	Philadelphia Pa	39 57	75 9
Cambr'ge, Mass				37 14	77 24
Cape May, N. J.		74 57	Portland, Me	43 89	70 15
Cape Horn		67 16		41 49	71 24
Charleston, S. C.		79 56	Quebec C. E.	46 40	71 12
Chicago, Ill	41 54	87 38		37 82	77 26
Cincinnati, O		84 30	Rochester, N. Y	43 8	77 51
Columbia, S. C.	84	81 02		22 56 B	43 9
Concord, N. H.	43 12	71 29		32 5 N	81 5
Council Bluffs.		95 48		38 35	121 28
Des Moines, Io.		93 40		29 48	81 6
Detroit, Mich.	42 20	83 2		38 87	90 15
Detroit, Mich Dover, Del	39 10	75 30	St. Paul, Minn		95 5
Dubuque, Io	42 30	90 40	Salt Lake City	40 46	112 6
Fred'cab'rg, Va		77 27		37 48	122 47
Fort Laramie		104 48		85 41	106 1
Ft. L'v'wth, Ks.		94 44		39 48	89 83
Frankfort, Ky	88 14	84 40	St. Joseph's, Mo		94 52
Galveston, Tex	29 18	94 47	Syracuse, N. Y	43 8	76 9
Georgetown,		· · ·	Toronto, C. W	43 81	79 23
Bermuda, W. I.	32 22	64 87	Trenton, N. J.		74 45
Guayaquil		79 53	Troy, N. Y.	42 44	73 41
Havana	23 9 N		Valparaiso,	33 7 a	71 41
Halifax	44 89	63 35	WASHINGTON	38 53 N	77 0
<ul> <li>Harrisburg, Pa.</li> </ul>	40 16	76 50	Washington West Point, N. Y.	41 23	73 57
Hartford, Conn	41 46	72 41	Wheeling, W. Va	40 7	80 42
Ind'nap'lis, Ind	39 55	86 5	Wilmington Del	34 14	77 57
Jeffer' City, Mo	88 86 N	92 8	Wilmington, Del Worcester, Mass	42 16	71 48
Key West, Fla,	24 33	81 47	Yorktown, Va	37 13	76 34

A difference of 15 degrees of Longitude equals a difference of one hour of time.

The degrees of Longitude between two cities, multiplied by 4,
equals, in minutes, the difference of time.

For a difference of	There is a difference of	For a difference of	There is a difference of
15° in Long.	1 hr. in Time. 1 min." "	10 " "	4 min." " 4 sec. " "
15" " "	1 sec. " "	1" " "	1-15 sec. in time

## EUROPE, ASIA, AFRICA, AND THE OCEANS.

Place. ,	Lat.	Long.	Place.	Lat.	Long.
	<del>。,</del> -	- <del></del>		0,	0 /
Antwerp	51 13 N	4 24 B	Leghorn	43 82	10 18 E
Alexandria	31 12	29 53	Leipsic	51 20	12 22
Archangel		40 33	Lisbon	38 42	9 9w
Athens		23 44	Moscow	55 40	85 83 E
Aleppo		37 10	Malta	35 54	14 80
Algiers		34	Messina	38 12	15 35
Amsterdam	52 22	4 53	Mocha	13 20	43 12
Borneo	5	115	Muscat	28 87	58 85
Botany Bay		151 13	Marseilles	48 18	5 22
Barcelona		2 11	Manilla	14 86	121 2
Bombay	18 56	72 54	Madras	14 4	80 16
Bremen	53 5	8 49	Madrid	40 25	3 42W
	52 80	13 24	Malaga	36 43	4 26
Brussels		4 222	New Zealand		173 1 E
Cape Clear	51 26	9 29w	New Hebrides	15 28	167 7
	50 58	1 51 E	Niphon	34 36 N	
Constantinople	41 1	28 59	Naples	40 50	14 16
Canton	23 7	113 14	Odessa	46 28	30 44
	59 59	29 47	Pekin	39 54	116 28
Copenhagen	55 41	12 34	Palermo	38 8	18 22
Cape of G. Hope.	33 56 s	18 29	Paris	48 50	2 20
Calcutta	22 34 n	88 20 E	Rome	41 54	12 27
Corinth	37 54	22 52	Rotterdam	51 54	4 29
Cairo	30 3	31 18	Smyrna	38 26	27 7
Ceylon	9 49	80 23	Singapore	1 17	108 50
Dublin	53 23	6 20w	Siam	14 55	100
Dover	51 8	1 19 E	Sierra Leone	8 30	13 18w
	55 57	3 12w	St. Helena	15 55 B	5 45
Feejee Group		178 53E	Suez	29 59 N	32 34 E
Florence	43 46 N	11 16	Steckholm	59 21	18 6
GREENWICH	51 29		St. Petersburgh .	59 56	30 19
Geneva	46 12	6 9	Toulon	43 07	5 22
Glasgow	55 52	4 16w	Tripoli	34 54	18 11
Gibraltar	36 7	5 22	Tunis	36 47	10 6
Genoa	44 24	8 53 E	Tangier	35 47	5 54
Honolulu		157 52w	Venice	45 50	12 26
Hamburg	53 33	9 58 E	Vienna	48 13	16 23
Havre	49 29	6	Warsaw	52 13	21 2
Jerusalem	31 48 N		Zanzibar	6 28 s	39 83
Liverpool	53 25	3		j	1

# MEASURE OF CIRCLES; OR ANGLES.

The UNIT is the degree, which is 1-300 part of the circumference of any circle.

60 Seconds (") = 1 Minute. '
60 Minutes = 1 Degree. °
30 Degrees = 1 Sign. S
13 Signs, or 360° = 1 Circle. C

G 2

And Statute Limitations in the different States.

In some States there are exceptions, and any of the data are liable to change by the action of the State Legislatures.

The English legal rate is 5 per cent.

	e of	Rates all'wd by Contract.	D	Statu	te Limi	tat'n.
States and Territo-	ra Se	122	Penalties for Usury.	Ореп		Judg
ries.	21 16	80	Forfeiture of		Note.	-
	Legal rate o Interest.	Rat by	2011018410 01	Acc'ts Yrs.	Yrs	ment. Yrs.
Alabama,	8	8	Entire interest	- 3	6	20
Alaska,		١. ١				į
Arizona,	10	Any.				
Arkansas, California,	8	Any.		3226633353	1	10 10
Colorado,	10	Any.		5	4	1 15
Connecticut	6	Tuy.	Entire interest	1 ã l	6	17
Dakota,	7-10			Ğ	15	6
Delaware,	6	6	Principal	Š	6	20
Dist. of Columbia.	6	10	Entire interest	3	8	12
Florida,	8	Any.	_	5	5	ŀ
Georgia,	7	10	Excess	8	3	12
Idaho,	10	Any.		1 .	_	
Illinois,	6	10	Entire interest	5.	6	16
Indiana	6	10	Excess	. 6	20	20
Indian Territory,	6	۱ ۸۸	Entire interest		10	20
Iowa, Kansas,	7	10	Entire interest	3	5	10
Kentucky,	6	10		5 3 2 3 6 3 6 6 6 3	7	14
Louisiana	5	8	Entire interest	3	5	10
Maine,		Any.		6	6	2ŏ
Maryland,	Ğ	6	Excess	8	3	12
Massach usetts	6	Any.		6	6	20
Michigan,	7	10	Excess	6	6	20
Minnesota,	7	12		6	6	10
Mississippi,	6	10	==	3	6	20
Missouri,	6	. 10	Entire interest	5	10	20
Montana,	10	Any.	Entire interest	4	5	5
Nebraska, Nevada,	10	10 Any.	Entire interest	4	3	,
New Hampshire,	6	Ally.	Thrice excess	6	6	20
New Jersey,	6	6	Entire interest	6	16	2ŏ
New Mexico,		ľ		"		""
New York,	ĕ	6	Excess	6	6	20
North Carolina	6	8	Entire interest	6 6 6	8	10
Ohio	6	8	Excess .	6	15	20
Oregon	10	12		6	6	10
Pennsylvania	6	Any.		6	6	20
Rhode Island	6	Any.		6	6	20
South Carolina,	7	Any.	T-acce	6	6	20 10
Tennessee,	8	10	Excess	2	6	10
Texas, Utah	10	Any. Any.		*	4	10
Vermont,	6	Any.	Excess	6	6	6
Virginia,		12	10	5	5	10
Washington	10	Auy.			_	1
West Virginia,	Ğ	6	Excess	5	5	10
Wisconsin,	7	10	Entire interest	10	6	10
Wyoming,	10	Ι.	_	1		l

Paper is bought at wholesale by the bale, bundle and ream; and at retail by the ream, quire and sheet.

2 Reams - 1 Bundle, 24 Sheets - 1 Quire, 20 Quires - 1 Ream. 5 Bundles - 1 Bale.

The names generally define the sizes. Writing and Drawing Papers differ in size from Printing Papers of the same name.

English sizes differ from American.

#### SIZE OF FOLDED PAPERS, IN INCHES.

Letter, 10x16
Commercial Letter, 11x17
Packet Post, 11½ x 18
Extra Packet Post, 111/2x181/2
Foolscap, 123/4×16

FLAT CAP PAPERS.						
Law Blank,	13x16	Medium, 18x23				
Flat Cap,	14x17	Royal, 19x24				
Crown,	15x19	Super Royal, 20x28				
Demy,	16x21	Imperial, 22x30				
Folio Post,	17x22	Elephant, 22½ x27¾				
Check Folio,	17x24	Columbia, 23x33¼				
Double Cap,	17 x 28	Atlas, 26x33				
Extra Size Folio,	19x23	Double Elephant, 26x40				

#### SIZE OF PRINTING PAPERS.

Medium, 19x24	Double Medium, 24x38
Royal, 20x25	Double Royal 26x40
Super Royal, 22x28	Double Super Royal, 28x42
Imperial, 22x32	" " 29x43
Medium-and-half, 24x30	Broad Twelves, 23x41
Small Double Medium 24x36	Double Imperial 82x46

#### Books.

The terms folio, quarto, octavo, duodecimo, etc., indicate the number of leaves into which a sheet of paper is folded.

Wh is f	en a sh olded 11	eet } The Book { nto } is called { Pa	1 sheet of per makes	When a sheet is folded into	The Book ( is called (	1 . sheet of Paper makes
2 1	leaves	. A Folio.	4 pages	16 leaves.	A 16mo.	32 pages
4	46	A Quarto or 4to.	8 "	18 "	An 18mo.	36 **
8	44	An Octavo or 8vo.	. 16 "	24 "	A 24mo.	43 "
12	" A	Duodecimo or 12mo	. 24 **	32 "	A 82mo.	64 "

Clerks and Copyists are often paid by the Folio for making copies of legal papers, records and documents.

72 words make 1 folio or sheet of Common Law.

90 " " " " " Chancery.

A Folio varies in different States and Countries but usually contains from 75 to 100 words.

GOLD COINS—their weight, fineness, and value in British and United States money, based on U. S. Mint assays, computed by C. FRUSHER HOWARD.

Country.	Denomination.	We	ight.	Fineness.		Value.	
		Grains.	Ounces.	1000ths	Carats.	£ s. d.	Ŭ. S. \$
Austria,	Union Crown,	171.36	0.357	900.	21.60	1,, 7,, 31/2	6.6419
Belgium,	25 France,	121.92	0.254	899.	21.57	19,, 41/2	4.7203
Bolivia,	Doubloon,	416.16	0.867	870.	20.88	3,, 4,, 1	15.5925
Brazil,	20 Milries,	276.00	0.575	917.5	22.02	2,, 4,, 10	10.9057
Chili,	Doubloon,	416.16	0.867	870.	20.88	3,, 4,, 1	15.5925
Denmark,	10 Thaler,	214.96	0.427	895.	21.48	1,,12,, 51/2	7.9000
England,	Bovereign,	123.27	0.2568	916.6	22.00	1,, 0,, 0	4.8665
France,	20 France,	99.60	0.2075	899.	21.57	15,,101/4	3.8562
Germany,	20 Marks,	122.90	0.256	900.	21.60	19,, 61/2	4.7627
Greece,	20 Drachms,	88.80	0.185	900.	21.60	14,, 13/4	3.4419
India,	Mohur,	179.52	0.374	916.	22.00	1,, 9,, 1	7.0818
Italy,	20 Lire,	99.36	0.207	898.	21.55	15,, 91/4	3.8426
Japan,	5 Yen,	128.30	0.267	900.	21.60	1,, 0,, 5	4.9674
Mexico,	Doubloon,	416.16	0.8675	870.5	20.89	3,, 4,, 11/2	15.6105
" ,	20 Pesos,	518.88	1.081	873.	20.95	4,, 0,, 2	19.5083
Netherl'ds.	10 Guilders,	103.72	0.216	899.	21.57	16,, 5	3.9956
Peru,	Doubloon,	416.16	0.867	868.	20.83	3,, 3,,111/4	15.5567
"	20 Soles,	496.80	1.035	898.	21.55	3,,18,,111/2	
Portugal,	Gold Crown,	147.84	0.308	912.	21.88	1, 3,,101/2	5.8066
Rome,	2½ Scudi,	67.20	0.140	900.	21.60	10,, 8	2.6047
Russia,	5 Roubles,	100.80	0.210	916.	22.00	16,, 4	3.9764
Spain,	100 Reales,	128.64	0.268	896.	21.50	1,, 0,, 5	4.9639
Sweden,	Ducat,	53.28	0.111	975.	23.40	9,, 2	2.2372
Turkey,	100 Piasters,	110.88	0.231	915.	21.96	17,,111/2	4.3693
United )	20 Dollars,	516.00	1.075	900.	21.60	4,, 2,, 21/2	20.0000
States.	One Dollar.	25.80	.05375	900.	21.60	.2054888	1.0000

The Gold Talent of Scripture—£5464, 5,8-\$26592.809.

" Silver " —£ 341,,10,,4-\$ 1662.025.

Exactly the existing ratio between U.S. Gold and Silver Coins--16 to 1.

Table of various Silver Coins, showing their weight, fineness and quota of pure silver, computed from U. S. Mint assays, by C. FRUSHER HOWARD.

Country.	Denomination.	Fine-	₩ei	Weight.		Pure Silver.		
		ness.	Ounces.	Grains.	Grains,	Cunces.		
Austria,	New Florin,	.900	0.397	190.56	171.504	.357300		
. "	" Dollar,	.900	0.596	286.08	257.472	.536400		
Belgium,	5 Frances,	.897	0.803	385.44	345.739	.720291		
Bolivia,	New Dollar,	.9035	0.643	308.64	278.856	.580950		
Brazil,	Double Milries.	.9185	0.820	393.60	361.521	.753170		
Canada,	20 Cents,	.925	0.150	72.00	66.666	.138750		
Cen. America.	Dollar,	.850	0.866	415.68	353.328	.736100		
Chili,	New Dollar,	.9005	0.801	384.48	346.224	.721300		
China, Hong K.	English Dollar,	.901	0.866	415.68	374.527	.780266		
Denmark,	Two Rigsdaler,	.877	0.927	444.96	390.230	.812979		
England,	New Shilling,	.9245	0.1825	87.60	80.986	.168721		
France,	5 Franc,	.900	0.800	384.00	345.6	.720000		
Germany,	Mark,	.900	0.1785	85.70	77.13	.160650		
Greece,	5 Drachms,	.900	0.719	345.12	310.608	.647100		
Rast Indies,	Rupee,	.916	0.374	179.52	164.44	.342584		
Japan,	New Dollar,	.900	0.875	420.00	378.000	.787500		
Mexico,	""	.903	0.8675	416.40	376.009	.783352		
Naples,	Scudo,	.830	0.844	405.12	336.249	.700520		
Holland,	21 Guilders,	.944	0.804	385.92	364.308	.758976		
Norway,	Specie Daler,	.877	0.927	444.96	390.229	.812979		
Peru,	Dollar 1858,	.909	0.766	367.68	334.221	.696294		
Rome,	Scudo,	.900	0.864	414.72	373.248	.777600		
Russia, 🕳	Rouble,	.875	0.667	320.16	280.140	.583625		
Spain,	New Pistareen,	.899	0.166	79.68	71.632	.149234		
Sweden,	Rix Daler,	.750	1.092	524.16	393.120	.819000		
Turkey,	20 Piasters,	.830	0.770	369.60	306.765	.639100		
Tuscany,	Florin,	.925	0.220	105.60	97.680	.203500		
United States.	Dollar	.900	0.8594	412.50	371.25	.773437		
"	Trade "	.900	0.875	420.00	378.00	.787500		

Table showing the value in U.S. Gold Coin of an ounce of silver (480 gr.), and a Standard dollar (412½ gr.), each 9-10 fine, at London quotations for Silver bullion .925 fine, calculated at the par of exchange, \$4.8665, to the pound sterling, by C. Frusher Howard.

Londo Pence.	n Price.	Value of Ounce. 480 Grn's.	Value of Stand. \$ 4121 G.	_		Value of Ounce. 480 Grs.	Value of Stand. \$ 4124 Grs.
	12	\$	8 1		1 0		
50	.2083	0.986	0.847	55 <del>1</del>	.2302	1.089	.936
50 <del>1</del>	.2094	0.991	0.851	551	.2312	1.094	.940
50 <u>1</u>	.2104	0.996	0.855	55₫	.2323	1.099	.945
50 <del>4</del>	.2115	1.001	0.860	56	.2333	1.104	.949
51	.2125	1.006	0.864	56 <del>1</del>	.2343	1.109	.953
51 <u>1</u>	.2135	1.011	0.868	<b>5</b> 6⅓	.2354	1.114	.958
51	.2146	1.016	0.873	56≩	.2365	1.119	.962
514	.2156	1.020	0.877	57	.2375	1,124	.967
52	.2167	1.025	0.881	571	.2385	1.129	.971
52 <del>1</del>	.2177	1.030	0.886	57 1	.2396	1.134	.975
521	.2187	1.085	0.890	57#	.2406	1.139	.979
525	.2198	1.040	0.894	58	.2417	1.144	.984
53	.2208	1.045	0.898	581	.2427	1.149	.988
531	.2219	1.050	0.903	581	.2437	1.154	.992
581	.2229	1.055	0.907	58	.2448	2.159	.996
584	.2239	1.060	0.911	59	.2458	1.164	1.000
`54	.2250	1.065	0.915	59 <del>1</del>	.2469	1.169	1.004
541	.2260	1.070	0.920	593	.2479	1.178	1.009
54 <u>1</u>	.2271	1.075	0.924	59#	.2489	1.178	1.018
542	.2281	1.080	0.928	60	.2500	1.183	1.017
55	.2292	1.085	0.932				

The Trade dollar is worth two-tenths of a cent. more than the Mexican. 1\frac{1}{2} cents more than the U.S. Standard Dollar.

The value in U. S. Gold Coin of 1 ounce of silver, .9 fine  $= .01972931 \times$  the given number of pence per ounce in the bondon market.

The value of the U.S. Standard silver dollar  $= .01695 \times$  the market price in pence.

The Standard weight and fineness, respectively of the Indian Rupee is 180 grains, and 916.6 millesimal fineness.

The value of the Rupee in pence  $= .37162 \times \text{the gives}$  number of pence per ounce.

Francs 
$$\times \frac{4}{100} = \pounds$$
 sterling;  $\pounds \times \frac{100}{4} =$  Francs.

THE METRIC SYSTEM of Weights and Measures is based upon the decimal scale; its paramount simplicity insures its early adoption by all civilised nations.

The Meter is the base of the system, and = 39.37079 in.

The Are (air) is the unit of surface, the Store (stair) is the unit of volume, the Litre (leeter) is the unit of capacity, the Gram is the unit of weight; these constitute the primary units of the system.

The Multiple Units, or higher denominations, are named by prefixing to the name of the primary units the *Greek* numerals *Deka* (10), *Hecto* (100), *Kilo* (1,000), and *Myra* (10,000).

The submultiple units, or lower denominations, are named by prefixing to the names of the lower denominations the *Latin* numerals,  $\mathcal{E}$  Deci  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ , Centi  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ , Milli  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ .

The Name of a unit indicates whether it is greater or less than the standard units, and

also how many times.

MEASURES OF EXTENSION.

The Meter is the unit of the length, and = 39,37079 inches, and is used in measuring cloths and short distances.

The Kilometer is commonly used for measuring long distances, and is about five-eights of an English mile.

or an ingusi	2   "	1	ł		
	TABLE.		<b>-</b>  -	_	l
Metric Denominations	1 Millimeter	English or U.S. values.	-		١
10 Millimeters,	mm. =1 Centimeter	= .3937079 ,,	O.0		l
10 Centimeters,	cm. =1 Decimeter	= 3.937079 ,,	_	_	l
10 Decimeters,	dm. = 1 Meter	=39.37079 ,,	_	١.	١
10 Meters,	M. =1 Dekameter	=32.808992 ft.	-	1 2	l
10 Decameters,	Dm. = 1 Hectometer	=19.927817 rd.	<b>i</b> -	Inches	l
10 Hectometers,	Hm. =1 Kilometer	= .6213824  mi		_	1
10 Kilometers,	Km.=1 Myrameter	= 6.213824 ,,			

The Are is the unit of land measure, and is a square whose side is 10 meters, equal to a square dekameter, or 119.6 sq. yards.

#### TABLE.

```
1 Centiare, ca. = (1 Sq. Meter) = 1.196034 sq. yd.

100 Centaires, ca. = 1 Are = 119.6034 sq. yd.

100 Ares, A. = 1 Hectare (Ha.) = 2.47114 acres.
```

The Square Meter is the unit for measuring ordinary surfaces; as flooring, ceilings, etc.

#### TABLE.

```
100 Sq. Millimeter, sq. mm.=1 Sq. Centimeter = .155+ sq. in.
100 Sq. Centimeters, sq. cm.=1 Sq. Decimeter, =15.5+ sq. in.
100 Sq. Decimeters, sq. dm.=1 Sq. Meter (Sq. M.)= 1.196+ sq. yd.
```

The Stere is the unit of wood or solid measure, and is equal to a cubic meter, or .2759 cord.

#### TABLE.

```
1 Dicistere = 3.531+ cu. ft.

10 Dicisteres, dst. =1 Stere = 35.316+ cu. ft.

10 Steres, St. =1 Dekastere (DSL) =13.079+ cu. yd.
```

The Cubic Meter is the unit for measuring ordinary solids; as excavations, embankments, etc.

### TABLE.

```
      1000 Cu. Millimeters,
      cu. mm.=1 Cu. Centimeter=
      .061+ cu. in.

      1000 Cu. Centimeters,
      cu. cm. =1 Cu. Decimeter = 61.026+ cu. in.

      1000 Cu. Decimeters,
      cu. dm. =1 Cu. Meter = 35.316+ cu. ft.
```

### MEASURES OF CAPACITY.

The *Liter* is the *unit of capacity*, both of Liquid and Dry Measures, and is a vessel whose volume is equal to a cube whose edge is one-tenth of a meter, equal to 1.05673 Liquid Measure. and .9081 quart Dry Measure.

#### TABLE.

```
10 Milliliters, ml = 1 Centiliter. 10 Dekaliters, Dl. = 1 Hectoliter. 10 Centiliters, cl. = 1 Deciliter. 10 Hectoliters, Hl. = 1 Kiloliters, Hl. = 1 Kiloliters, Hl. = 1 Myrialiter. 10 Liters, Ll. = 1 Dekaliter. (Ml.)
```

The Hectoliter is the unit in measuring liquids, grain, fruit and roots in large quantities

#### EQUIVALENTS IN U. S. AND IMPERIAL MEASURES.

Metric Denominat'ns.	Cubic Measure.	Dry Measure.	Wine Measure.	Imp. Measure.
1 Myrialiter=10	Cubic Meter	s=283.72‡bu.	=2641.4‡gal.=	2200.96711gal.
1 Kiloliter = 1	Cubic Meter	=28.372‡bu.	=264.17 gal.=	220.09671gal,
1 Hectoliter= $\frac{1}{10}$	Cubic Meter	=2.8372‡bu.	=26.417 gal.=	22.00967gal.
1 Dekaliter =10	Cu.Decimet':	r=9.08 qts.	=2.6417 gal.=	2.20096gal.
			=1.0567 qt. =	7.0430 gills
1 Deciliter $=\frac{1}{10}$	Cu.Decimet'ı	=6.1022 c.in	=.845 gill =	.7043 gill.
1 Centiliter=10	Cu. C'ntim't'ı	=.6102cu.in	=.338 fl'd oz.=	.0704 gill.
1 Milliliter = 1	Cu. C'ntim't'ı	=.061 cu. in:	=.27 fl'd dr. =	.0070 gill.

#### MEASURES OF WEIGHT.

The Gram is the unit of weight, and equal to the weight of a cube of distilled water, the edge of which is one hundredth of a meter, equal to 15.432 Troy grains.

The *Kilogram*, or *Kilo*, is the *unit* of common weight in trade, and is a trifle less than  $2\frac{1}{k}$  lbs. Avoirdupois.

The Tonneau is used for weighing very heavy articles, and is about 204 lbs. more than a common ton.

#### TABLE.

```
10 Milligrams,
                                            .15432+ oz. Troy.
                 mg.
                       =1 Centigram
 10 Centigrams
                       =1 Decigram
                                           1.54324+ "
                 cg.
 10 Decigrams.
                 dø.
                       =1 Gram
                                          15.43248+ "
 10 GRAMS.
                 G.
                       =1 Dekagram
                                            .85273+ oz. Avoir.
 10 Dekagrams,
                 Dø,
                       =1 Hectogram
                                           8.52739+ "
                       =1 (Kilogram, )
                 Hg.
 10 Hectograms.
                                           2.20462+ lb.
                           or Kilo,
                 Kø.
 10 Kilograms.
                       =1 Myriagram
                                          22.04621+ "
 10 Myriagrams, or Mg. =1 Quintal
                                       = 220.46212+ "
100 Kilograms
                      10 Quintals, or
1000 KILOS.
```

#### Comparison of the Common and Metric Systems.

```
1 Inch, =
                2.54 Centimeters
                                             1 Cu. in.=16.89 Cu. Centim't'rs
1 Foot, =
               80.48 Centimeters
                                                " ft.,=28320 "
                                               " yd.,=.7646"
1 Yard, =
                      9144 Meters
                                                                   Meters.
                     5.029 Meters
1 Rod.
                                             1 Cord,
                                                           =
                                                                   8.625 Steres
1 Mile,
               1.6093 Kilometers
                                             1 Fl. ounce, = .2.958 Centiliters
1 Sq. in. =6.4528 Sq. Centim't'rs

1 Sq. ft., = 929 Sq. Centimeters

1 'yard, = 8.361 Sq. Meters
                                             1 Gallon,
                                                           =
                                                                   3.786 Liters
                                                           = .8524 Hectoliter
                                             1 Bushel,
                                                           = 64.8 Milligrams
                                             1 Troy gr.
1 " lb.
                   25.29 Centairs
                                                                      .873 Kilo
      rod
                                             1 Av. 1b.
                       40.47 Ares.
                                                           =
                                                                     .4538
1 Sq. mile, =
                     269 Hectares
                                             1 Ton.
                                                                 .907 Tonnean
```

#### MARKING GOODS.

Removing the decimal point one place to the left on the cost of a dozen articles, gives the cost of one article with 20 per cent. added. We remove the point one place to the left, because 12 tens make 120. Hence, to find the selling price, to gain the required percentage of profit, we have the following general rule:

RULE.—Remove the decimal point one place to the left on the cost per dozen, to gain 20 per cent.; increase or diminish to find the percentage, as per following table:

TABLE FOR MARKING ALL GOODS BOUGHT BY THE DOZEN.

To make 20% remove the point 1 place to left.

	,-		<u>.</u>	<u>.</u>				
66	25%	66 -	"	"	"	Add	124	itself.
66	26%	"	"	"	"	"	20	"
66	28%	46	"	"	46	"	1 7 8	66
"	30%	66	"	"	66	"	1 1 2	66
"	32%	"	"	"	66	66	1 10	۲.
66	331%	"	"	"	66	"	1 9	46
66	35%	"	"	"	66	"	18	"
"	$37\frac{1}{2}\%$	66	66	"	"	"	17	66
46	40%	"	66	"	66	"	7 1 8	"
"	44%	66	66	66	"	ii	5 5	"
66	50%	"	"	66	6.	"	5 1	"
"	60%	"	66	"	"	66	18	66
"	80%	66	66	66.	66	"	8 1 2	66
66	$12\frac{1}{2}\%$	"	"	66	66 an	btrac		66
"	163%	"	66	66	"	66		ci
"	184%	66	"	"	"	46	36	66

See page 62.

## POPULATION OF CITIES.

Table showing the Population of the principal Cities and Towns of the United States as shown by Census of 1880.

New York	.209.561	l
New York	847,452	
Brooklyn, N. Y	556,930	k .
Obleans III		1
Chicago, Ill	503,298	i
St. Louis, Mo	375,000	
Boston, Mass	863,938	1
Baltimore, Md	830,000	i
Cincinnati, O	255,809	Ι.
San Francisco, Cal	233,066	1
New Orleans Le	215,239	l
New Orleans, La Washington, D. C		l
wasnington, D. C	161,111	1
Cleveland, O	159,504	1
Pittsburgh, Ps	153,883	1
Buffalo, N. Y	149,500	j .
Buffalo, N. Y Newark, N. J Louisville, Ky	137,162	4
Lonisville Kv	126,566	
Jersey City, N. J	122,207	l
Wilmanhaa Wia	115 710	l
Milwaukee, Wis	115,712	1
Detroit, Mich	115,007	1
Detroit, Mich	104,760	
Albany, N. Y	87,584	l
Rochester, N. Y	78,087	l
Allegheny City, Pa	78,472	
Indianapolis, Ind	76,200	l
Richmond, Va	63,243	l
Now Marian Ot		1
New Haven, Ct	62,861	l
Lowell, Mass	59,340	
Worcester, Mass Troy, N. Y	58,040	1
Troy, N. Y	57,000	
Kansas City, Mo	56,904	l
Tolede, O	<b>5</b> 3,635	1
Tolede, O	52,860	l
	52,158	1
Columbus, O.	51,650	
Columbus, O Paterson, N. J. Denver, Col.	50,950	
Denver Col	85,718	1
Charleston C C	40.007	
Charleston, S. C	49,027	
Fall River, Mass Minneapolis, Minn	48,909	1
Minneapolis, Minn	48,323	
Scranton, Pa	45,925	1
Atlanta, Ga	45,000	
Nashville. Tenn	43,543	1
Reading, Pa Hartford, Conn	43,230	i
Hartford, Conn.	42,560	1
Wilmington, Del	42,000	1
St. Paul, Minn	41,639	1
Lawrence Mess	90,000	1
Lawrence, Mass	39,068	I
Dayton, Ohio	38,751	l
Lynn, Mass	38,376	l
Memphis, Tenn	35,000	l
St. Joseph, Mo Oakland, Cal	35,000	l
Oakland, Cal	34,700	l
Utica, N. Y	33,927	1

shown by Census of	1880.
Portland, Me	88,829
Dallas, Tex	83,486
Dallas, Tex	88,149
Savannah, Ga	82,916
Manchester, N. H	82,458
Grand Rapids, Mich	82.087
Peoria, Ill	81,789
Peoria, Ilf	81,789 81,295
Wheeling, W. Va	81,186
Harrisburg, Pa. Omaha, Neb. Trenton, N. J. Evansville, Ind.	80,728
Omaha, Neb	80,642
Trenton, N. J	29,938
Evansville, Ind	29,366
Erie, Pa	28,346
Quincy, Ill	27,428
Salem, Mass	27,428 27,847
Salem, Mass Terre Haute, Ind	26,522
Lancaster, Pa Leadville, Colo	25,846
Leadville, Colo	15,000
Sacramento, Cal Des Moines, Iowa Galveston, Texas	25,000
Des Moines, Iowa	22,900
Galveston, Texas	22,308
Dubuque, Iowa Holyoke, Mass	22,276
Holyoke, Mass	24,926
Davenport, Iowa	21,812
Portland, Oregon	21,000
Springfield, Ohio Elmira, N. Y. San Antonio, Texas	20,727
Elmira, N. Y	20,646
San Antonio, Texas	20,594
Springfield, Ill	19,500
Leavenworth, Ks	18,800
Burlington, Iowa	19,000
Council Bluffs, Iowa.	18,400
Bloomington, Ill	17,700
Houston, Texas Akron, O Jackson, Mich	16,632
Tackson Wich	16,462 16,121
Binghamton	16,000
Binghamton	15,753
Oshkosh, Wis Newport, R. I	15,698
Topeka, Kan	15,433
Atchison, Kan	15,130
Little Rock, Ark	15,000
La Crosse Wis	14,470
La Crosse, Wis Knoxville, Tenn	13,928
Rock Island, Ill	13.699
Lincoln, Neb	13,697
San Jose Cal	12,615
San Jose, Cal Cedar Rapids, Ia	12,500
Keokuk, Ia	12,176
Keokuk, Ia Kalamazoo, Mich	12,078
Pueblo, Colo	7,000

### MÉTHODE DE CALCUL POUR L'ESPACE DE TRENTE SIÈCLES.

REGLE.—Des deux derniers chiffres de l'an, rejetez tous les sept, tout en retenant le restant; divisez les deux derniers chiffres de l'an par quatre, retenant le quotient, sans tenir compte du restant, s'il y en a;—puis prenez le jour du mois, ensuite le chiffre donné pour le mois, et finalement celui pour le siècle. Ayez toujours soin de rejeter les sept où il y en a.

Le chiffre 1 (un) restant représente le premier; 2, le second; &c., et O (zéro) le dernier jour de la

semaine.

#### TABLE DES CHIFFRES POUR LES MOIS.

1, Septembre et Déc. 2, Artil et Juillet. 4, Mai. 5, Août. 6, Fév., Mars, Nov. 0, Juin. Nota,—Dans l'année bissextile le chiffre pour Janvier est 2, et celui pour Février 5.

### TABLE DES CHIFFRES POUR LES SIÈCLES.

1,	est	le	chiffre	pour	les	2ème, 9ème, et 16ème, siècles. [siècles.
2.	46	44	44	- "	"	1er, 8ème, 15ème, 18ème, 22ème, 26ème, 80ème,
8.	"	"	"	66	66	7ème, 14ème siècles. [siècles,
ď.	"	"	44			6ême, 13ême, 17ême, 21ême, 25ême, 29ême,
5,	"	"	"			5ème, 13ème, 20ème, 24ème, 28ème, siècles.
6.	"	"	**	**		4ème, 11ème siècles,
0,	"	"	•	44		3ème, 10ème, 19ème, 23ème, 27ème, siècles.

EXEMPLE.—Quel fut le jour de la semaine au 31 Août, 1873? Réponse, Dimanche.

### Procédé—

Deux derniers chiffres de l'an, 73-70=3Quotient de 73 divisé par quatre, 18+3-21=0Jour du mois, 31-28=3Chiffre pour le mois, 5+3-7=1

Après avoir rejeté tous les sept il reste le chiffre 1; ce fut donc, le premier jour de la semaine, Dimanche.

N.B.—Les siècles pairs non-divisibles par le chiffre 400 ne sont par

des années bissextiles.

### Mehtode zu fagen den Zag in der Woche nach jedem Datum bon Chrifti Geburt drei. taufeud Jahr.

Methode.—Streich die Sieben aus von die beiben letten Rummern auf das Jahr, ber Minuent von den beiben letten Nummern im Jahre, bivibirt bei viergebrauche nicht den Reft-ben Datum auf ben Monat, und die Figur auf das Jahr. Was überbleibt ift der Laa in der Woche, der erste Sonntag, der zweite Montag u. f. w.

Die Kiguren vor bie Monate. 1 vor Sept. u. Decbr. 8 vor Jan. u. Oct. 6 vor August. 2 vor April und Juli. 4 vor Mat. 6 vor Feb., A 0 vor Juni. 6 vor Feb., Marg, Rov.

Der Datum im Januar und Februar ift ein weniger im Schaltjahr. Datum auf bie Jahre.

```
1, ift bie Figur vor bas Ste, 9te unb 16te Jabrhunbert.
                                      " 1te, 8te, 15te, 18te, 22te, 26te unb 30te Jahrhunbert. , 7te, 14te Jahrhunbert.
8, ,,
                              ,,
                                          6te, 13te, 17te, Alte, Aste, 29te Jahrhunbert.
5te, 12te, 20te, 24te, und 28te Jahrhunbert.
4te nnd 11 Jahrhunbert.
8te, 10te, 19te, 28te und 87te Jahrhunbert.
4, ,,
                              "
                                      "
```

Erempel.—Welcher Tag in der Woche war der 31. August, 1873? Antwort, Sonntag.

```
Die letten beiben Figuren im Jahre, 73 - 70 = 3
Minuent auf bo. - bei vier,
                                 18 + 3 - 21 = 0
Datum im Monat.
                                 31 - 28 = 3
                                  5 + 3 - 7 = 1
Figur auf den Monat,
```

Der Rest I zeigt Euch ben ersten Tag in der Woche, welcher ist Sonntag.

To find the figure for any Century from the 1st to the 1stn, multiply the figures expressing the hundreds in the given year by 6, add 2, and divide by 7; the remainder is the figure for the Century.

To find the figure for the 17th and succeeding Centuries, subtract 16 from the number of hundreds in the given year, multiply by 5%, to the product—less the fraction—add 4, and divide by 7; the remainder is the figure for the Century. remainder is the figure for the Century.

Nors—Between the Julian and the Augustan Calendars there was a difference of ten days in 1583 and of eleven days in 1753. At the present time the difference is twelve days. The latter came into use in Catholic countries in 1583 and in England in 1758.

## Howard's California Calendar for Thirty Centuries.

RULE.—Cast all the sevens out of the last two figures of the year; add the remainder to the quotient\* of the last two figures of the year, divided by four; take this sum with the day of the month, the figure for the month, and the figure for the century, dropping all the sevens as they occur, one remainder will be the the first day of the week, Sunday; 2, the second, &c.; 0, last day of the week, Saturday.

\* Disregard the fraction, if any, in the quotient.

#### TABLE OF FIGURES FOR THE MONTHS.

1, Sept. and Dec. 3, Jan. and Oct. 5, August. 0, June. 2, April and July. 4, May. 6, Feb., March, Nov.

Note.—The figure for January is 2, and February 5 in leap year.

### TABLE OF FIGURES FOR THE CENTURIES.\*

```
1, is the figure for the 2d, 9th, and 16th centuries.
2, """ 1st, 8th, 15th, 18th, 22d, 26th, 30th centuries.
3, """ 1th, 14th centuries.
4, """ 6th, 18th, 17th, 21st, 28th, 29th centuries.
5, """ 5th, 12th, 20th, 24th, 28 centuries.
6, """ 4th, 11th centuries.
0, """ 3d, 10th, 19th, 23th, 27th centuries.
```

Example.—What day of the week was the 31st August, 1873? Sunday, Ans.

#### Process—

Last two figures of the year, 73 - 70 = 3Quotient of  $73 \div$  by four, 18 + 3 - 21 = 0Day of month, 31 - 28 = 3Figure for the month, 5 + 3 - 7 = 1

\*Pay no attention to the figure for this, the 19th century, as it is 0; for the last century, add 2; for the coming century, add 5,

After casting out the sevens the remainder is 1:

hence it was on the first day of the week, Sunday.

N. B.—The even centuries not divisable by 400 are not leap years.

### HOWARD'S

### Tables of Standard Weights and Measures.

A Standard Measure is a fixed unit established by law, by which quantity, as extent, dimension, capacity or value is measured.

The English Standard units are the YARD, the IMPERIAL GALLON, the TROY POUND, and the GOLD SOVEREIGN.

The U. S. Standard units are the YARD, the GALLON, the BUSHEL, the TROY POUND, and the GOLD DOLLAR.

The Standard unit of weight must be of definite dimensions, and of definite gravity, of some substance, a certain volume of which, under certain conditions, will always have a certain weight.

One cubic inch of pure water weighed in vacuo, thermometer 62° Fahrenheit, Barometer 30°= 252.458 grains.

5760 grains = 1 Troy pound.

In the Treasury at Washington is a brass scale which, at a temperature of 62° Fahrenheit, is 82 inches long; all U.S. weights and measures are referred to this unit.

### LONG MEASURE.

### Surveyors'

IN.	FT.	YD.	RD.	PUR			Long Measure.					RE.
_					_		IN.	L.	RD.	C.		
12	1				1	Foot.		-	-	-	_	-
36	3	1			1	Yard.	7.92	1			1	Link.
198	161/2	51/4	.1		1	Rod.	198	25	1		1	Rod.
7920	660	220	40	. 1	1	Furling	793	100	4	.1	1	Ch'n.
63360	5280	1760	320	8	1	Mile.	63360	8000	320	80	1	Mile.

The Geographical Mile equals 1.15 Statute Miles,

### COMPARISON OF STANDARD MEASURES OF DISTANCES.

Country.	T. S. Mile.	Country.	U.S Mile,
Austria, 1 Mile,	= 4.98	Persia,1 Far	sang. = 4.17
China,1 Li,	= .35	Portugal,1 Mil	
East Indies, 1 Coss,	= 1.14	Prussia, 1 Me	
Egypt,1 Mili,	= 1.15	Russia, 1 Vc	
England, 1 Mile,	= 1.00	Spain, 1 Let	$gue_{\bullet} = 4.15$
France, 1 Kilome	et`r.= .62	Sweden, 1 Mil	
Japan,1 Ri,	=2.562	Switzerland, 1 Lie	ue, $= 2.98$
Mexico,1 Silio,	<b>—</b> 6.76	Turkey,1 Be	rri, = 1.04
			TT

#### For measuring Land, Boards, Painting, Paving, Plastering, etc.

sq. inch.	sq. FOOT.	sq. YARD.	sq. RD.	sq. R.	sQ. A.		
144	1					1	sq. FT.
1296	9	1				1	YARD.
39204	2721/4	301/4	1			1	ROD.
1568160	10890	1210	40	1		1	ROOD.
6272640	43560	4840	160	4	1	:1	ACRE.
4014489600	27878400	8097600	102400	2560	640	1	MILE.
	<u>'                                    </u>	1	·	·			1

In measuring Roofing, Paving, etc., 100 square feet - one square.

One thousand shingles, averaging 4 inches wide, and laid 5 inches to the weather, are estimated to be a square.

One mile square—1 section—640 acres. 36 square miles (6 miles square)—1 township.

The sections are all numbered 1 to 36, commencing at the northeast corner, thus:

6	5	4	8	2	NW   N
7	8	9	10	11	12
18	17	16*	15	14	13
19	20	21	22	23	24
80	29	28	27	26	25
31	82	83	84	85	36

The sections are all divided into quarters, which are named by the cardinal points, as in section 1. The quarters are divided in the same way. The description of a forty-acre lot would read: The south half of the west half of the south-west quarter of section 1 in township 24, north of range 7 west, or as the case might be; and sometimes will fall short, and semetimes overrun the number of acres it is supposed to contain.

\*Reserve for school purposes,

Gunter's Chain is a unit of measure, and is four Rods, or 66 feet long; it consists of 100 links. It is also common to use a chain, or measuring tape, 100 feet long, each foot divided into tenths.

In the Pacific Coast States and Territories the divisions of Land are frequently expressed by the old Mexican Measurements:

A fifty Vara lot is 1371/2 feet square.

1 Vara=33-36=11-12 of a yard.

Varas×11-12=yards,

Yards×12-11=Varas.

For measuring	r timber.	stone.	boxes.	nackages.	canacity	of rooms.	etc.

cu. in.	CU. FT.	CU. YD.	CD. FT	CD.	PCH.		
1728	1			:		1	Cubic Foot,
16656	27	1	<b></b>	. <b></b>		1	Cubic Yard.
27648	16	16-27	1			1	Cord Foot.
221184	128	4 20-27	8	1		1	Cord of Wood.
42768	24%	<b>.</b>			1	1	Perch of Stone.
69120	40	 			<b></b>	1	U.S.Ton,ShipCarge
	i	ı	1	1	1	l.	l.

One ton of square timber = 50 cubic feet.

The English shipping ton = 42 cu. ft. The Register ton = 100 cu. ft.

A cord of wood is a pile 4 ft. high, 4 ft. wide, and 8 ft. long.

A cord foot is one foot in length of such a pile.

A cubic vard of common earth is called a load.

In Board measure all boards are assumed to be 1 inch thick.

A board foot is 1 ft. long, 1 ft. wide and 1 in. thick, hence 12 board feet make 1 cubic foot.

Board feet are changed to cubic feet by dividing by 12.

Cubic feet are changed to Board feet by multiplying by 12.

Masonry is estimated by the CUBIC FOOT and FERCH; also by the SQUARE FOOT and SQUARE YARD.

SQUARE FOOT and SQUARE YARD.

CUBIC FEET×4-99=PERCHES.

Five courses of bricks in the height of a wall are called a foot,

In board and lumber measure, estimates are made on 1 inch in thickness; one-fourth the price is added for every 1/4 inch in thickness over one inch.

### MISCELLANEOUS WEIGHTS AND MEASURES.

12 Units, 1 Dozen.	8 Pigs, 1 Fother.
12 Dozen, 1 Gross.	2 Weys (328 lb) 1 Sack of Wool.
12 Gross, 1 Great Gross.	12 Sacks, (4368 lb.) 1 Last.
20 Things, 1 Score.	3 Inches, 1 Palm.
196 lbs 1 Barrel of Flour.	4 " 1 Hand.
200 "1 Bbl. Beef, Pork, Fish.	9 " 1 Span.
56 " 1 Firkin of Butter.	3 ft1 common pace.
14 " 1 Stone, Avoir.	6 " 1 Fathom.
28 " 1 Quarter, "	3 Miles, 1 League.
211/2 Stones, 1 Pig of Iron.	360 Degrees, 1 Circle.
	н 2

### 114 TROY WEIGHT.

### AVOIRDUPOIS WEIGHT.

For Gold, Silver, Jewels, etc.

For Groceries, Provisions, etc.

Gr.	Pwt.	0z.			. Gr.	0z.	Lb.		
24	1		1	Pennyweight	4371/4	1		1	Ounce
480	20	1	1	Ounce.	7000	16	1	1	Pound.
5760	240	12	1	Pound.	14000000	32000	2000	1	Топ.

The Standard unit is the Troy Pound.

The Long Ton = 2240 lbs. 1 cwt. = 112 lbs.
The Short Ton=2000 lbs. Long Tons×1.12=Short Tons.

To compare Troy weights with Avoirdupois, reduce both to grains. Pounds Avoirdupois × 100×7-48= ounces Troy.

Troy ounces ×.08 6.7= Pounds avoirdupois; that is, ounces multiplied by .06+1-7 of the product.

	POT	HEC	ARI	es' \	Weight.	Apothecaries' Measure.
GRS.	вс. Э	DR.	0 <b>z.</b> 3			60 Minims = 1 Fluid Drachm.
20 60 480 5760	1 8 24 288	1 8 96		1 1 1	SCRUPLE, DRAM. OUNCE, POUND.	8 Fl. Drms = 1 Fluid Ounce.  16 Fl. Ozs. = 1 Pint.  8 Pints = 1 Gallon.  Used in compounding liquid medicines.

The grain, ounce and pound are the same as Troy Weight.

Drugs are bought and sold in quantities by Avoirdupols Weight.

1 Teaspoon = 45 Drops. 1 Tablespoon = ½ Fluid Ounce.

### COMPARISON OF LIQUID MEASURES.

		40	
Country.	U. S. Gals.	Country.	U. S. Gale
England, 1 Galk	on, — 1.2	Switzerland, 1 Pot,	40
France, 1 Deka		Turkey,1 Almud	1, - 1.38
Prussia,1 Quar		Mexico,1 Fasco.	
Austria, 1 Maai		Brazil,1 Medid	
Sweden,,1 Kanı	na, — .69	Cuba 1 Arrob	
Denmark, 1 Kan	ie, — .51	South Spain, 1 Arroba	a. — 4.25

#### COMPARISON OF GRAIN MEASURES.

Country.	U. S. Bushels.	Country.	U. S. Bushels.
	Bushel, - 1.031	Germany,1	Schef 1.5 to 3
	Hectoliter=2.84	Persia,1	Artaba, - 1.85
	Scheffel, - 1.56		Kilo, - 1.03
Austria,1	Metze, — 1.75	Brazil,1	
	Chetverik— .74	Mexico,1	
Greece,1	Kailon, -2.837	Madras,1	Parah, -1.743

### COMPARATIVE TABLE OF POUNDS IN DIFFERENT COUNTRIES

Austria, 100 lbs 123.50 U. S	S. Nederland, 100 lbs 108.93 U. S.
Bavaria, "123.50 "	Portugal, "101.19 "
Belgium, "103.85 "	Prussia, "110,25 "
Bremen, "110,12 "	Russia, " 90.00 "
Berlin, "103.11 "	Spain, "101.44 "
Denmark, "110.00 "	St. Domingo, "107.93 "
Ger. Zoll. States, 110.25 "	Trieste, "123.60 "
Hamburg,110.04 "	•

### COMPARISON OF COMMERCIAL WEIGHTS.

Country.	Weight-	U. S. Lbe.	Country.	Weight	U. S. Lbs.
Austria	1 Pfund.	- 1.23	Mexico	1 Libra,	- 1.02
Arabia				1 Vis.	
Brazil,	1 Arrate	1,- 1.02	Persia	1 Rattel.	- 2.116
China,	1 Catty,	- 1.33		1 Funt,	
Denmark.	1 Pund.	<b>—</b> 1.10	Sweden.	1 Pund,	93
East Indie	s1 Seer.	- 2.06	Spain	1 Libra,	-1.016
Egypt,				1 "	
France,				1 Oka,	= 2.82
Germany,			Japan,		62

		Tro	y.	Apo	thecaries	Avoirdupois.			
1 Pound	=	5760 g	grains	=	5760	grain	s =	7000 gr	rains.
1 Ounce	=	480		=	480		=	437.5	**
		175 F	ound	3=	175	pound	ls=	144 po	unds.

### RAILROAD FREIGHT .- TABLE OF GROSS WEIGHTS.

When the actual weights are not known, the articles are billed as per the following table.

Ale and Beer, 320 lb. per bbl.	Lime, 200 lb. per bbl.
170	Malt, 38 " " bu.
100 14	Millet, 45 " "
Apples, dried, 24 " " bu .	Nails, 108 " " keg
" green, 50 " " "	Oil, 400 " " bbi.
" 150 " " bbl.	Peaches, dried, 33 " " bu.
Beef, 320 " " "	Pork, 320 " " bbl.
Bran, 20 " " bu.	Potatoes (com.) 150 " "
Brooms, 40 " doz.	Salt, Fine, 300 " " "
Cider, 850 " " bbl.	" Coarse, 350 " " "
Charcoal,22 " bu.	" in Sack, 200 " " "
Eggs, 200 " " bbl.	Turnips, 56 " " bu.
Fish, 300 " " "	Vinegar, 850 " " bbl.
Flour,200 " " "	Whiskey, 350 " " "
Highwines,850 " " "	One Ton Weight, 2000 lb.

CU.FT.	CU. IN.	,	CU.FT.	cu. in.	
.0167	28.875	4 Gills,'1 Pint.	11.229	19404	2 Tiecs1 Punsh'n.
.0334	57.75	2 Pints 1 Quart.	4.2109	7276.5	31½ Gals1 Bbl.
.13368	, 231	4 Qts., 1 Gallon.	8.421	14553	2 Bbls1 Hhd.
1.3368	2310	10 Gals 1 Anker.	16.84	29106	2 Hhds1 Pipe.
2.406	4158	18 Gals 1 Runlet.	83.68	58212	2 Pipes1 Tun.
5.614	9702	42 Gals 1 Tierce.			

The U. S. Standard Gallon contains 231 cubic in.—8½ lbs. avoirdup's.
"Imperial" 277.274 "—1.2 U. S. gallons.
" old Beer Measure" 282 "

In measuring tanks, reservoirs, etc., it will be sufficiently accurate to regard one cubic foot—7½ U. S. or 6½ Imperial gallons.

The contents of a circular tank, in barrels of 31½ gallons,—the square of the diameter (in ft.) multiplied by the depth, mul. by .1865.

The number of U. S. gallons in a round tank=the square of the diameter, in feet, x by the depth x 5%.

The number of U. S. gallons in a round tank, wider at one end than the other,=% the sum of the squares, plus the product of the two end diameters, in feet,×the depth×5%.

For Imperial gallons × 4.9 or 4.89469.

#### GAUGERS' WORK.

To find the contents of a cask in gallons.

RULE.—Add two-thirds the difference of the head and bung diameters to the head diameter, to find the mean diameter; then multiply the product of the square of the mean diameter into the length, all in inches, for U.S. Gallons × .0034, for Imperial gallons × .0029, for Ale gallons × .0028.

Note.—If the staves are but little curved, add .6 instead of 3.

How many U.S. gallons in a cask, length 40 in., head diameter 21 in. and bung diameter 30 in.?

- $.21+(\overline{30-21}\times\frac{2}{3})=27$  in. mean diameter.
- ... $27^2 \times 40 \times .0034 = 99.144$  gallons, Ans.

Or  $27^2 \times 40 \times .0029 = 84.564$  Imperial gallons.

# DRY MEASURE, IMP. AND U. S. STANDARD. For measuring Grain, Fruit, Roots, Coal, etc.

IMP. CU. IN.	U. S.	PT.	QT.	GAL. PK.		PR. BU.		QR.		
34.659	83.60	1				ļ			1	Pint.
69.318	67.20	2	1		<b> </b> .	<b></b>		<b></b> .	1	Quart,
277.274	268.80	8	4	1				<b> </b>	1	Gallon.
554.548	537.60	16	8	2	1	<b> </b>			1	Peck.
2218.192	2150.42	64	82	8	4	1			1	Bushel.
8872.768	8601.68	256	128	32	16	4	1		1	Coomb.
17645.536	17208.36	512	256	64	82	8	2	1	1	Quarter.
70582,144	68813.44	2048	1024	256	128	32	8	4	1	Chaldron.
	77415.12	2304	1152	288	144	36	or c	OAL	1	Chaldron.

The U. S. Standard Bushel contains 2150.42 cubic inches. The Imperial English " 2218.192 " "

A cylinder 1814 inches in diameter, 8 inches deep= 1 Bushel.

5 Stricken measures = 4 heap measures.

Cubic feet x.8 = U. S. bushels nearly; add 44.5 for every 10,000 bushels.

Cubic feet  $\times$ .779 = Imperial bushels nearly.

Imperial Bushels $\times$ 1.03152 the Product=U. S. Bushels.

U. S. Bushels × .969444 the Product=Imperial Bushels.

Any three factors that will produce the number of inches in a given quantity, will be the inside dimensions of a box to hold that quantity; hence a box  $11.2\times16\times12$  in., will contain 1 Standard Bushel. 824 cu. inches = 4 Liquid Gallons; therefore a box  $12\times7\times11$  inches will contain 4 gallons.

An open box made with the greatest economy of material; the altitude= the radius of the Base; if with a cover the altitude= the base.

The number of bushels  $+ \frac{1}{2}$  = the number of cubic feet.

The number of cubic feet-1-5=the number of Bushels. U.S.

The price per cental=the price per bushel×100:the number of pounds in the bushel. See page 75.

It is usual—with some local exceptions—to estimate the number of pounds to the bushel, as follows: Bran, 20 lbs.; Oats, 32 lbs; Barley, 48 lbs.; Maize and Rye, 56 lbs.; Wheat, Beans, Clover Seed, and Potatoes, 60 lbs.

### DIAMOND WEIGHT.

ASSAYERS' WEIGHT.

16 Parts = 1 Grain.

240 Grains = 1 Carat.

4 Grains = 1 Carat.

2 Carats = 1 Ounce.

1 Carat = 31-5 Troy grs. (nearly.) 24 Carats = 1 Pound.

The term Carat is also employed in estimating the fineness of Gold and Silver; when perfectly pure the metal is said to be "24 Carats fine." English Gold coin is 22 carats fine, that is, it consists of 22-24 pure gold, and 2-24 alloy.

To compute the fineness in thousandths, and the weight in ounces and thousandths is simpler, and admits of very minute subdivisions with great facility.

The coining of gold or silver does not change the REAL value of cither; it stamps each piece of metal with a national, official certificate of its weight and fineness.

From one Troy pound of gold 22 carats, or .916 2-3 fine 46 29-40 Sovereigns are made, each weighing 123.27448 grains = 113.001605 grains of fine gold = \$4.866563.

1 ounce of U. S. Standard Gold = \$18.00465 = £3.8230 = £3,16,, 5½

1 "British" = 18.94918 = 3.8938 = 3,17,10½

1 "British" = 18.94918 = 3.8938 = 3,17,,101/4
1 "Pure "= 20.67184 = 4.248 = 4,, 4,,111/4

Thousandths of an ounce  $\div$  100  $\times$  48 = grains.

Grains  $\times$  100  $\div$  48 = thousandths of an ounce.

U. S. Standard ounces of Gold - .05375 = U. S. Dollars.

U. S. Gold Dollars  $\times$  .05375 = Standard ounces.

To multiply by .05375, remove the point one place to the left and divide by 2, divide this quotient by 20, and the second quotient by 2; the sum of the quotients is the answer.

EXAMPLE.—How many ounces in one U. S. Gold dollar?

20 .05 2 .0025 .00125 .05375

Ans. .05375 ozs. `

The weight of gold, in ounces, and the fineness being given, to find its value in U. S. Gold Coin.

RULE.—Multiply the weight by twice the fineness, multiply by 10 and divide the product by 30, and the quotient by 129; the sum of the product and the quotients is the answer.

EXAMPLE. - Find the value of one ounce of gold 9-10 fine.

30 18. 129 .6 .00465 18.60465

Ans. \$18,60465.

Or multiply the given weight by the fineness  $\times$  1000  $\times$  8, and divide the product by 387.

$$1 \times .9 \times 1000 \times 8 \div 887 = 18.60465$$
.

The fineness and weight of Silver being given, to find its value in U. S. Silver dollars 9-10 fine, 4121/2 grains weight.

Rule.—For pure silver, if in grains, divide by  $9\times10\times11\times3$  and multiply by 8, or divide by  $.9\times412.5$ .

Example.—Pure silver, grains  $371.25 \times 8 \div 9 \times 10 \times 11 \times 3 = $1$ .

If in ounces, divide the weight and fineness by  $.9 \times .895375$ .

Or multiply the given weight by the fineness and by 1.28; repeat the figures in the product, under, and two places to the right, as often, and to as many decimal places as the answer requires; the sum is the answer.

Example. - Find the value in silver dollars of 1 oz. of silver 9-10 fine.

$$1 \times .9 \times 1.98 = 1.152$$
 $1152$ 
 $1152$ 

\$1,1636352 Ans.

To make a compound of any weight and fineness.

RULE. Divide the fineness sought by the fineness to be alloyed; the quotient is the weight required to make a compound of one ounce of the desired fineness.

EXAMPLE.—Required to make a compound of one ounce 14 carats fine by alloying gold 22 carats fine.

 $14 \div 22 = .68636 \text{ gold} + .86364 \text{ alloy} = 1 \text{ ounce.}$ 

To find how many ounces of a lower fineness must be added to one ounce of a higher fineness to make a compound of any given fineness.

RULE.—Divide the difference of the two higher by the difference of the two lower finenesses.

EXAMPLE.—Required a compound of 14 Carats fine by mixing 12 carat fine with 21 carat fine.

$$21 - 14 = \frac{7}{14 - 12} = 3\frac{1}{2}$$
.  $3\frac{1}{2}$  oz. 12 fine  $+ 1$  oz. 21 fine  $= 4\frac{1}{2}$  oz. 14 Carat fine.

The silver dollar weighs 4121/4 grains, nine-tenths of which is pure silver. At the English mint, a mixture of 11 ozs., 2 pwts. of pure silver, with 18 pwts. of alloy, is coined into 66 shillings. When English coin silver is worth 54 pence an ounce, in gold, and the pound stg. (gold) is worth \$4,86 in United States gold, what is the value in U. S. gold coin of the silver contained in the dollar? (The value of the alloy in the English silver is not to be considered.

11 ozs., 2 pwts. = 
$$\frac{222}{240}$$
 = .925 of an ounce. Ans. 89½ cts.

54 pence = £0.225. 
$$225 \times 4.86 = 1.0985$$
.  $\frac{1.0985 \times 412.5 \times .9}{490 \times .925} = .895$ 

SEC.	MIN.	HRS.	DA.	wĸ.		,
3600	1	1			1	Minute.
86400	1440	24	1		1	Day,
604800 81536000 <sup>1</sup>	10080 525600	168 8760	365	1 52	1	Week, Common Year,
31622400	527040	8784	366		1	Leap Year.

Time is a measured portion of duration, the unit of which is the mean solar day.

12 Calender months = 13 lunar months = 1 year.

365 days, 5 hrs. 48 minutes, 50 seconds = 1 Solar year.

10 years = 1 decade. 10 decades = 1 century.

400 years = 146,097 days, a number exactly divisible by 7.

The civil day begins and ends at 12 o'clock, Midnight.

The Astronomical day begins and ends at 12 o'clock, Noon.

As the year contains 365½ days, nearly, we reckon three years in every four as containing 365 days, and the fourth, leap year, as containing 366 days; the leap year is always a multiple of 4.

The even centuries not divisable by 400 are not leap years.

Formerly the new year began on the 25th of March and was so reckoned in England until 1753.

In ordinary business computations, 1 year = 12 mos. = 360 ds. 1 month = 30 days.

$$+1$$
  $-2$   $+1$   $+1$   $+1$   $+1$   $+1$   $+1$  Jan. Feby. Mar. Apl. May, June, July, Aug. Sept. Oct. Nov. Dec.

In the common year February has two days less than 30, in leap year 1 day less; seven months have one day more.

To find the exact number of days between two dates.

Multiply the number of entire months by 3, call the product tens; add the extra days, and 1 day for each month of 31 days; when Feb'y occurs, deduct 2 days for the common, and 1 day for Leap year.

How many days from 1st of the 4th month to 9th of the 11th month. 11 mo. -4 mo. = 7 mo.  $= 7 \times 30 + 9 + 4 = 223$  days.

	st of Counterfeit Bank Notes.
ONES.	New York, N. Y Mechanics'
Boston, Mass:Nat. Eagle	New York, N. Y Mechanics' New York, N. Y Merchants'
TWOS.	New York, N. Y. N. B. of Com're New York, N. Y. N. B. State N. Y New York, N. Y Union Philadelphia, Pa First
	New York, N. Y. N. B. State N. Y
Kinderhook, N. Y. Nat. Un'n 1 Linderpark, N. Y. Nat. union	New York, N. YUnion
1 Linderpark, N. Y. Nat. union	Philadelphia, PaFirst
Newport, R. I. N. B. of R. I. New York, N. Y Ninth New York, N. Y Marine New York, N. Y Market New York, N. Y. St. Nicholas	Philadelphia, Pa. Third Poughkeepsie, N. Y. First Poughkeepsie, N. Y. City Poughkeepsie, N. Y. First Red Hook, N. Y. First
New York, N. Y Ninth	Poughkeepsie, N. YFirst
New York, N. Y Marine	Poughkeepsie, N. YCity
New York, N. Y Market	Poughkeepsie, N.Y. F' mr's & Mf'
New York, N. Y. St. Nicholas	Red Hook, N. Y First
Peekskill, N.Y.Westchst'r Co	Richmond, Ind Richmond
•	Rochester, N. Y Flour City
FIVES.	Rome N V Central
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2 Aurora, IllFirst	Tron N V Matrol
Docton Mass Clobs	Troy, N. YMutual Waterford, N.Y. Saratoga County
Boston, Mass Pacific	wateriord, N. I. Saratoga County
2 Canton, IllFirst	8 Watkins, N. Y Watkins
1 Cecil, IllFirst	TWENTIES.
2 Chicago, IllFirst	Indianapolis, IndFirst
8 Chicago, IllCentral	New York N V First
8 Chicago, III	Now York N V Market
8 Chicago, IllGerman	Now York N V Morehente
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Dedham, Mass Dedham	New Tork, N. 1 Tradesmen's
Fall River, Mass Pocasset	8 Philadelphia, Pa Fourth
1 Galena, IllFirst	Portland, ConnFirst 1 Utica, N. YCity
2 Hanover, PaFirst Jackson, MichPeople's	1 Utica, N. YCity
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4 Payton Ill First	New York, N. Y Metropolitan
9 Porn Ill First	New York, N.Y. N. B. of Com'rc
Rome N V Fort Stanwix	New York, N. Y. Nat. Broadway
Southbridge Mess Southbr	New York, N. YTradesmen's New York, N. YUnion
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2 Tamaqua, PaFirst 2 Troy, N. Y National State	ONE HUNDREDS.
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2 Westfield, MassHampden	Boston, MassFirst
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Newburg, N. 1 Highland	1 No such bank.
New York, N. Y First	2 All notes of this bank of this de-
1 New York, N. Y American	nomination are replaced by notes of
8 New York, N. Y Croton	other denominations.
Lockport, N. Y. First Muncie, Ind. Muncie Newburg, N. Y. Highland New York, N. Y. First 4 New York, N. Y. American 8 New York, N. Y. Croton New York, N. Y. Marine New York, N. Y. Market	8 Failed, and notes being retired.
New York, N. Y Market	4 Notes are being retired.

### MISCELLANEOUS.

How many strokes does a clock strike in 12 hours?

$$\frac{\overline{12+1}\times 12}{2} = 78 \text{ strokes.} \qquad \frac{\cancel{3}}{\cancel{3}}$$

How many barrels in a triangular pile, 49 barrels at the base and 1 at the top?

$$\frac{49+1\times49}{2}=1225$$
 barrels.

O'Leary with ten tramps have two days start, and make 8 miles a day; how long will it take Rowell with 5 trampers travelling 10 miles a day to overtake O'Leary and his men?

$$16 \div 2 = 8$$
 days.

The sum of two numbers is 140; the larger is to the smaller as 1 to 5, what are the numbers?

$$\frac{9}{9} + \frac{5}{9} = \frac{14}{9} \qquad \frac{140 \times \frac{6}{14} = 90}{140 \times \frac{5}{14} = 50} = 140$$

A Bin 9 ft. 6 in. long, 6 ft. wide, 4 ft. 3 in. deep, will hold how many Imperial bushels.

$$\frac{19}{2} \times \frac{6}{1} \times \frac{17}{4} \times \frac{8}{10} - 4.845 = 188.955$$
 bushels. Ans.

NOTE. The imperial bushel is 2218.192 Inches, ten eighths of a foot, nearly, deduct 2½ from every 100 bushels in the product, this result multiplied by 8 will be the number of Imp. gallons,

What is the cost of 732 lbs. of Coal at \$14. per ton, 2240 lbs. to the ton?

$$\frac{732\times14}{8\times4\times7}$$
 =\$4.575. Ans

A bin 9 ft, 6 in. long, 6 ft. wide, and 4 ft. 8 in. deep is full of wheat, what is its value at \$2.05 & bushel?

$$\frac{19}{2} \times \frac{6}{1} \times \frac{1}{4} \times \frac{6}{10} + .87 \times 2.05 = $399.07$$
. Ans.

Note. The standard bushel is 2150.42 inches; ten-eighths of a foot, nearly, the difference is .44 bu. in each 100. R.259,

Divide £1 into 3 parts in the proportion of A,  $\frac{1}{2}$ , B,  $\frac{1}{3}$ , C,  $\frac{1}{4}$ . 6+4+3=13.

12 Ans. \(\frac{a}{13}\), \(\frac{a}{13}\), \(\frac{a}{13}\), \(\frac{a}{13}\), \(\frac{a}{13}\), \(\frac{a}{13}\).

How many cubic feet in a case 3 ft. 6 in. by 2 ft., 8 in. by 1 ft. 10 in?

$$\frac{7}{2} \times \frac{8}{3} \times \frac{1}{9} = 17 \frac{1}{9} \text{ ft. Ans.}$$

If 7 cats, kill 7 rats, in 7 minutes, how many cats will kill 100 rats in 50 minutes?

$$\frac{7\times7\times100=14.}{7\times50}$$

Ans. 14 cats.

If it cost \$24 to carry 6 tons 20 miles, what will it cost to carry 12 tons 120 miles?

$$24 \times 12 \times 120 = 288.$$

$$6 \times 20$$

Ans. \$288.

How many bricks will pave a walk 200 ft. long, by,16 feet; bricks 8 in., by 4 in?

$$\frac{200 \times 16 \times 3 \times 3}{2 \times 1} = 14,400.$$
 Ans. 14400 bricks.

Multiply £19 19s. 113d by 1918 110 000.

$$\frac{(£19,19,11\frac{3}{4}-£_{9\frac{1}{6}0})\times20+£_{(9\frac{1}{6}0})^{2}}{£399\frac{19}{26}\frac{24}{240}\frac{24}{99\frac{1}{600}}}$$
or  $\frac{£399\frac{19}{26}\frac{24}{240}\frac{24}{99\frac{1}{600}}}{£399,19,2\frac{1}{9\frac{1}{60}}}$  of a farthing.

Multiply 66 by 
$$\frac{2}{3}$$
: 22  $\frac{66 \times 2}{3}$  = 44.

Divide 66 by 
$$\frac{3}{3}$$
: 33  $\frac{66 \times 3}{2}$  = 99 56

Divide  $168 \times 2 \times 7$  by  $7 \times 3$ :  $\frac{7 \times 2 \times 168}{7 \times 3} = 112$ .

Divide £99 amongst 3 persons, A to have  $\frac{1}{12}$ , B  $\frac{1}{12}$ , and C  $\frac{1}{12}$ .

$$II \mid {}^{999}_{5} \mid II \mid {}^{999}_{4} \mid II \mid {}^{999}_{2} \mid A£45, B£36, C£18.$$

Two merchants load a ship with goods worth £5000, A owns £3500, and B the rest; the goods suffer damage valued at £1000, what is each man's share of the loss?

$$5000 \mid 1000 \atop 3500$$
  $5000 \mid 1000 \atop 1500$  A loses £700. B , £300.

B and C gain by trade £182; B put in £300, and C £400, what is the gain of each?

A person owning  $\frac{3}{2}$  of a mine sells  $\frac{3}{4}$  of his share for £1710, what is the value of the whole mine?

$$190 \quad \frac{\cancel{17\cancel{10}} \times 4 \times 5}{\cancel{3} \times \cancel{3}} = \cancel{£}3800.$$

How much money will buy  $\frac{3}{4}$  of  $\frac{3}{4}$  of a mine worth £3800?

$$\frac{3}{8} \times \frac{3}{8} = \frac{9}{20} \qquad \frac{3800 \times 9}{20} = £1710.$$

If  $\frac{1}{3}$  of 6 be 3, what will  $\frac{1}{4}$  of 20 be?

$$\frac{3 \times 3 \times \cancel{20}5}{2 \cancel{0} \times \cancel{4}} = 7\frac{1}{2}.$$

A compositor can set 20 pages in  $\frac{2}{5}$  of a day, another could set 20 pages in  $\frac{3}{4}$  of a day, how long will it take the two men working together to do the work?

$$\frac{4}{3} + \frac{5}{2} = \frac{23}{6}$$
  $\frac{23}{6}$  inverted  $= \frac{6}{23}$  of a day.

A cistern has 5 faucets; the first will fill it in 1 hour, the second in two, the third in 3, the fourth in 4, and the fifth in 5 hours; in what time will the cistern be filled, all the faucets running at once?

$$\frac{60+30+20+15+12}{60} = \frac{137}{60} \quad \frac{137}{60} \text{inv.} = \frac{60}{137} \text{ of an h'r.}$$

A says to B, give me \$7 and I shall have as much money as you; B replies, give me \$7 and I shall have twice as much as you; how much money had each?

$$7 \times 5 = 35$$
  $7 \times 7 = 49$  A \$35, B \$49.

How many different pairs can be made with 7 units?

$$\frac{7\times6}{2}=21$$
 pairs.

How many bricks,  $8\times4\times2$  inches, in a wall  $160\times20\times2$  feet?

$$\frac{160\times20\times2\times3\times3\times6}{2\times1\times1} = 172,800 \text{ bricks.}$$

How many shingles for a roof 60 ft. long, rafters 20 feet, two sides, shingles to show  $6\times 4$  inches.

$$\frac{60\times20\times2\times2\times3}{1\times1} = 14,400 \text{ shingles.}$$

If 21<sup>3</sup>/<sub>4</sub> bushels of oats will seed 9<sup>3</sup>/<sub>3</sub> acres, how many bushels will seed 100 acres?

$$\frac{87\times3\times100}{4\times29} = 225 \text{ bushels.}$$

How many 16ths are there in .85?

$$\frac{.85 \times 16}{100} = 13.6$$

\$150 is due Jan. 1st., \$78 is paid down, on July 1st., the account is settled by paying \$78. What rate per cent is paid for the accommodation?

\$150—78=\$72. 
$$\frac{6\times2\times100}{72}$$
=163 per cent.

Find the value of an ounce of silver, gold being worth £3,,18,,7 per ounce, ratio 15½ to 1.also 16 to 1.

£3,,18,,7 
$$\div$$
15½=60¾4d. £3,,18,,7 $\div$ 16=58¼4d.

To find the amount in 365 days of any given number of pence per day: Multiply the given number of pence by 1½, call it pounds, and add the product of the pence multiplied by 5.

DICE.—The number of different combinations that can be made with any given number of dice is equal to a power of 6, equal to the given number of Dice.

How much is due to a man working 22 days, at \$39 per month of thirty days; also 26 working days to the month?

$$\frac{39 \times 22}{30} = \$28.60. \qquad \frac{39 \times 22}{13 \times 2} = \$33.$$

Find the charges on 1000 cases, each  $16 \times 12 \times 6$  inches, at 16 shillings per ton of 40 feet.

$$\frac{1000 \times 4 \times 1 \times 1 \times 16}{3 \times 1 \times 2 \times 40} = 266.67s = £13 \text{ 6s. 8d.}$$

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### Howard's Copyright Perpetual Calendar-

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## THIS BOOK IS DUE ON THE LAST DATE STAMPED BELOW

### AN INITIAL FINE OF 25 CENTS

WILL BE ASSESSED FOR FAILURE TO RETURN THIS BOOK ON THE DATE DUE. THE PENALTY WILL INCREASE TO 50 CENTS ON THE FOURTH DAY AND TO \$1.00 ON THE SEVENTH DAY OVERDUE.

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